

TABLE 4.6—SUMMARY OF FRICTIONAL PRESSURE LOSS EQUATIONS*

	Newtonian Model	Bingham Plastic Model	Power-Law Model	
Mean Velocity, \bar{v}	<u>Pipe</u> $\bar{v} = \frac{q}{2.448d^2}$	$\bar{v} = \frac{q}{2.448d^2}$	$\bar{v} = \frac{q}{2.448d^2}$	
	<u>Annulus</u> $\bar{v} = \frac{q}{2.448(d_2^2 - d_1^2)}$	$\bar{v} = \frac{q}{2.448(d_2^2 - d_1^2)}$	$\bar{v} = \frac{q}{2.448(d_2^2 - d_1^2)}$	
Flow Behavior Parameters	$\mu = \theta_{300}$	$\mu_p = \theta_{600} - \theta_{300}$ $\tau_y = \theta_{300} - \mu_p$	$n = 3.32 \log \frac{\theta_{600}}{\theta_{300}}$ $K = \frac{510 \theta_{300}}{511^n}$	
	Turbulence Criteria	<u>Pipe</u> $N_{Re} = 2,100$ $N_{Re} = \frac{928 \rho \bar{v} d}{\mu}$	$N_{He} = \frac{37,100 \rho \tau_y d^2}{\mu_p^2}$ $N_{Re} \text{ from Fig. 4.33}$ $N_{Re} = \frac{928 \rho \bar{v} d}{\mu_p}$	$N_{Re} \text{ from Fig. 4.34}$ $N_{Re} = \frac{89,100 \rho \bar{v}^{2-n}}{K} \left(\frac{0.0416d}{3+1/n} \right)^n$
<u>Annulus</u> $N_{Re} = 2,100$ $N_{Re} = \frac{757 \rho \bar{v} (d_2 - d_1)}{\mu}$		$N_{He} = \frac{24,700 \rho \tau_y (d_2 - d_1)^2}{\mu_p^2}$ $N_{Re} = \frac{757 \rho \bar{v} (d_2 - d_1)}{\mu_p}$	$N_{Re} \text{ from Fig. 4.34}$ $N_{Re} = \frac{109,000 \rho (\bar{v})^{2-n}}{K} \left[\frac{0.0208(d_2 - d_1)}{2+1/n} \right]^n$	
Laminar Flow Frictional Pressure Loss		<u>Pipe</u> $\frac{dp_f}{dL} = \frac{\mu \bar{v}}{1,500 d^2}$	$\frac{dp_f}{dL} = \frac{\mu_p \bar{v}}{1,500 d^2} + \frac{\tau_y}{225 d}$	$\frac{dp_f}{dL} = \frac{K \bar{v}^n \left(\frac{3+1/n}{0.0416} \right)^n}{144,000 d^{1+n}}$
		<u>Annulus</u> $\frac{dp_f}{dL} = \frac{\mu \bar{v}}{1,000 (d_2 - d_1)^2}$	$\frac{dp_f}{dL} = \frac{\mu_p \bar{v}}{1,000 (d_2 - d_1)^2} + \frac{\tau_y}{200 (d_2 - d_1)}$	$\frac{dp_f}{dL} = \frac{K \bar{v}^n \left(\frac{2+1/n}{0.0208} \right)^n}{144,000 (d_2 - d_1)^{1+n}}$
Turbulent Flow Frictional Pressure Loss	<u>Pipe</u> $\frac{dp_f}{dL} = \frac{f \rho \bar{v}^2}{25.8 d}$	$\frac{dp_f}{dL} = \frac{f \rho \bar{v}^2}{25.8 d}$	$\frac{dp_f}{dL} = \frac{f \rho \bar{v}^2}{25.8 d}$	
	or	or		
	$\frac{dp_f}{dL} = \frac{\rho^{0.75} \bar{v}^{1.75} \mu^{0.25}}{1,800 d^{1.25}}$	$\frac{dp_f}{dL} = \frac{\rho^{0.75} \bar{v}^{1.75} \mu_p^{0.25}}{1,800 d^{1.25}}$		
	<u>Annulus</u> $\frac{dp_f}{dL} = \frac{f \rho \bar{v}^2}{21.1 (d_2 - d_1)}$	$\frac{dp_f}{dL} = \frac{f \rho \bar{v}^2}{21.1 (d_2 - d_1)}$	$\frac{dp_f}{dL} = \frac{f \rho \bar{v}^2}{21.1 (d_2 - d_1)}$	
or	or			
$\frac{dp_f}{dL} = \frac{\rho^{0.75} \bar{v}^{1.75} \mu^{0.25}}{1,396 (d_2 - d_1)^{1.25}}$	$\frac{dp_f}{dL} = \frac{\rho^{0.75} \bar{v}^{1.75} \mu^{0.25}}{1,396 (d_2 - d_1)^{1.25}}$			

* Alternate turbulence criteria are to assume the flow pattern which gives the greatest frictional pressure loss.

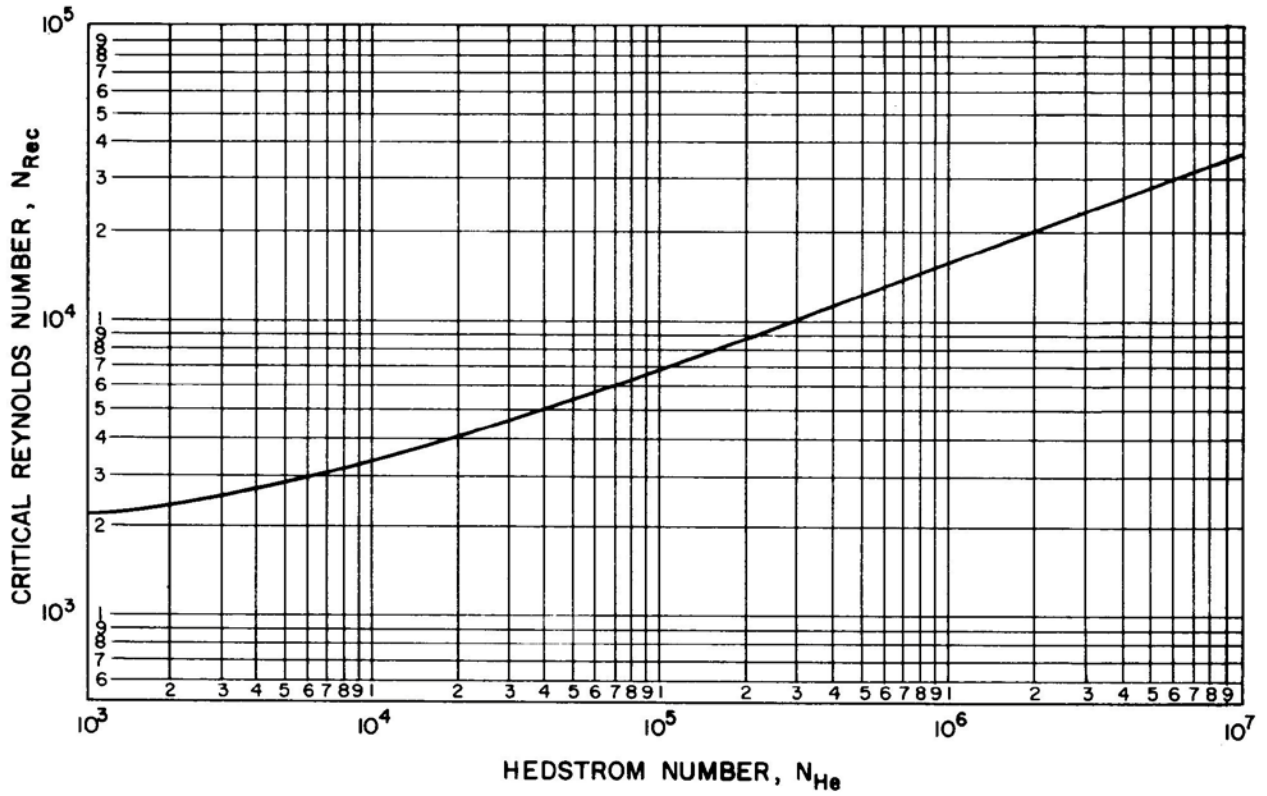


Fig. 4.33—Critical Reynolds numbers for Bingham plastic fluids.

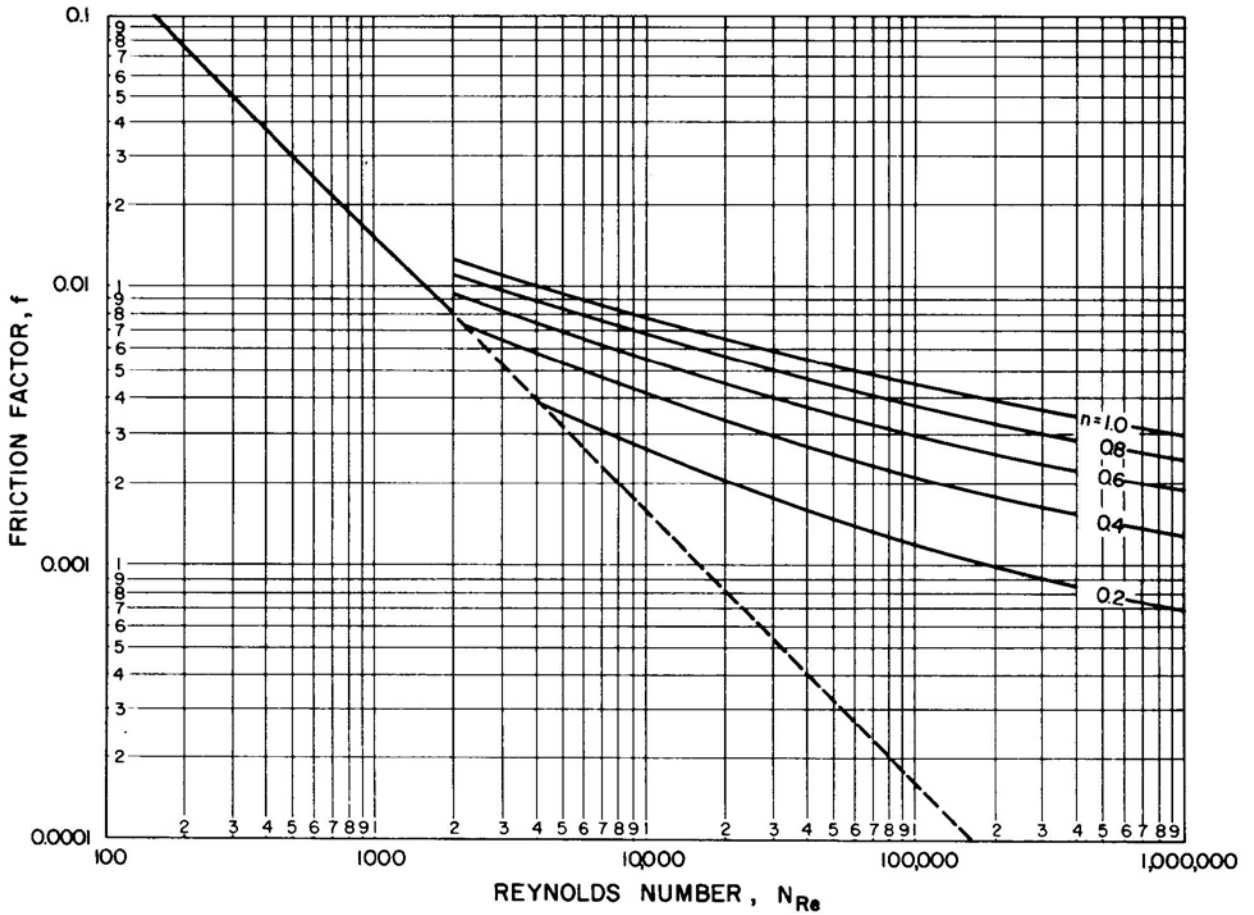


Fig. 4.34—Friction factors for power-law fluid model.

