

Cosmology's Century

Large Scale Structure of Dark Universe

Shant Baghram

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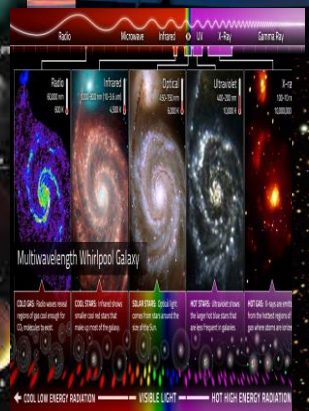
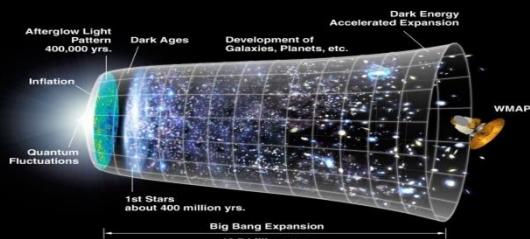
Colloquium 16 May 2021

Manoucher Yektai (1921 –2019)

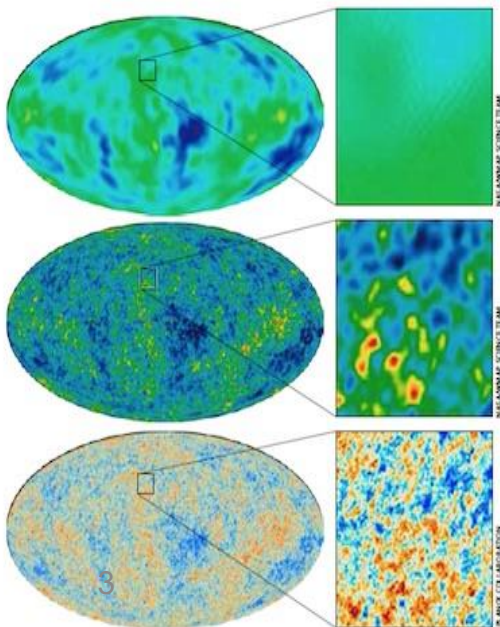


Overture*

**Overture* in music was originally the instrumental introduction to a ballet, opera, or oratorio.



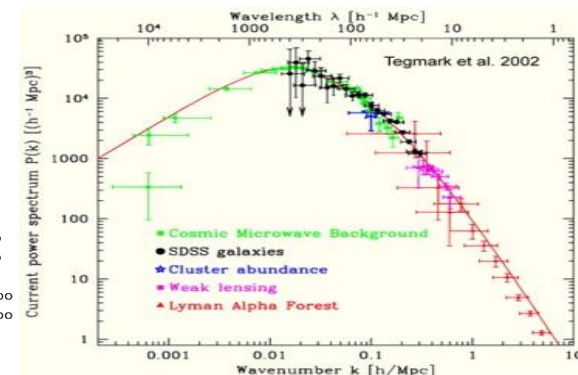
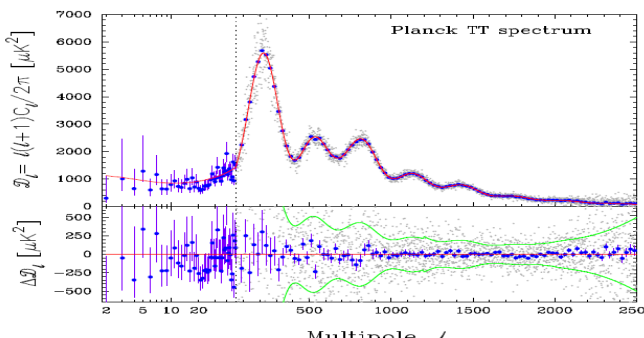
CLOSE-UP VIEWS OF THE CMB

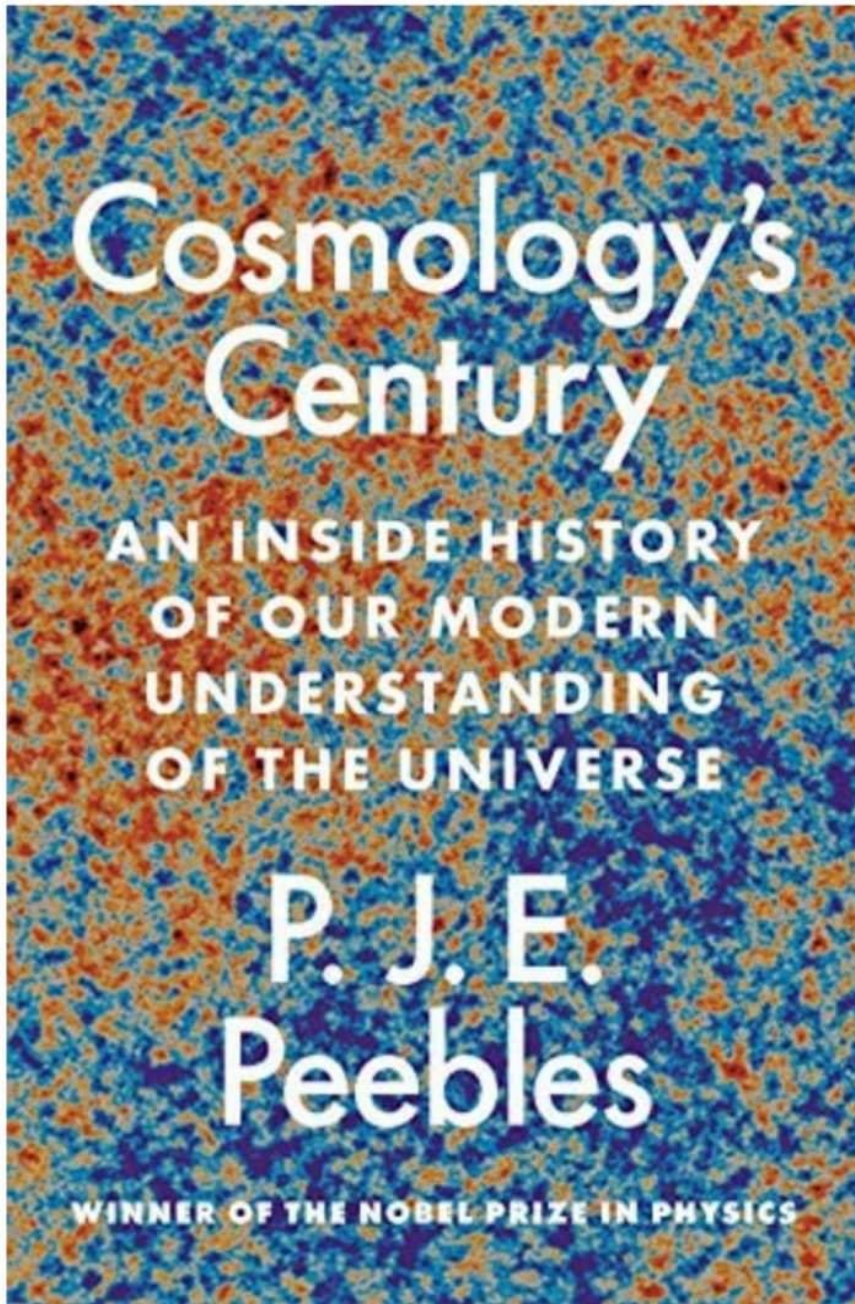


COBE: 1990 map
Resolution: 7°

WMAP: 2013 map
Resolution: 0.5°
(5 times more sensitive than COBE)

Planck: 2013 n
Resolution: 0.1°
(15 times more sensitive than COBE)





You should enter science because you are fascinated by it. That's what I did!
James Peebles

Prelude*

**A prelude is a short piece of music, the form of which may vary from piece to piece.
The prelude may be thought of as a preface*

“If you wish to make an apple pie from scratch you must first invent the universe.” by Carl Sagan

6 Lines of Thought to 6 parameter model

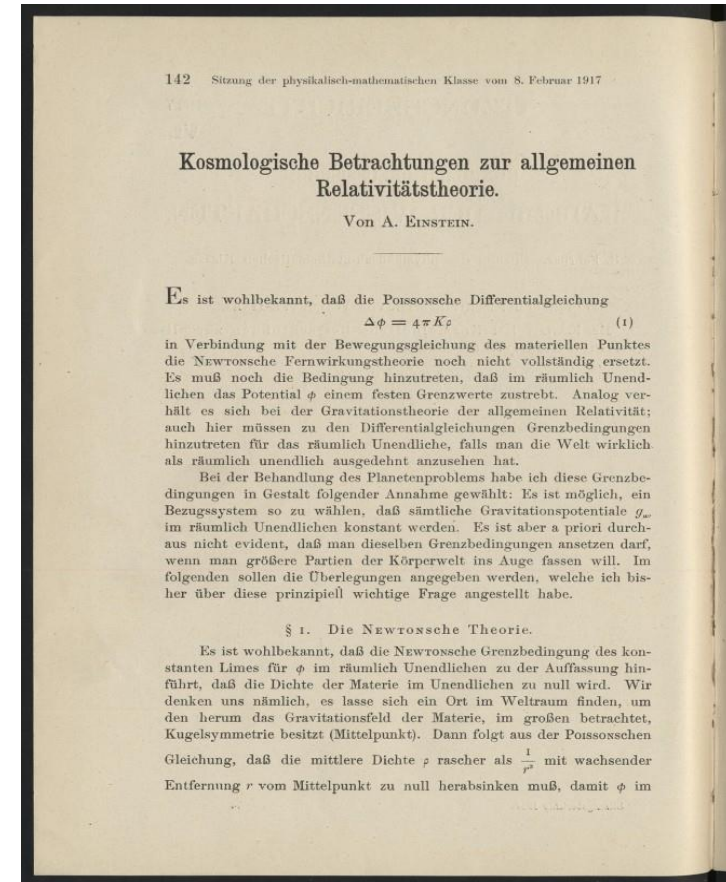
I. General relativity and the Universe

Asking for a Homogenous and Isotropic one!

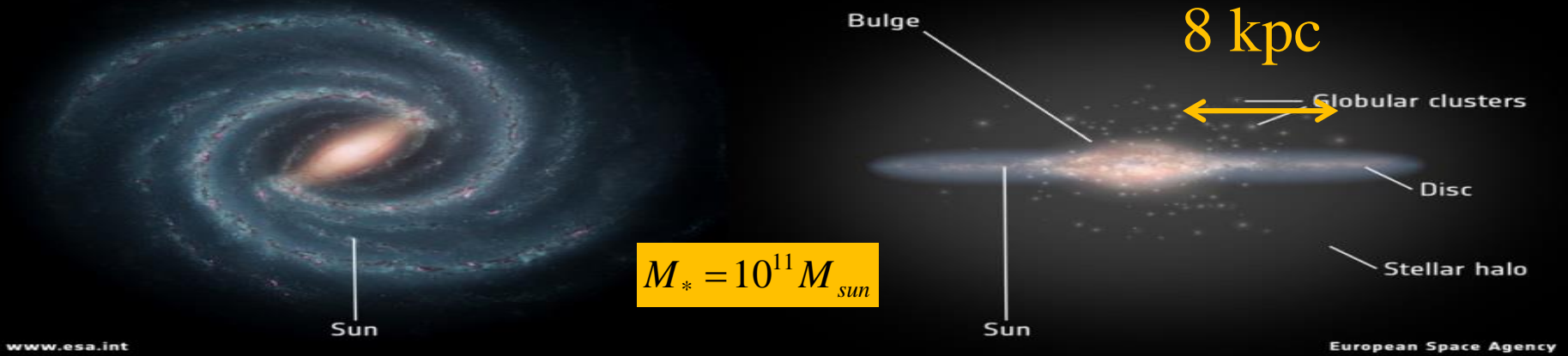
GR+ Homogenous and Isotropic Universe (Einstein Cosmological Principle ECP)

- Nonempirical theory assessment
- From solar system to the Universe

$$R_{\mu\nu} - \frac{1}{2} g_{\mu\nu} R = \frac{8\pi G}{c^4} T_{\mu\nu}$$



$$ds^2 = -c^2 dt^2 + a^2(t) \left[\frac{dr^2}{1 - kr^2} + r^2 (d\theta^2 + \sin^2 \theta d\varphi^2) \right]$$



$1 \text{ parsec} = 3.26 \text{ ly} = 3.1 \times 10^{16} \text{ meter}$



Empirical Evidence of ECP

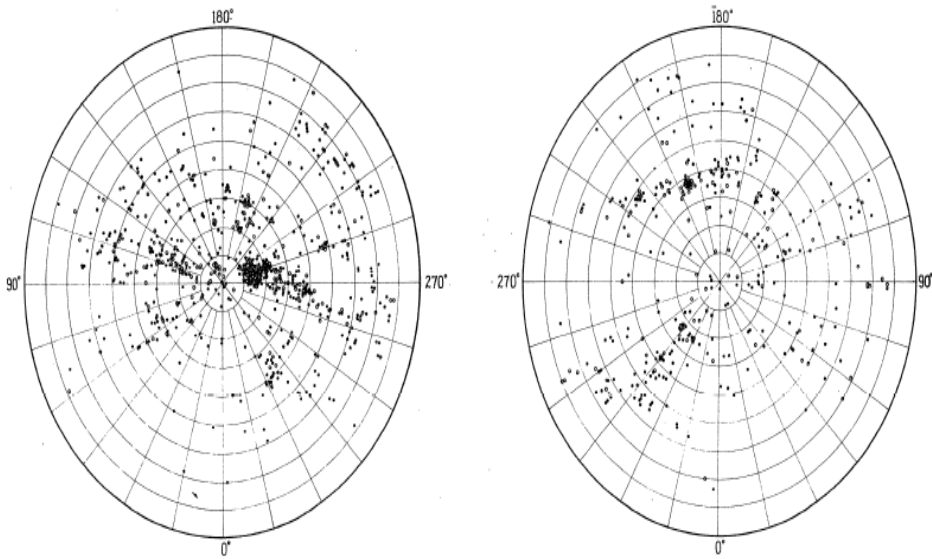


FIGURE 2.2. The Shapley and Ames (1932) map of galaxies brighter than apparent magnitude 13. Courtesy of the John G. Wolbach Library, Harvard College Library.



(1871-1952) Harlow Shapley

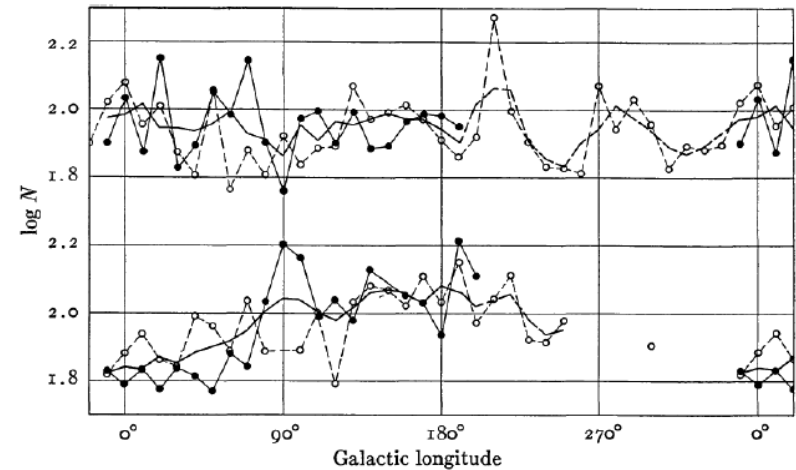
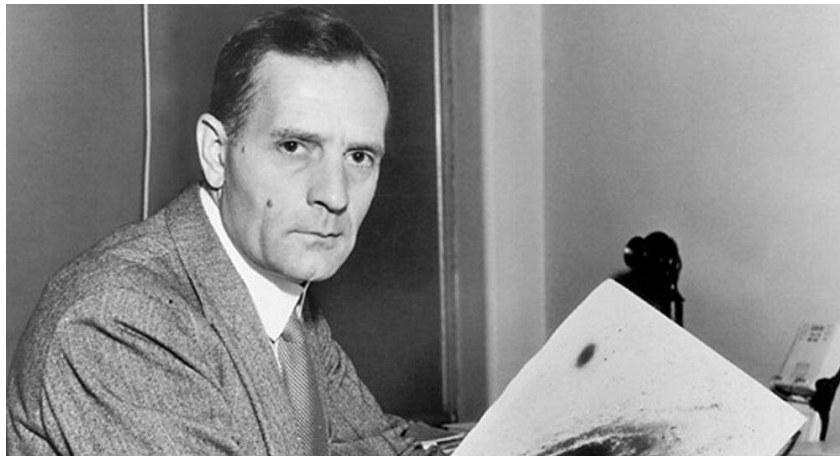


FIGURE 2.3. Hubble's (1934) counts of galaxies at high galactic latitudes in the upper curves, and at low latitudes in the lower curves. © AAS. Reproduced with permission.

Empirical Evidence of ECP

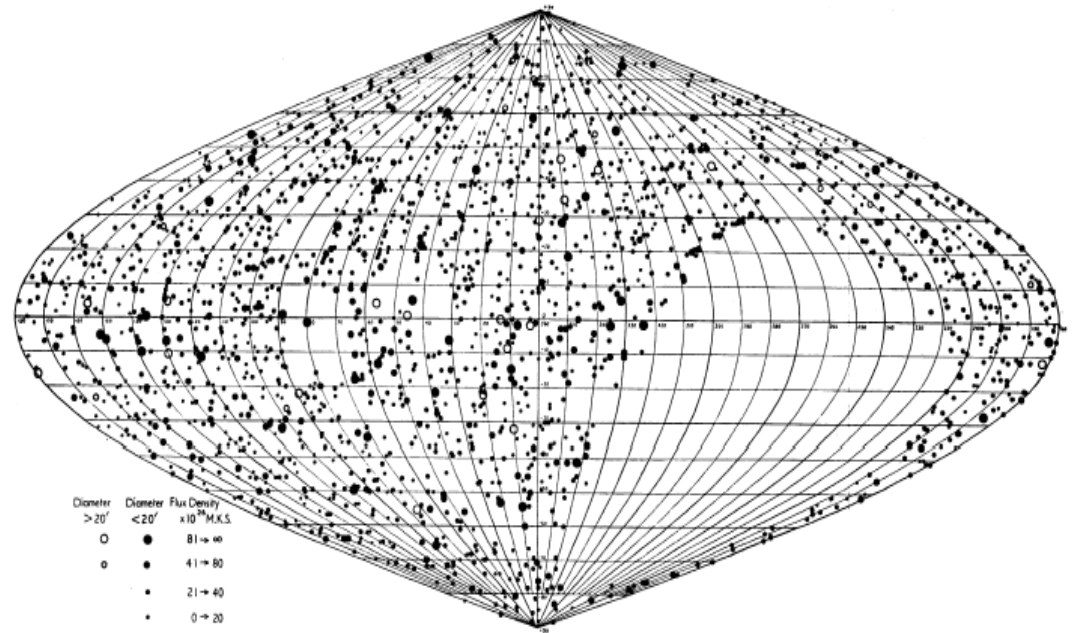
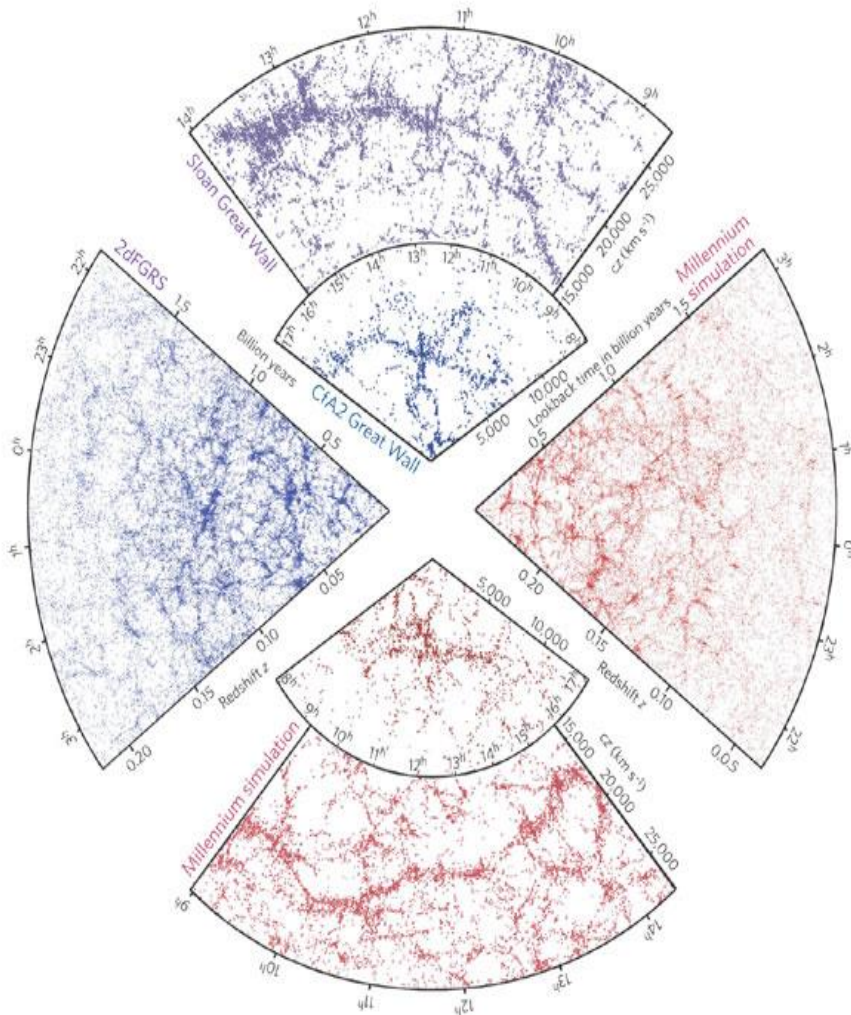


FIGURE 2.4. The Second Cambridge Catalog of Radio Sources (Shakeshaft, Ryle, Baldwin, et al. 1955).

One antenna of the One-Mile Telescope (left), two of the Half-Mile Telescope (centre) and the remains of the 4C Array (right)

Empirical Evidence of ECP



The Sloan Digital Sky Survey or SDSS is a major multi-spectral imaging and spectroscopic redshift survey using a dedicated 2.5-m wide-angle optical telescope at Apache Point Observatory in New Mexico

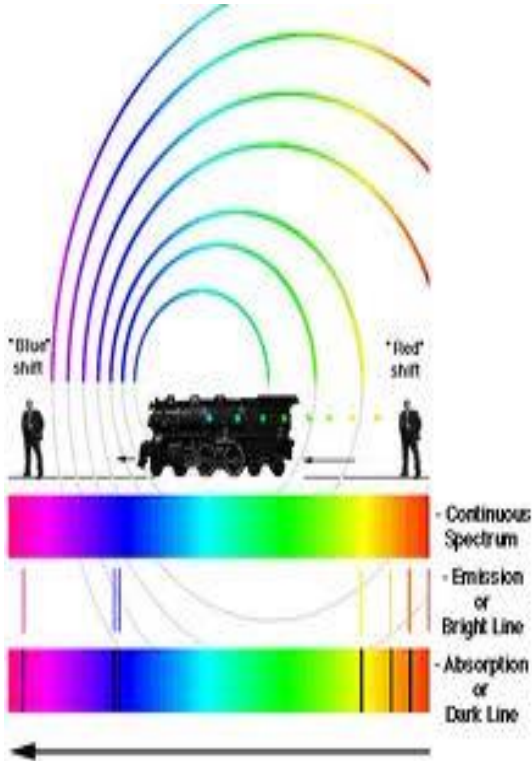
6 Lines of Thought to 6 parameter model

I. General relativity and the Universe

Asking for a Homogenous and Isotropic one!

II. Expanding Universe and measuring Ω

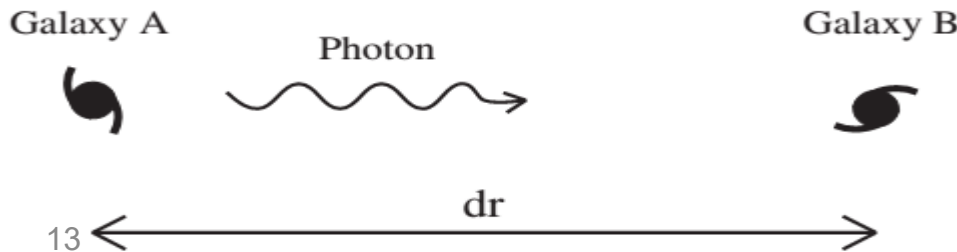
An idea from Mozart's Neighbor to Harvard Computers



Female astronomers at Harvard. Credit: Harvard University Archive, Williamina Fleming, Henrietta Leavitt, Edward Pickering

$$z \sim \frac{v}{c}$$

$$z = \frac{\lambda_{obs} - \lambda_{em}}{\lambda_{em}}$$



Albert Einstein, Edwin Hubble, and Walter Adams (l-r) in 1931 at the Mount Wilson Observatory 100" telescope, in the San Gabriel Mountains of southern California.

The Dynamics of the Universe

- The fundamental equations that governs the dynamics + GR

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3} (\rho_\gamma + \rho_m + \rho_b + \rho_\nu + \rho_\Lambda) - \frac{k}{a^2}$$

$$\rho_c = \frac{3H_0^2}{8\pi G} \rightarrow \Omega_i = \rho_i / \rho_c$$

- For a flat (Omega=1) homogenous and isotropic universe

$$H^2 = H_0^2 (\Omega_\gamma (1+z)^4 + \Omega_{m(dm+baryon)} (1+z)^3 + \Omega_\Lambda)$$

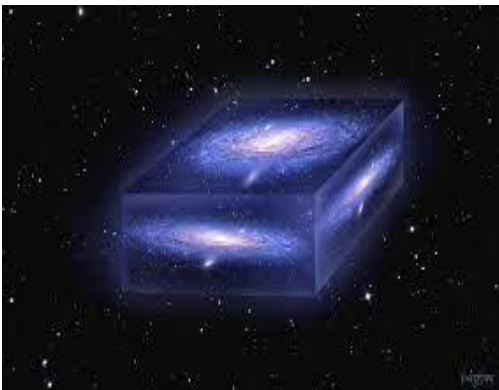
Source	Ω_m	Comment		
1 Hubble (1936)	0.002	galaxy counts and masses	21 Lynden-Bell, Lahav, and Burstein (1989)	~ 0.2 motion of the Local Group
2 Hubble (1936)	0.2	mass per galaxy in clusters	22 Efstathiou, Sutherland, and Maddox (1990)	~ 0.3 large-scale clustering ^a
3 Oort (1958)	0.03	$j = 2.9 \times 10^8 h, M/L = 29h$	23 Bahcall and Cen (1992)	~ 0.25 rich clusters in CDM ^{a,c}
4 van den Bergh (1961)	0.024	$j = 2.7 \times 10^8 h, M/L = 25h$	24 Strauss et al. (1992)	0.27 to 0.76 motion of the Local Group
5 Fall (1975)	0.01 to 0.05	Irvine-Layzer equation	25 Vogeley et al. (1992)	~ 0.3 large-scale clustering ^a
6 Gott and Turner (1976)	0.08	$j = 0.9 \times 10^8 h, M/L = 240h$	26 Briel, Henry, and Böhringer (1992)	0.14 ± 0.07 cluster baryon fraction ^{b,c}
7 Seldner and Peebles (1977)	0.69 ± 0.11	cluster ξ_{cp} and ξ_{cg}	27 White et al. (1993)	$\simeq 0.2$ cluster baryon fraction ^{b,c}
8 Peebles (1979)	0.4 ± 0.2	relative velocity dispersion	28 Dekel et al. (1993)	0.5 to 3 velocity and gravity fields
9 Yahil, Sandage, and Tammann (1980)	0.04 ± 0.02	Virgocentric flow	29 Fisher et al. (1994)	0.1 to 0.6 mean flow convergence
10 Davis et al. (1980)	0.4 ± 0.1	Virgocentric flow	30 Hudson et al. (1995)	0.61 ± 0.18 velocity and gravity fields
11 Tonry and Davis (1981)	$0.5^{+0.3}_{-0.15}$	Virgocentric flow	31 Shaya, Peebles, and Tully (1995)	0.17 ± 0.10 Virgocentric flow
12 Aaronson et al. (1982)	0.10 ± 0.03	Virgocentric flow	32 Davis, Nusser, and Willick (1996)	0.2 to 0.4 velocity and gravity fields
13 Davis and Peebles (1983a)	$0.2e^{\pm 0.4}$	relative velocity dispersion	33 Bahcall, Fan, and Cen (1997)	0.34 ± 0.13 evolution of rich clusters ^{a,c}
14 Bean et al. (1983)	$0.14 \times 2^{\pm 1}$	relative velocity dispersion	34 Carlberg et al. (1997)	0.19 ± 0.06 cluster masses
15 Loh and Spillar (1986b)	$0.9^{+0.7}_{-0.5}$	redshift-magnitude relation ^c	35 Eke et al. (1998)	0.36 ± 0.25 evolution of rich clusters ^{a,c}
16 Peebles (1986)	0.2 to 0.35	cluster ξ_{cp} and ξ_{cg}	36 Willick and Strauss (1998)	0.31 ± 0.05 velocity and gravity fields
17 Yahil, Walker, and Rowan-Robinson (1986)	0.85 ± 0.16	motion of the Local Group	37 Schmoldt et al. (1999)	$0.43^{+0.29}_{-0.17}$ motion of the Local Group
18 Strauss and Davis (1988)	0.4 to 0.9	motion of the Local Group	38 Tadros et al. (1999)	$0.28^{+0.18}_{-0.14}$ mean flow convergence
19 Blumenthal, Dekel, and Primack (1988)	~ 0.3	large-scale clustering ^a	39 Hamilton, Tegmark, and Padmanabhan (2000)	$0.23^{+0.13}_{-0.11}$ mean flow convergence
20 Regós and Geller (1989)	$\lesssim 0.5$	clustercentric flow	40 Percival et al. (2001)	0.29 ± 0.04 BAO ^{a,c}
			41 Hawkins et al. (2003)	0.31 ± 0.09 mean flow convergence
			42 Feldman et al. (2003)	$0.30^{+0.17}_{-0.07}$ relative peculiar velocities ^c

Vacant and Vast

- Critical Density $\rho_c = \frac{3H_0^2}{8\pi G}$

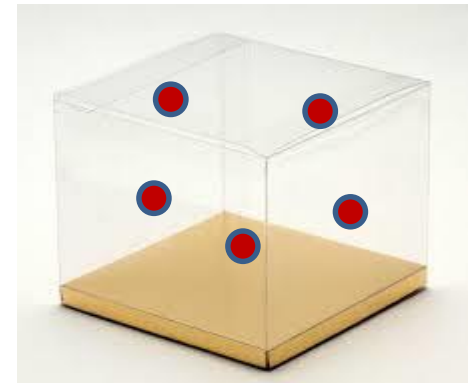
$$H_0 = 100h[\text{km} / \text{s} / \text{Mpc}](h \sim 0.7) \rightarrow \begin{aligned} H_0^{-1} &= 9.77h^{-1} \times 10^9 \text{ yr} \\ cH_0^{-1} &= 3000h^{-1} \text{ Mpc} \end{aligned}$$

$$H_0 \approx 70[\text{km} / \text{s} / \text{Mpc}] \rightarrow \rho_c = 1.88h^2 \times 10^{-26} \text{ kgm}^{-3}$$



$0.1 \text{ Milky - way} / \text{Mpc}^3$

$5 \text{ proton} / \text{m}^3$



Science of 2010-1926 – Alan Sandage

measuring two quantities + DE

$$H = \frac{\dot{a}}{a}, q = -\frac{\ddot{a}}{a\dot{a}}$$

$$\frac{\ddot{a}}{a} = -\frac{4\pi G}{3}(\rho + 3p) > 0$$

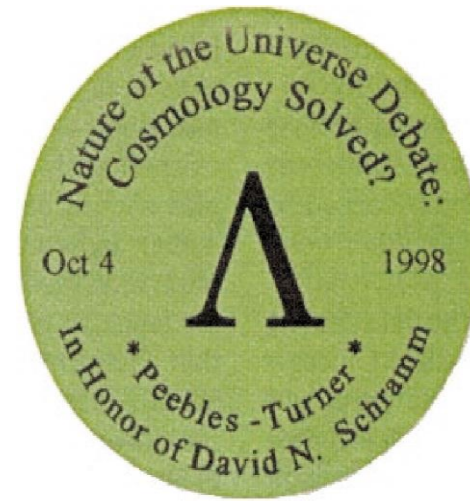


Photo: Lawrence Berkeley National Lab

Saul Perlmutter



Photo: Belinda Pratten, Australian National University

Brian P. Schmidt

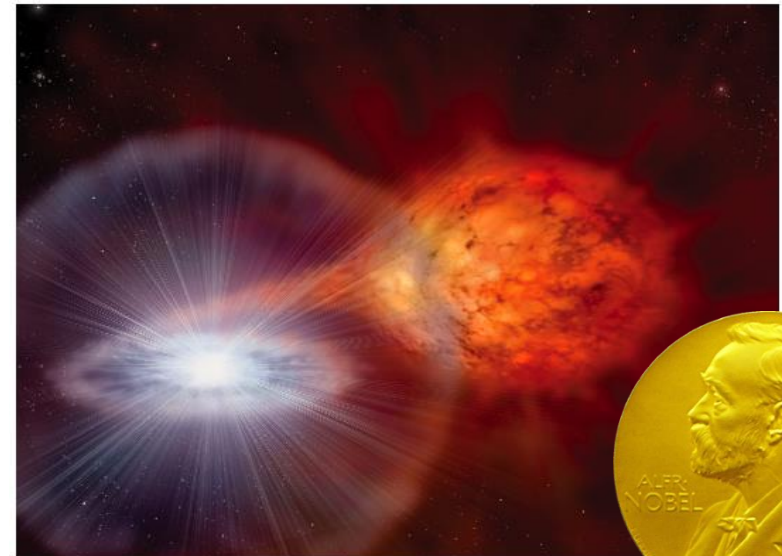


Photo: Scanpix/AFP

Adam G. Riess

The Nobel Prize in Physics 2011 was awarded "for the discovery of the accelerating expansion of the Universe through observations of distant supernovae" with one half to Saul Perlmutter and the other half jointly to Brian P. Schmidt and Adam G. Riess.

[Adam Riess et al. Astron.J. 116 \(1998\) 1009-1038 \(H-z\)](#)
[Perlmutter et al. Astrophys.J. 517 \(1999\) 565-586 \(SCP\)](#)



Artist's rendition of a white dwarf accumulating mass from a nearby companion star. This type of progenitor system would be considered to degenerate.

Image courtesy of David A. Hardy, © David A. Hardy/www.astroart.org.



Our route: 3 Steps to H_0

© Adam Riess

1 (Kpc)

2 (Mpc)

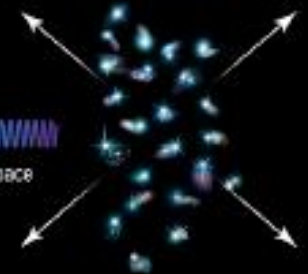
3 (Gpc)



Galaxies hosting Cepheids and Type Ia supernovae



Distant galaxies in the expanding Universe hosting Type Ia supernovae



Light redshifted (stretched) by expansion of space

0 - 10 Kpc 10 Thousand - 100 Million Light-years 100 Million - 1 Billion Light-years

18 1: Geometry \rightarrow Cepheids

2: Cepheids \rightarrow SN Ia

3: SN Ia $\rightarrow z, H_0$

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After World war II – Princeton days



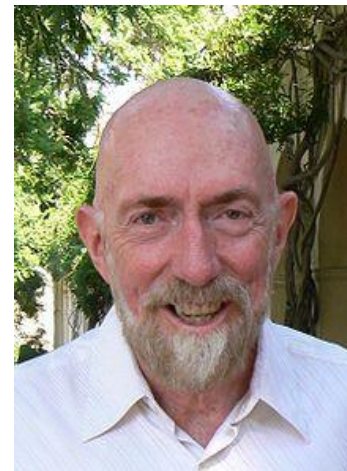
Fig. 1. Members of the senior faculty in the Department of Physics, Palmer Physical Laboratory, Princeton University, in about 1950: from the left Rubby Sherr, Allen Shenstone, Donald Hamilton, Eric Rogers, Robert Dicke, Walker Bleakney, John Wheeler, Rudolf Ladenburg, and Eugene Wigner.



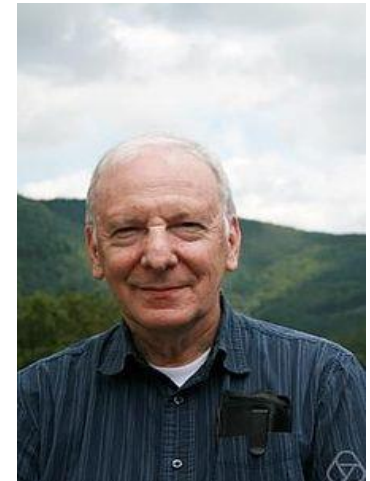
R. Feynman



B. Mashhoon



K. Thorne



R. Wald

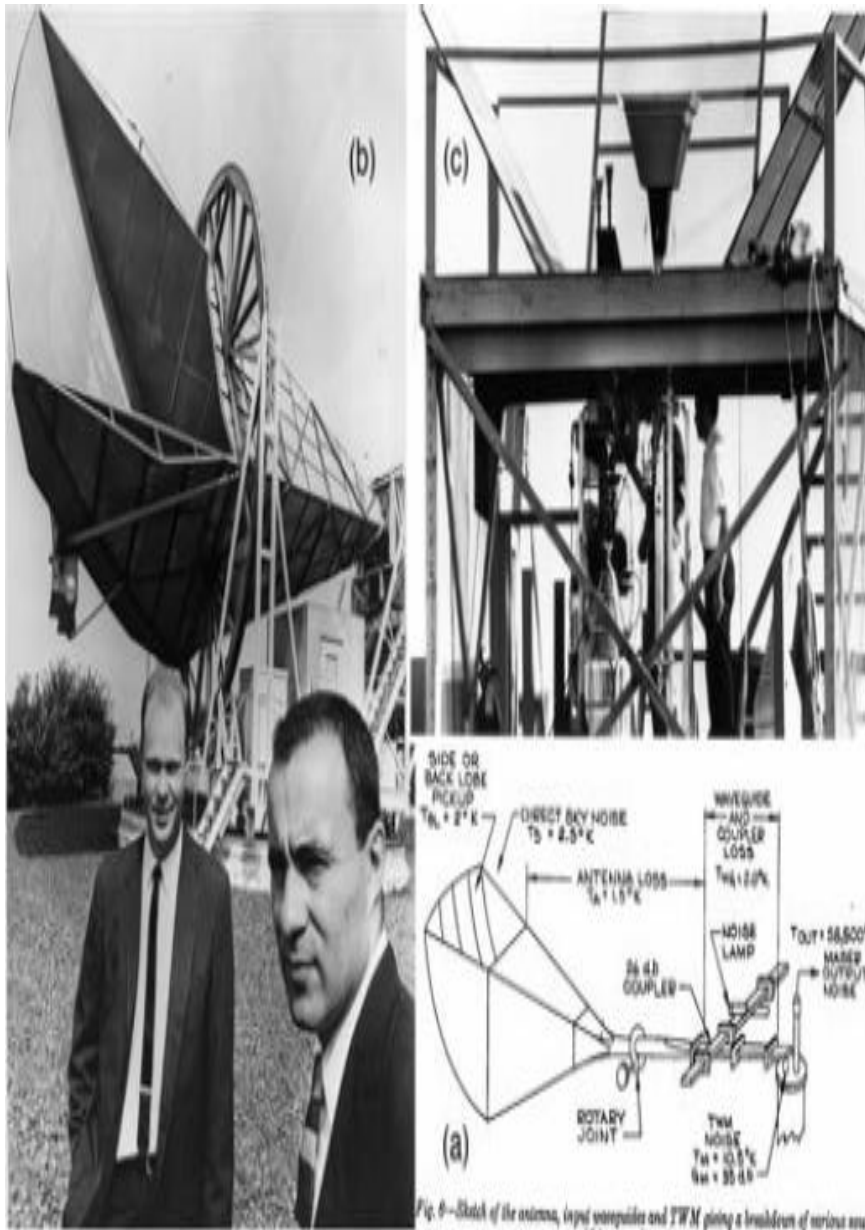


Fig. 9--Sketch of the antenna, input waveguides and TWM giving a breakdown of various sources of input noise temperature.



Wilkinson, Peebles, and Dicke left to right, in the late 1970s.

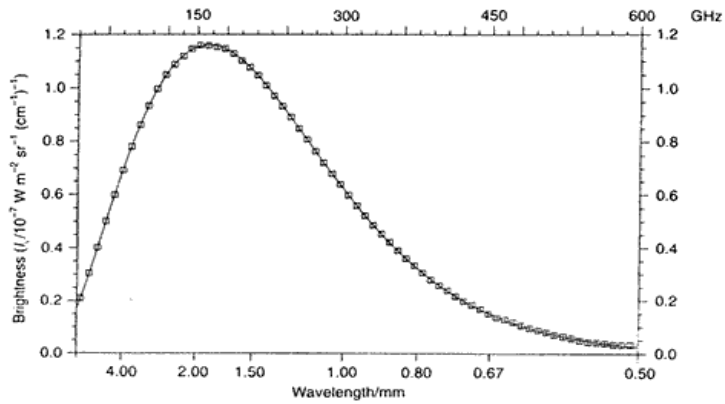
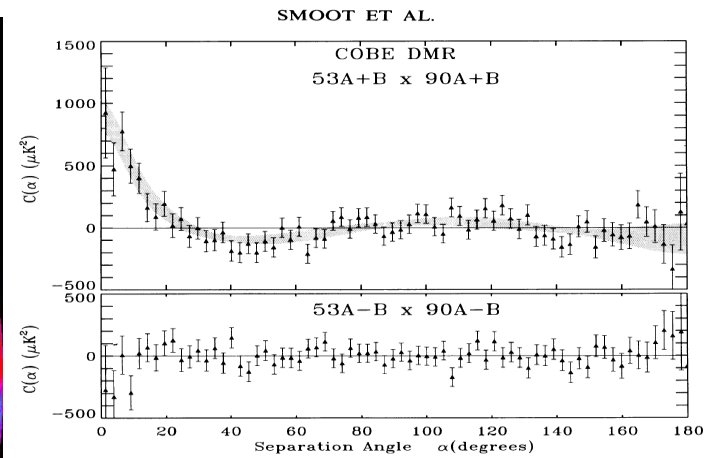
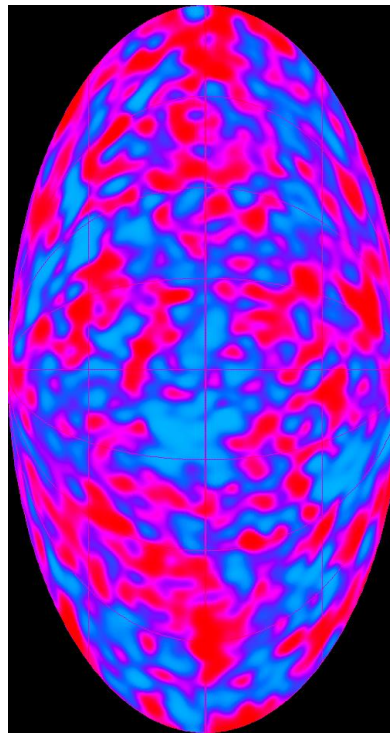


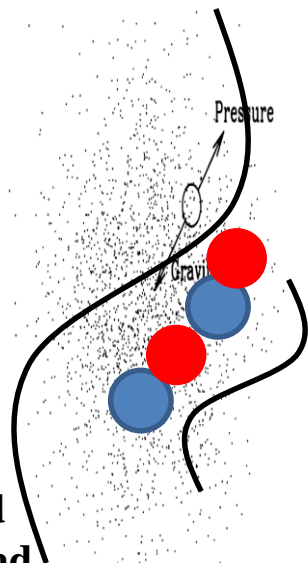
Fig. 2.1. The first published spectrum of the Cosmic Microwave Background Radiation as measured by the COBE satellite in the direction of the North Galactic Pole (Mather *et al.* 1990). Within the quoted errors, the spectrum is precisely that of a perfect black body at radiation temperature 2.735 ± 0.06 K. The more recent spectral measurements are discussed in the text. The units adopted for frequency on the ordinate are cm^{-1} . A useful conversion to more familiar units is $10^{-7} \text{ W m}^{-2} \text{ sr}^{-1} (\text{cm}^{-1})^{-1} = 3.34 \times 10^{-18} \text{ W m}^{-2} \text{ Hz}^{-1} \text{ sr}^{-1} = 334 \text{ MJ sr}^{-1}$.



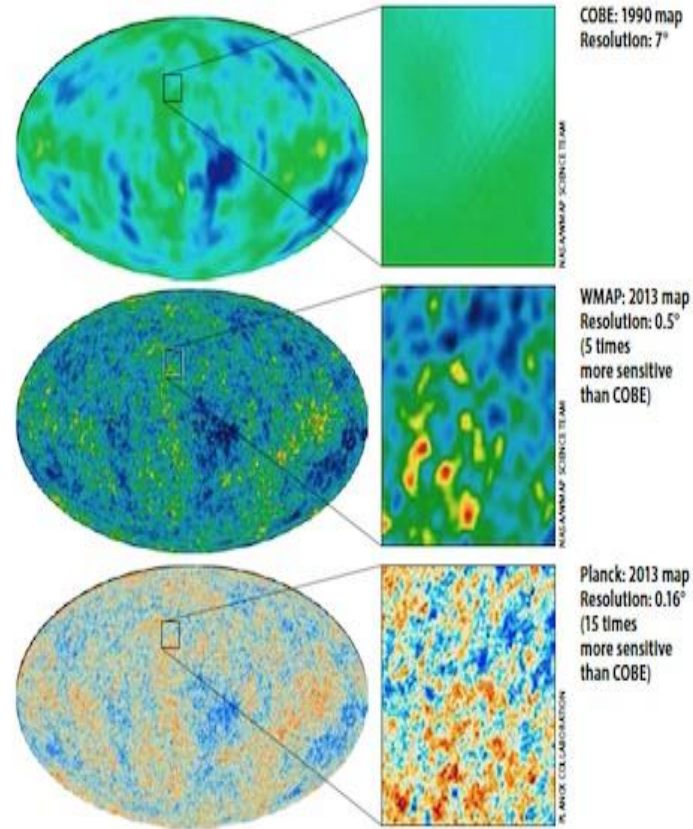
$$\epsilon(\nu)d\nu = \frac{8\pi h}{c^3} \frac{\nu^3 d\nu}{e^{h\nu/kT} - 1}$$

$$\epsilon_{rad} = \alpha T^4$$

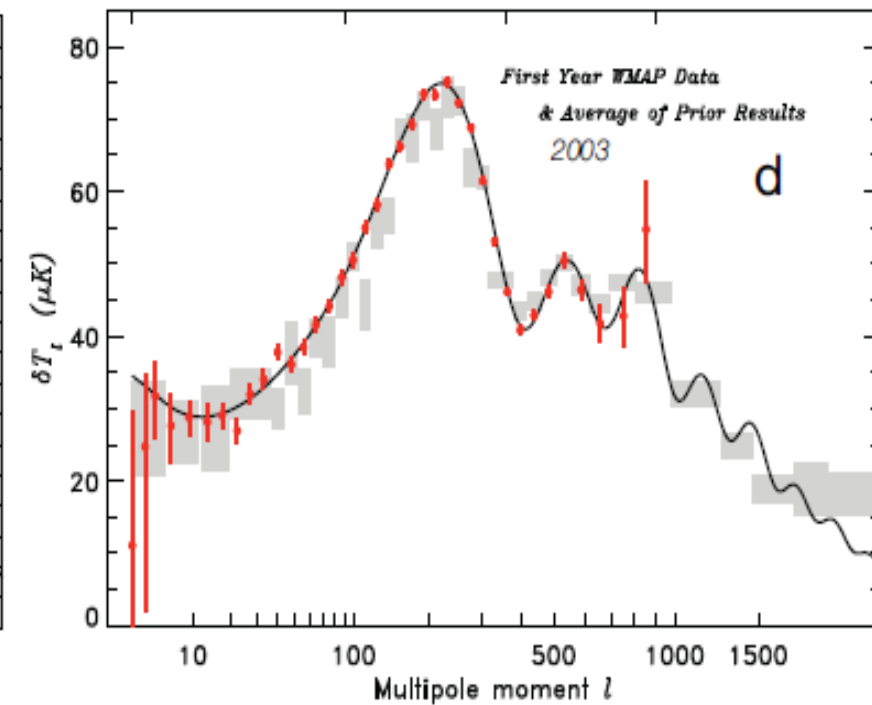
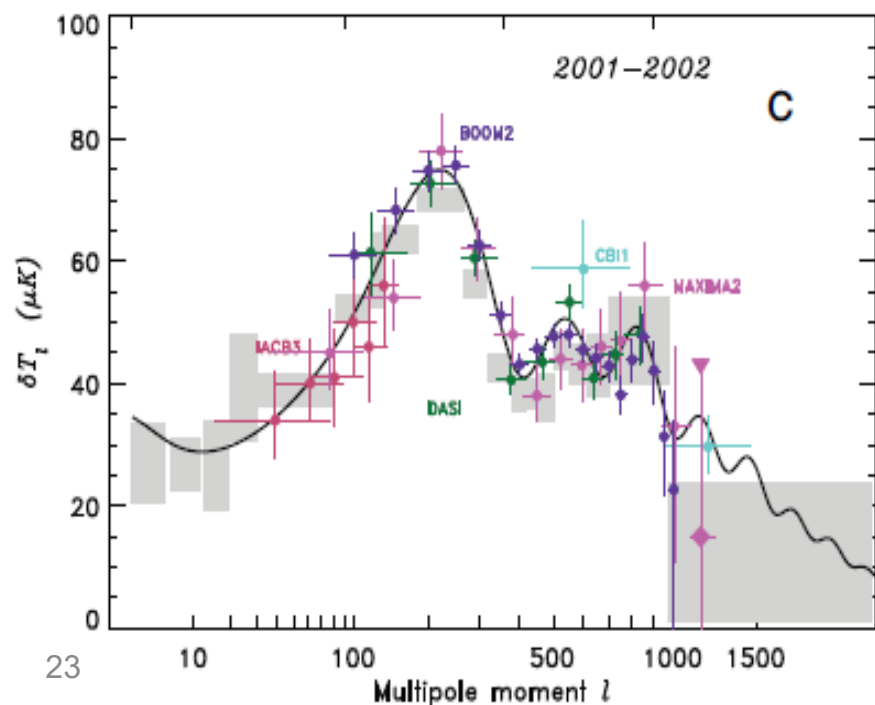
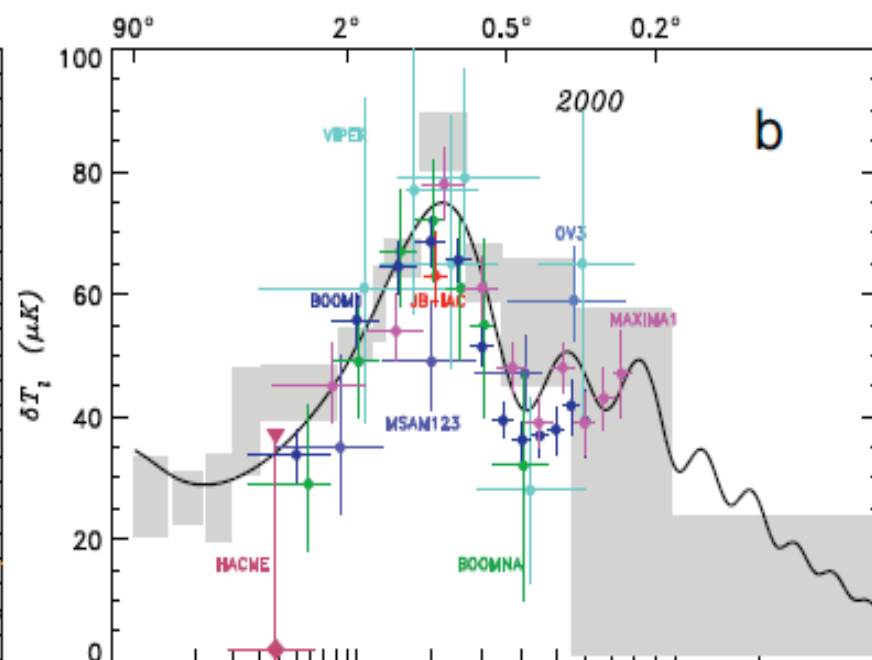
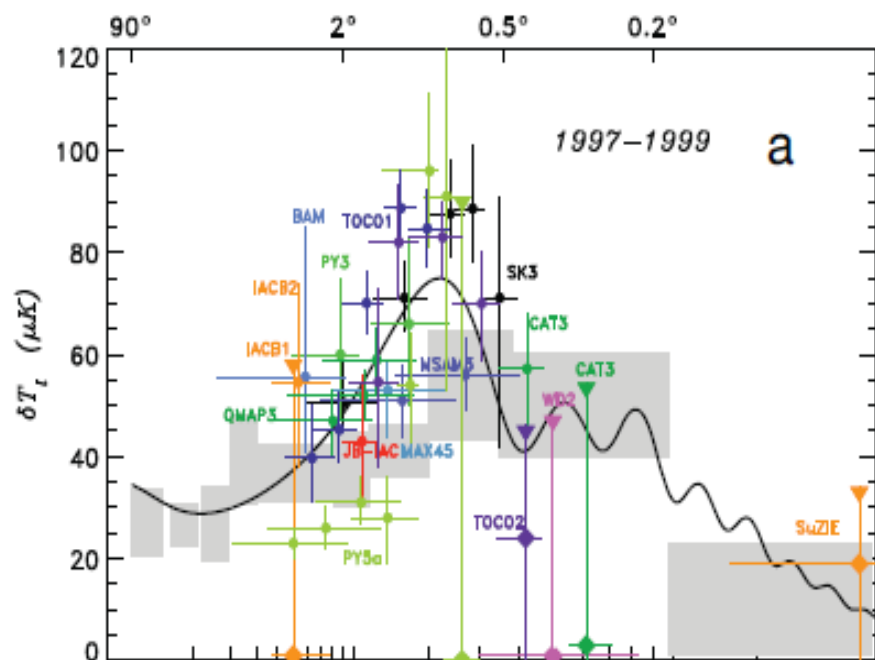
$$\alpha = 7.565 \times 10^{-16} \text{ Joule.m}^{-3} \text{ Kelvin}^{-4}$$



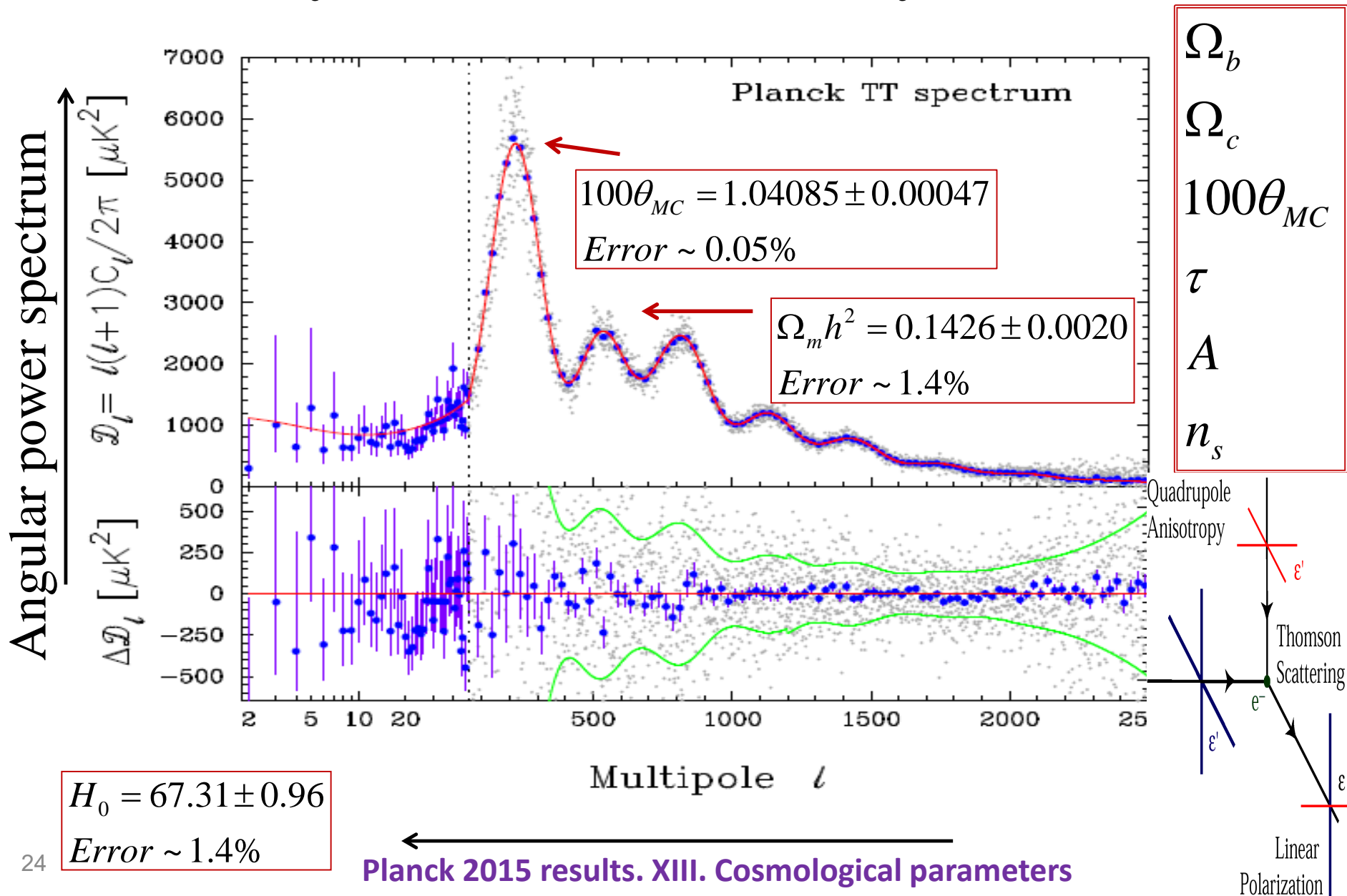
CLOSE-UP VIEWS OF THE CMB



The Nobel Prize in Physics 2006
John C. Mather and George F. Smoot
"for their discovery of the blackbody form and anisotropy of the cosmic microwave background radiation"



The Early Universe with the eyes of Planck



6 Lines of Thought to 6 parameter model

I. General relativity and the Universe

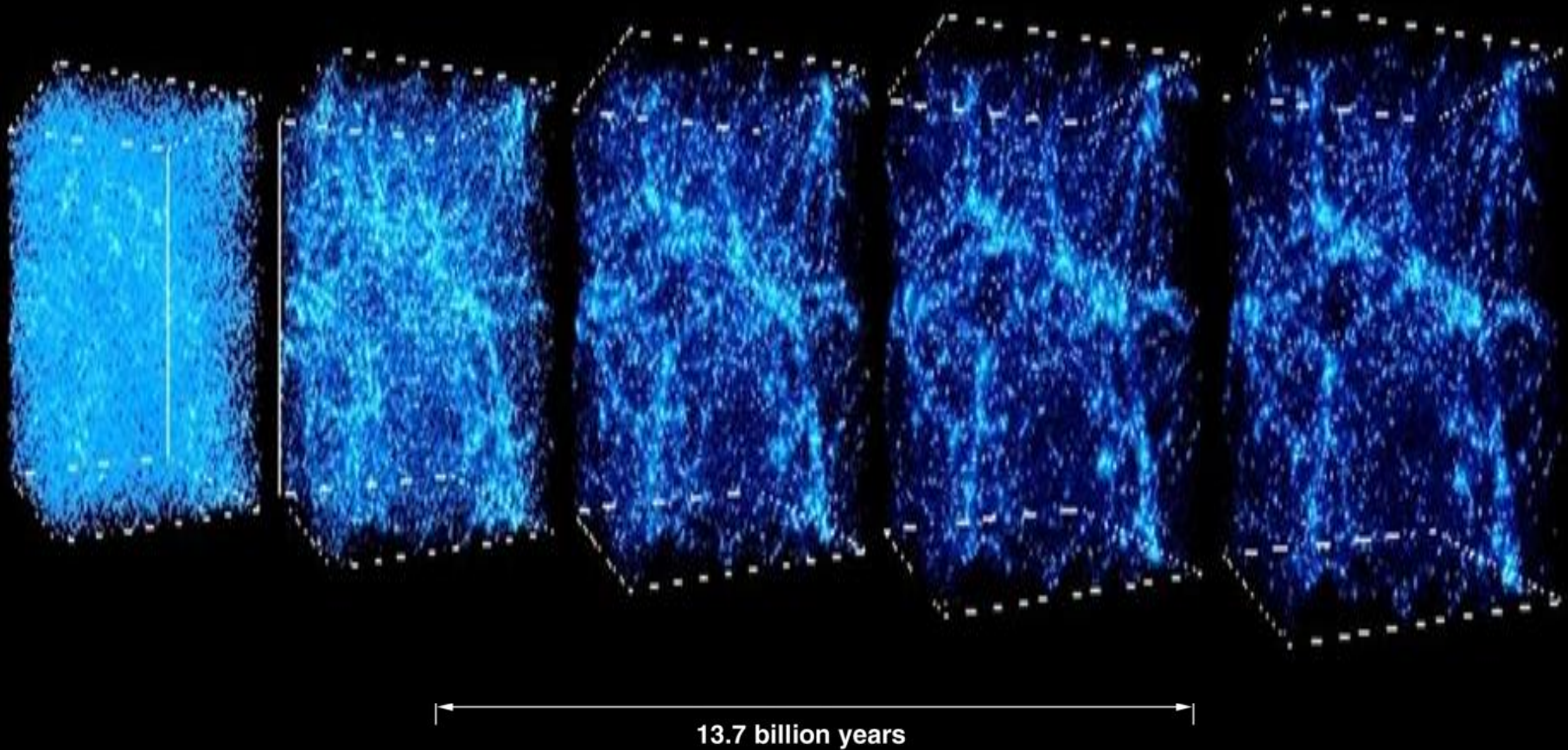
Asking for a Homogenous and Isotropic one!

II. Expanding Universe and measuring Ω

III. Cosmic Microwave Background Radiation

IV. Structure Formation and LSS

Cosmic Evolution and Gravitational instability



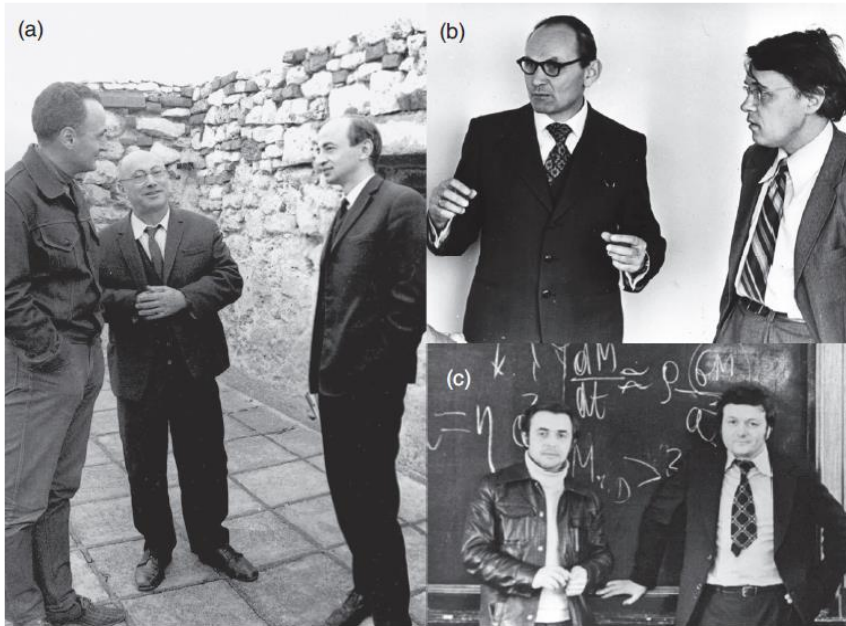
“My balance comes from instability.”

— **Saul Bellow**

Statistical Methods and 2 point correlations and the story of the two schools

$$P(k) = \langle |\delta_k|^2 \rangle \leftrightarrow \delta_m = \frac{\rho}{\bar{\rho}} - 1$$

$$\xi(\vec{r}) = \langle \delta(\vec{x})\delta(\vec{x} + \vec{r}) \rangle$$

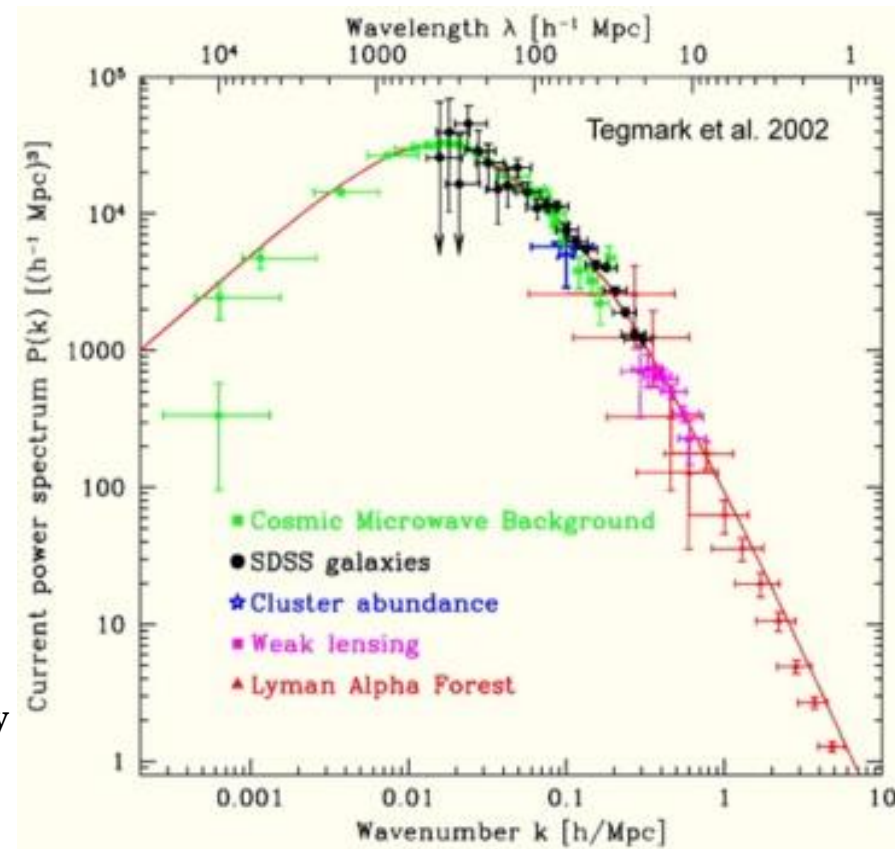


Cosmology in the Soviet Union.

(a) George Marx, Yakov Zel'dovich, and Igor Novikov (left to right) in Hungary in about 1970

(b) Jaan Einasto, left, and Andrei Doroshkevich at a Conference in Tallinn in 1977 and

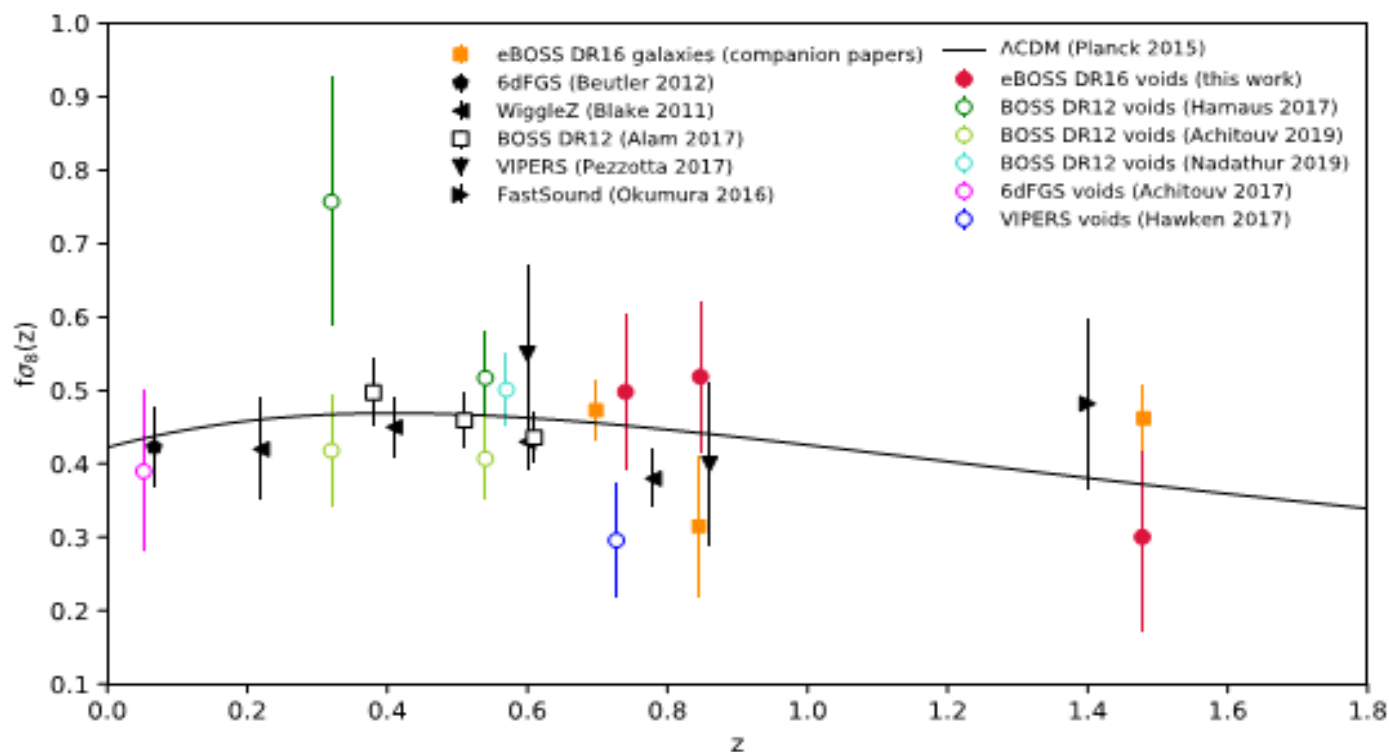
(c) Nikolay Shakura, left, and Rashid Sunyaev in the 1970s.



<https://arxiv.org/abs/2007.09013>

The Completed SDSS-IV Extended Baryon Oscillation Spectroscopic Survey: Growth rate of structure measurement from cosmic voids

Marie Aubert^{1*}, Marie-Claude Cousinou¹, Stéphanie Escoffier¹, Adam J. Hawken¹, Seshadri Nadathur², Shadab Alam³, Julian Bautista², Etienne Burtin⁴, Arnaud de Mattia⁴, Héctor Gil-Marín^{5,6}, Jiamin Hou⁷, Eric Jullo⁸, Richard Neveux⁴, Graziano Rossi⁹, Alex Smith⁴, Amélie Tamone¹⁰, Mariana Vargas Magaña¹¹



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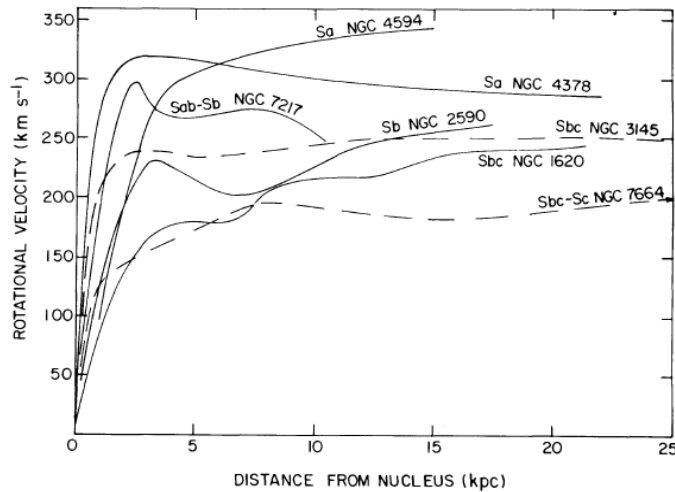
V. Subluminal matter

VI. Non-baryonic Dark Matter

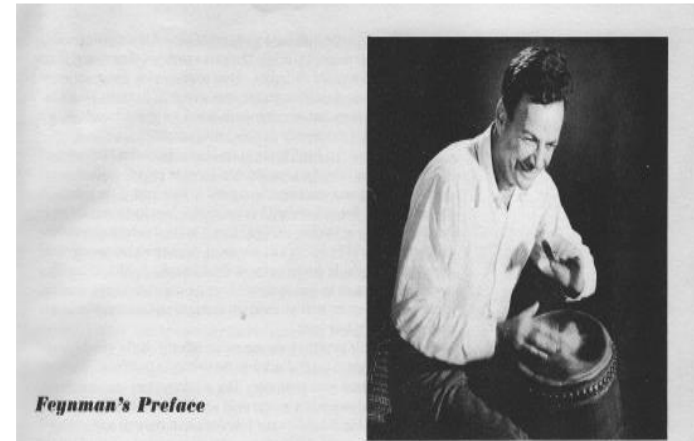
Something is missing! + Neutrinos



Vera Rubin and Kent Ford.



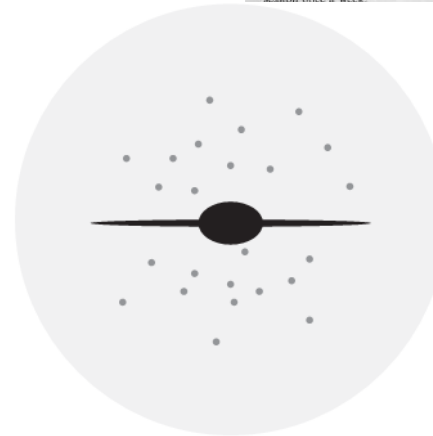
(Rubin, V.C., Ford, W.K. & Thonnard, N. 1978, *Astrophys. J.* 225, L107)



Feynman's Preface

These are the lectures in physics that I gave last year and the year before to the freshman and sophomore classes at Caltech. The lectures are, of course, not verbatim—they have been edited, sometimes extensively and sometimes less so. The lectures form only part of the complete course. The whole group of 180 students gathered in a big lecture room twice a week to hear these lectures and then they broke up into small groups of 15 to 20 students in recitation sections under the guidance of a teaching assistant. In addition, there was a laboratory session once a week.

*Dear Alex,
Thank you for your hospitality and help in Balatonfured and Debrecen. I won't forget my visit. I was surprised to learn that neutrinos mass could be limited by thoughts of cosmology!
Richard Feynman*



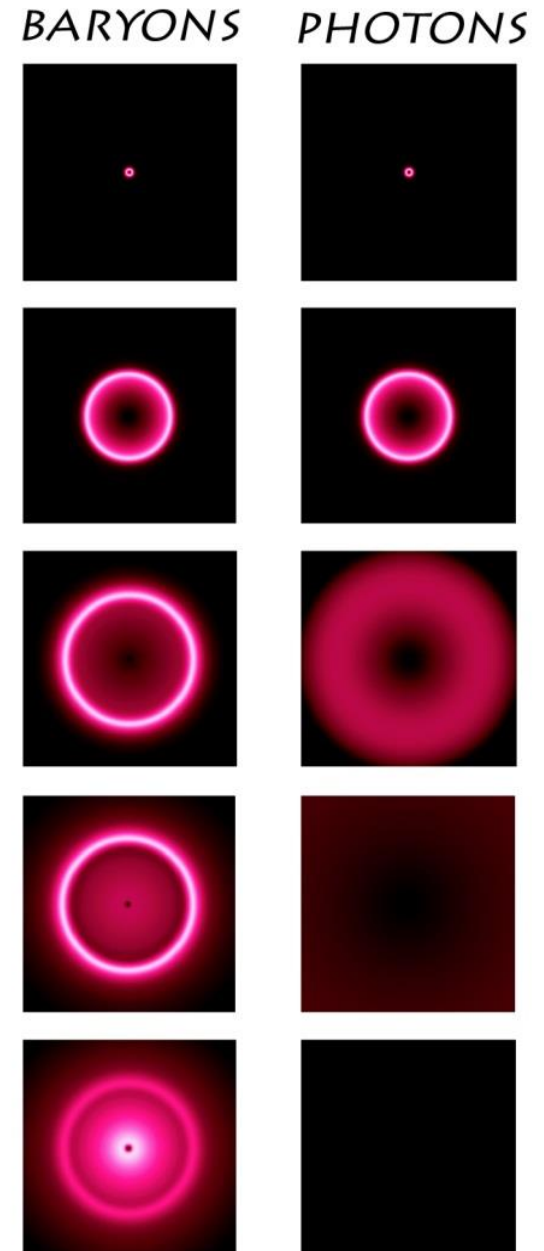
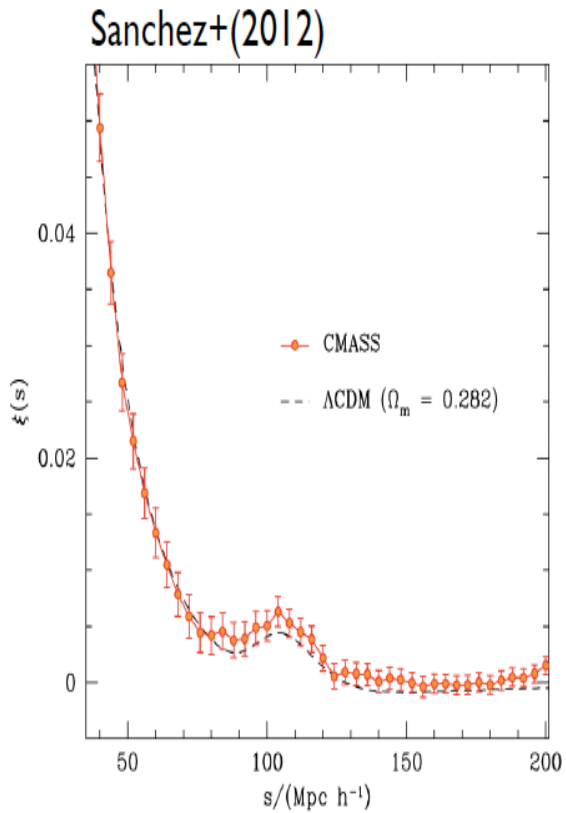
h these lectures was to maintain the art students coming out of the high lot about how interesting and excitement mechanics, and other modern us course, many would be very dis- grand, new, modern ideas presented planes, electrostatics, and so forth. The problem was whether or not we ore advanced and excited student by

to be a survey course, but are very it intelligent in the class and to make it student was unable to completely —by putting in suggestions of appli- directions outside the main line of hard to make all the statements as where the equations and ideas fitted ey learned more—things would be it is important to indicate what it is r—be able to understand by deduct- at is being put in as something new. deduce them if they were deducible,

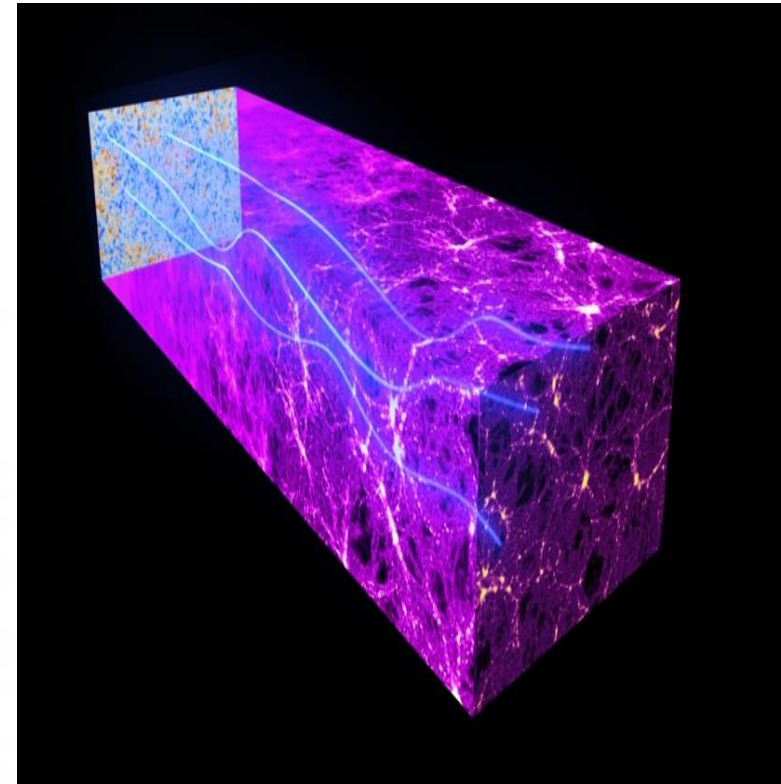
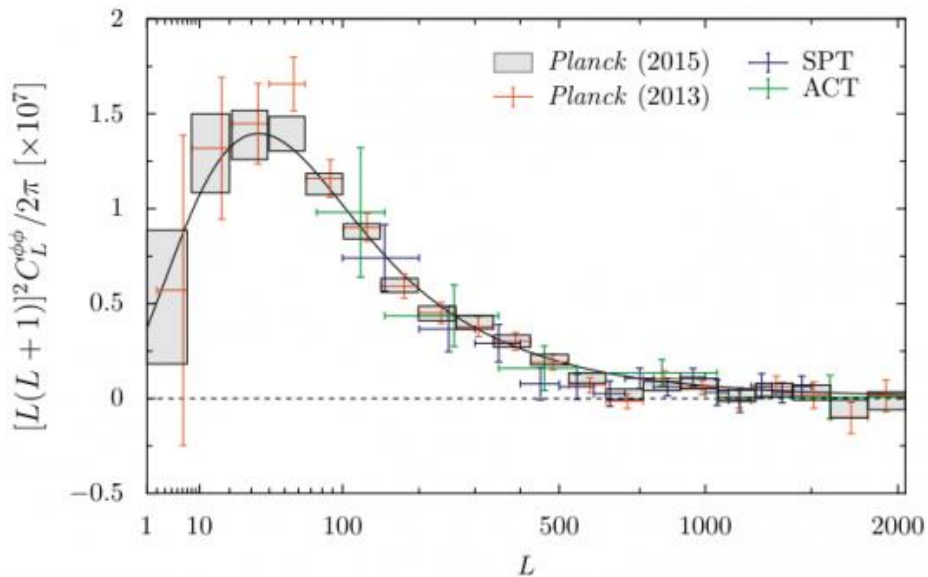
or to explain that it was a new idea which hadn't any basis in terms of things they had already learned and which was not supposed to be provable—but was just added in.

At the start of these lectures, I assumed that the students knew something when they came out of high school—such things as geometrical optics, simple chemistry ideas, and so on. I also didn't see that there was any reason to make the lectures

Mesmerizing Evidence of DM



CMB Lensing as an evidence of the DM



$$\tilde{\Theta}(\hat{x}) = \Theta(\hat{x}') = \Theta(\hat{x} + \vec{\nabla} \psi)$$

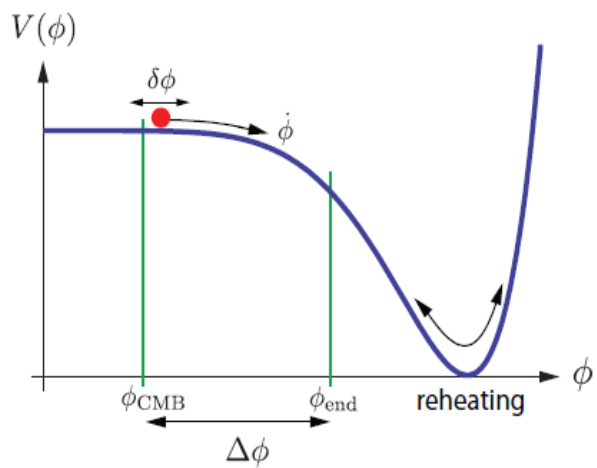
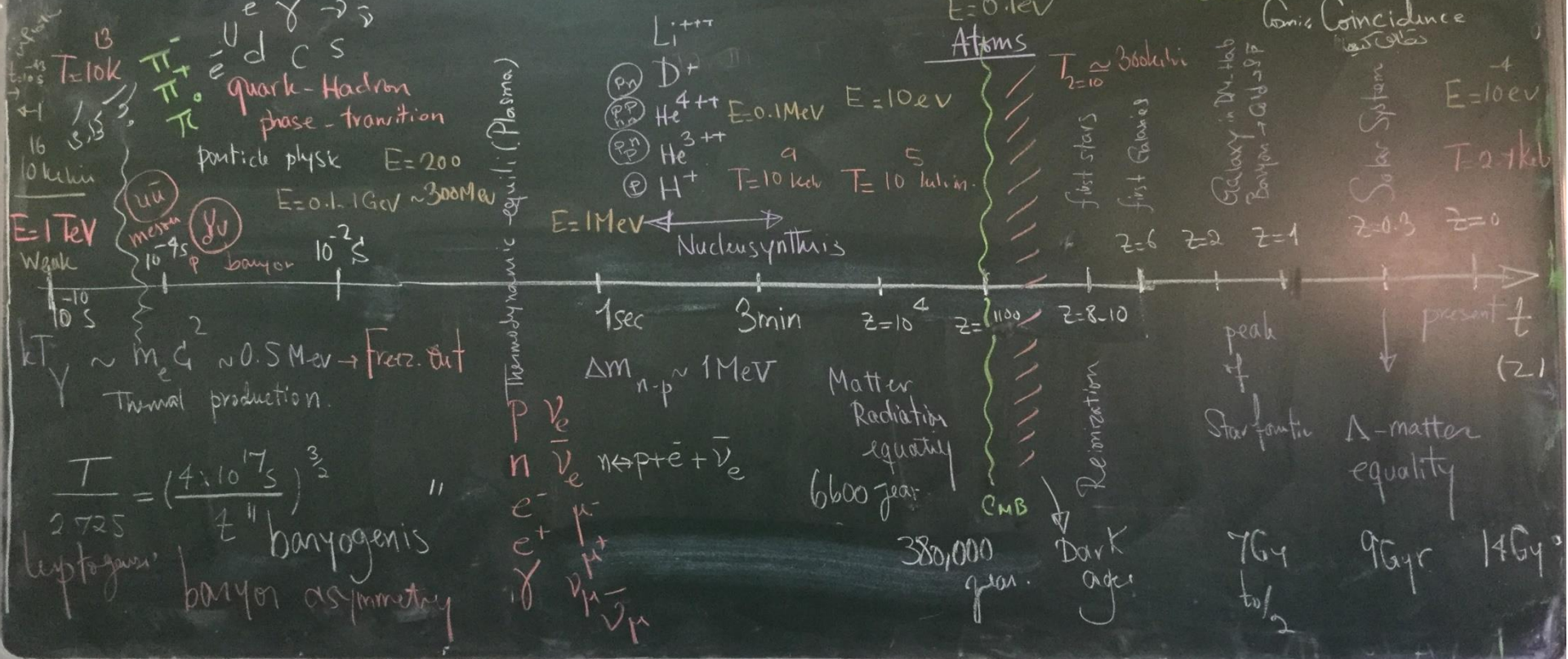
$$\psi(\hat{n}) \equiv -2 \int_0^{\chi_\infty} d\chi \left(\frac{\chi_\infty - \chi}{\chi_\infty \chi} \right) \Psi(\vec{x}', \eta)$$

$$\vec{x}' = \chi \hat{n}; \eta = \eta_0 - \chi$$

Cosmic Shear @ KIDs
M. Asgari

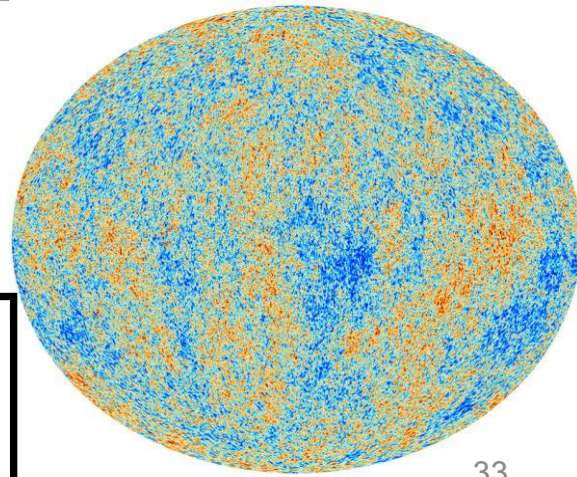
Farbod Hassani, SB, Hassan Firouzjahi, arXiv:1511.05534
Mohammad Ansari – Master Thesis.

1998-2003 Revolution - Λ CDM



Ali Akbar Abolhasani

$$\Delta_s^2 = \frac{1}{2\pi^2} k^3 P_s(k) = A_s \left(\frac{k}{k_p}\right)^{n_s-1}$$



1998-2003 Revolution - Λ CDM

- The universe is very old and very big!

Dark Energy

- The Gravity is the most essential force!

Dark Matter

- The initial condition of the Universe is very simple!

Early Universe Physics

Λ CDM with flat 6 parameter model with
nearly Gaussian, isotropic, adiabatic, nearly scale invariant
initial conditions

and

GR+ECP

Oratorio*

Based on:

- Encieh Erfani, Hamed Kameli, **SB**, Accepted for publication in MNRAS (2021)
- Hamed Kameli, **SB**, arXiv:2008.13175, submitted to MNRAS (2021)
- Hossein Moshafi, **SB**, Nima Khosravi, submitted to PRD, arXiv:2012.14377 (2021)
- Hamed Kameli, **SB**, 2020, MNRAS, V. 494, Issue 4, 4907
- Alireza Maleki, **SB**, Sohrab Rahvar, Phys. Rev. D 101, 103504, (2020)
- Nima Khosravi, **SB**, Niayesh Afshordi, Natacha Altamirano, Phys. Rev. D 99, 103526 (2019)
- **SB** et al. Physical Review E 99, 062101 (2019)
- Farnik Nikakhtar, Mohammadreza Ayromlou, **SB**, Sohrab Rahvar, M. Reza Rahimi Tabar, Ravi K. Sheth, MNRAS, 478, no.4, 5296-5300, (2018)



*An oratorio is a large musical composition for orchestra, choir, and soloists.

6 Lines of Thought to 6 parameter model

I. General relativity and the Universe

Asking for a Homogenous and Isotropic one!

II. Expanding Universe and measuring Ω

III. Cosmic Microwave Background Radiation

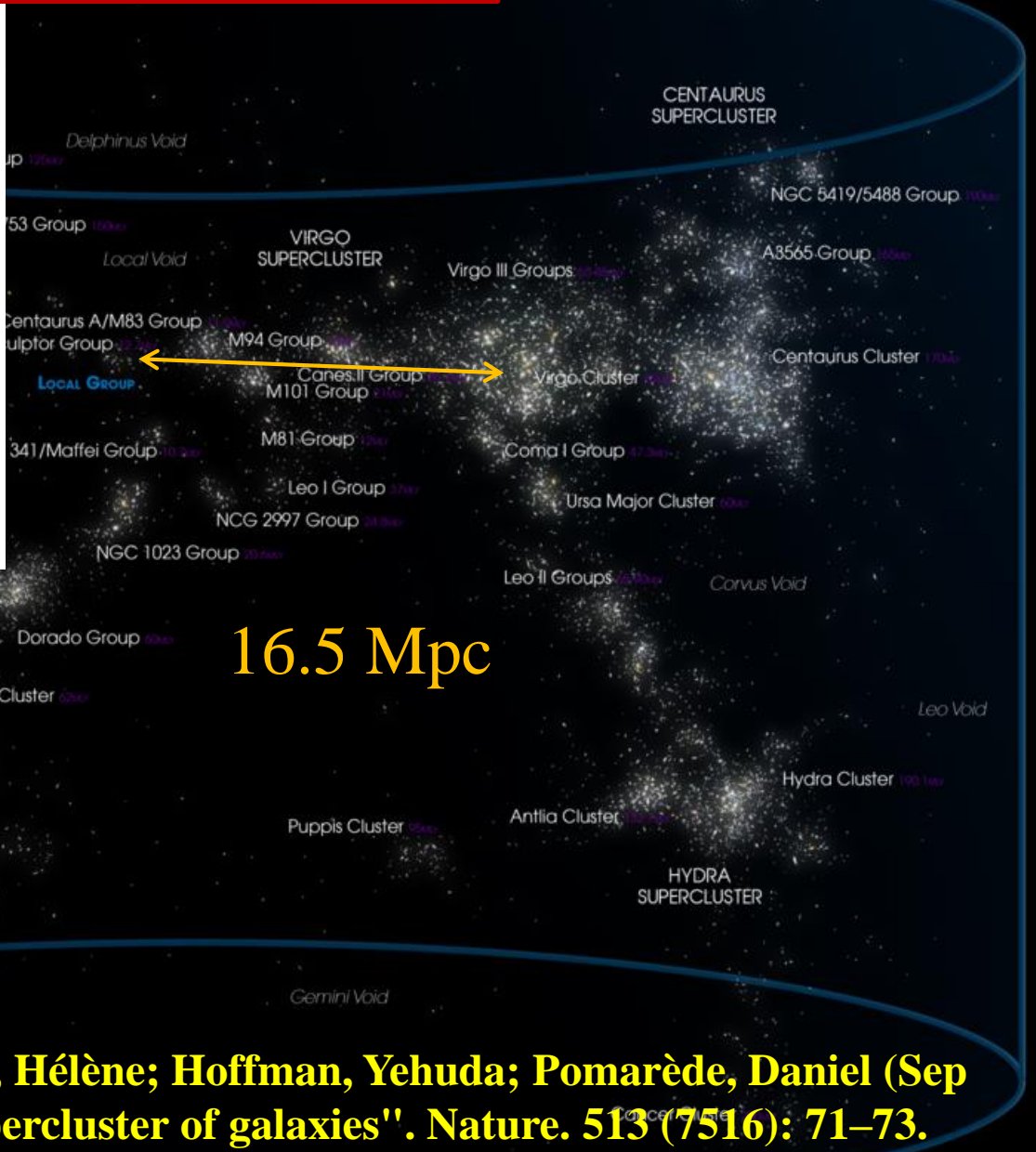
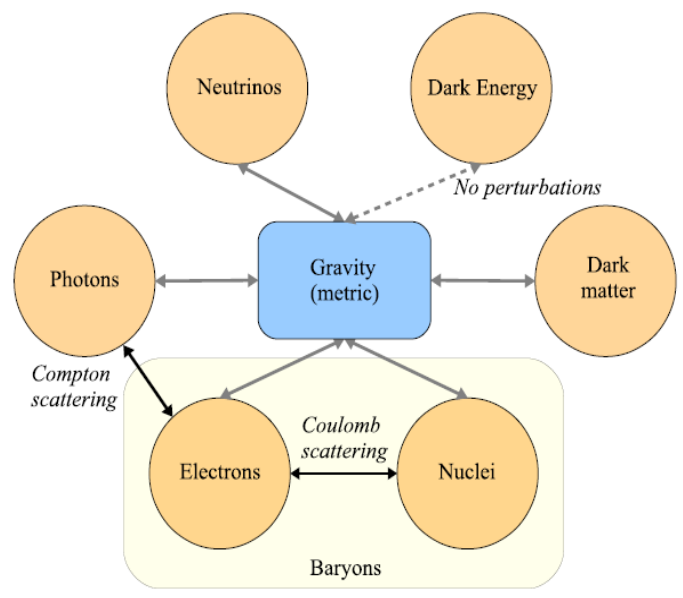
IV. Structure Formation and LSS

V. Subluminal matter

VI. Non-baryonic Dark Matter

❖ **More insight in LSS in non-linear scale
to introduce new Probes**

$$ds^2 = -(1 + 2\Psi(\vec{x}, t))dt^2 + a^2(t)\delta_{ij}(1 + 2\Phi(\vec{x}, t) + h_{ij})dx^i dx^j$$

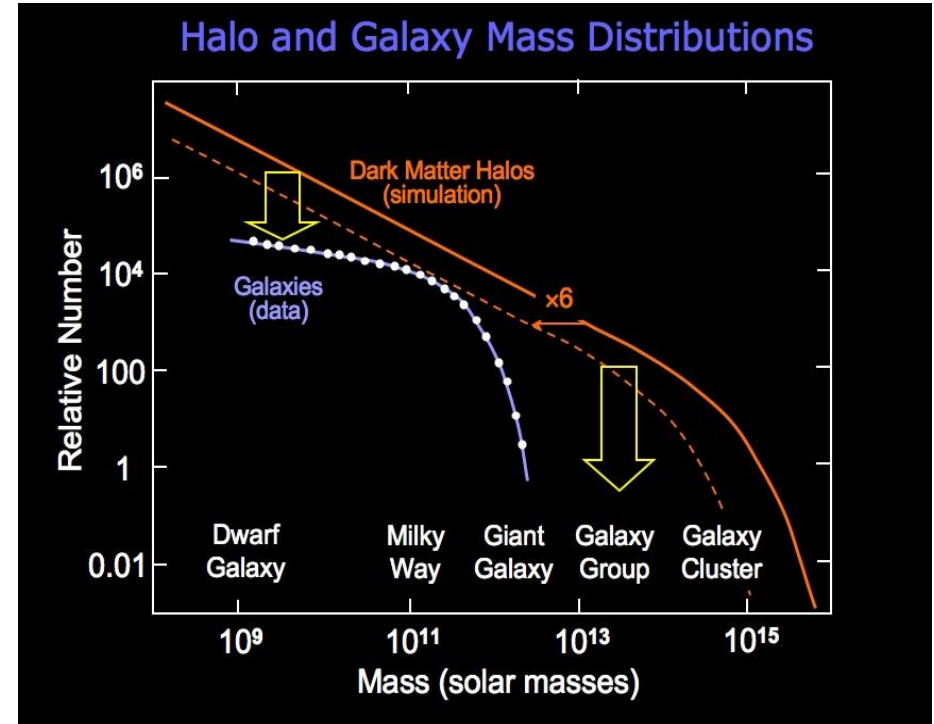
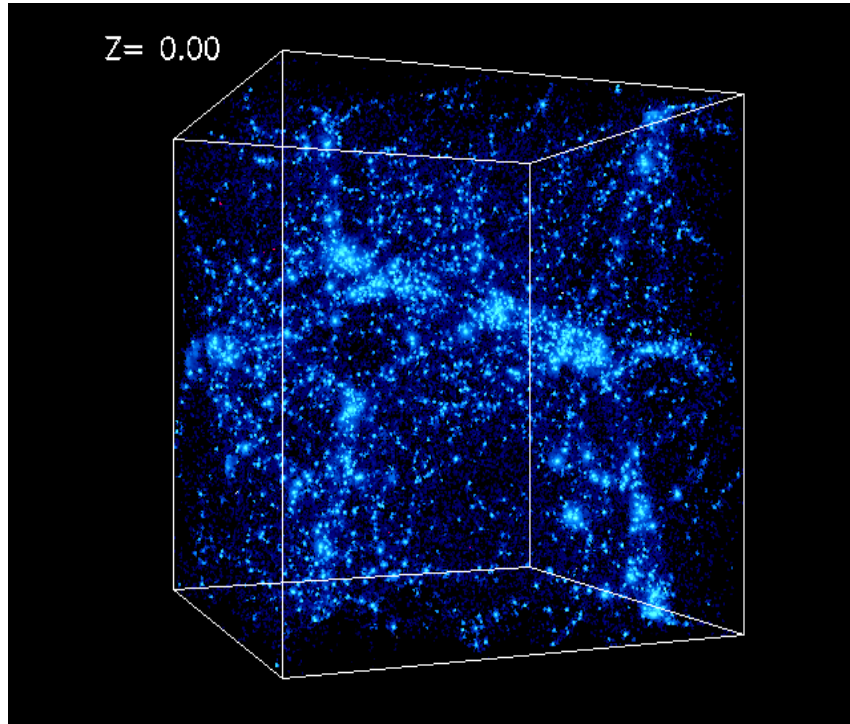


16.5 Mpc

LANIAKEA

Tully, R. Brent; Courtois, H el ene; Hoffman, Yehuda; Pomar ede, Daniel (Sep 2014). "The Laniakea supercluster of galaxies". Nature. 513 (7516): 71–73. arXiv:1409.0880. doi:10.1038/nature13674. ISSN 1476-4687

Non-linear Structures + baryonic physics



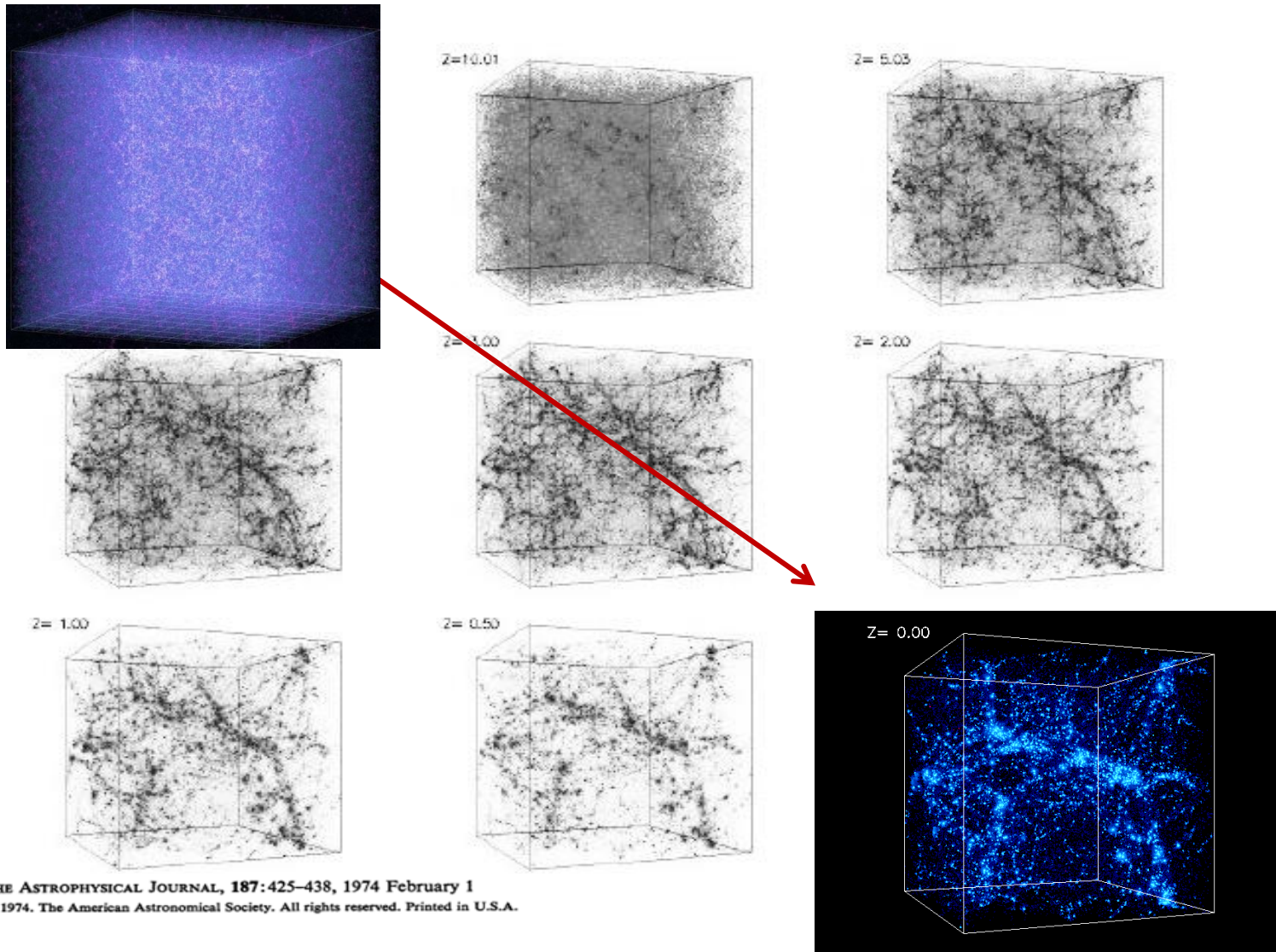
Cosmic Web: Halos, Filaments, Voids ,...

$$n = n(M, z, \dots)$$

If you are an astrophysicist you will ask about

$$\phi = \phi(L, z, \dots)$$

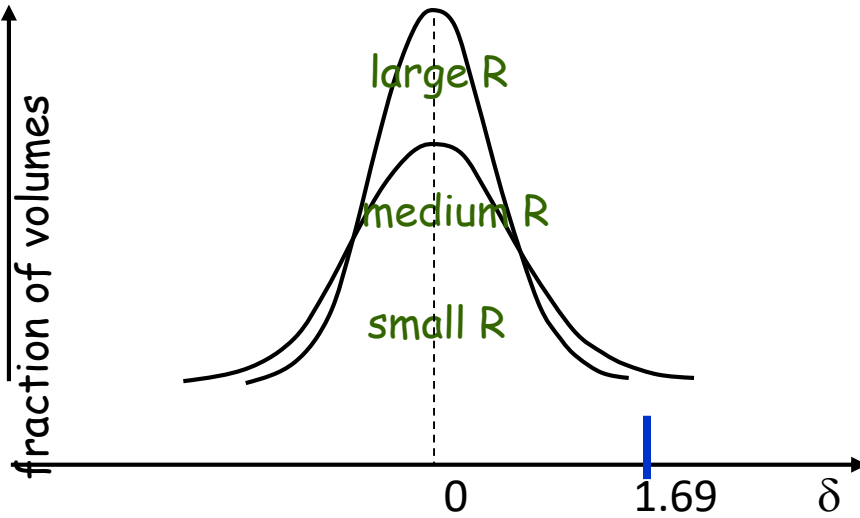
The musing of PS, BBKS, BCEK, **ST**



FORMATION OF GALAXIES AND CLUSTERS OF GALAXIES :
SELF-SIMILAR GRAVITATIONAL CONDENSATION*
WILLIAM H. PRESS AND PAUL SCHECHTER

Press & Schechter 1974

Dark Matter as the host of Luminous matter

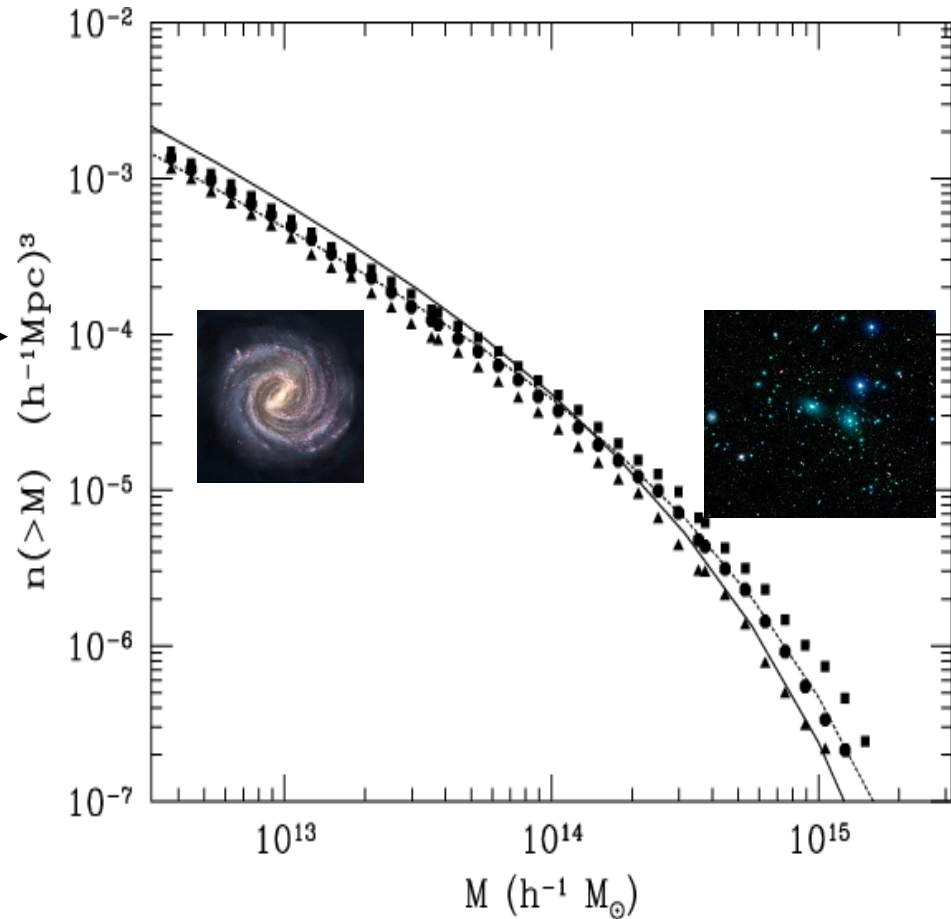


$$P(\delta) = \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{\delta^2}{2\sigma^2(M)}}$$

$$P_{\text{collapsed}}(\delta > \delta_c) = \int_{\delta_c}^{\infty} \frac{1}{\sqrt{2\pi\sigma^2}} e^{-\frac{\delta^2}{2\sigma^2(M)}}$$

$$f_{\text{uni}}(v) = v \frac{e^{-\frac{v^2}{2\sigma^2}}}{\sqrt{2\pi}}$$

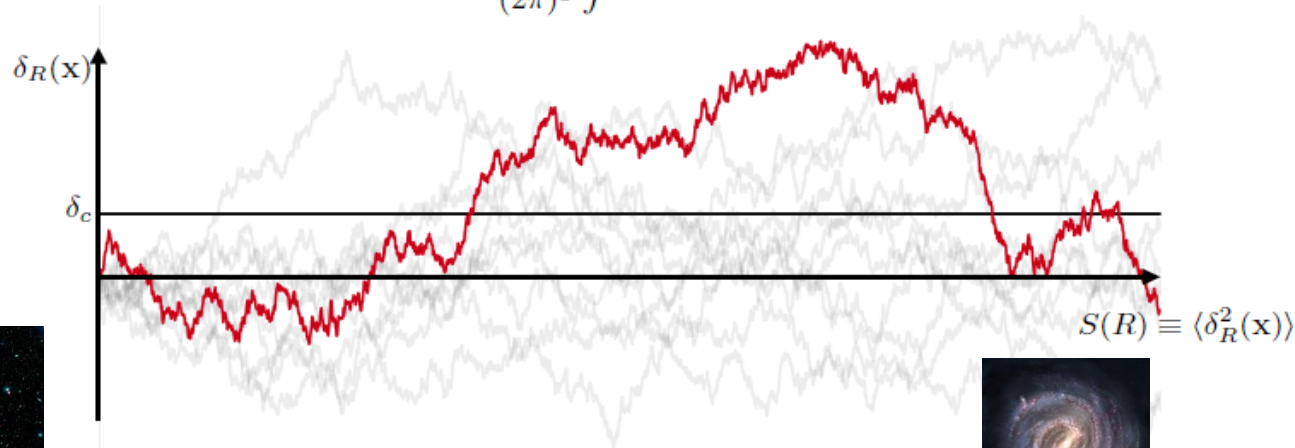
$$v \equiv \frac{\delta_c}{\sigma}, S = \sigma^2$$



$$n(M)dM = 2 \frac{\rho}{M^2} f_{\text{uni}}(v) \left| \frac{d \ln \sigma(M)}{d \ln M} \right| dM$$

Excursion Set theory of LSS

$$\delta_R(\mathbf{x}) = \frac{1}{(2\pi)^3} \int d^3k \tilde{W}(kR) e^{i\mathbf{k}\cdot\mathbf{x}} \delta(\mathbf{k})$$



These random trajectories have the variance

$$S(R) \equiv \langle \delta_R^2(\mathbf{x}) \rangle = \frac{1}{2\pi^2} \int P(k) \tilde{W}^2(kR) k^2 dk$$

$$\delta_c(t) = \frac{\delta_c}{D(t)}$$

$$f_{FU}(S, \delta_c) dS = \frac{1}{\sqrt{2\pi}} \frac{\delta_c}{S^{3/2}} e^{-\frac{\delta_c^2}{2S}} dS$$

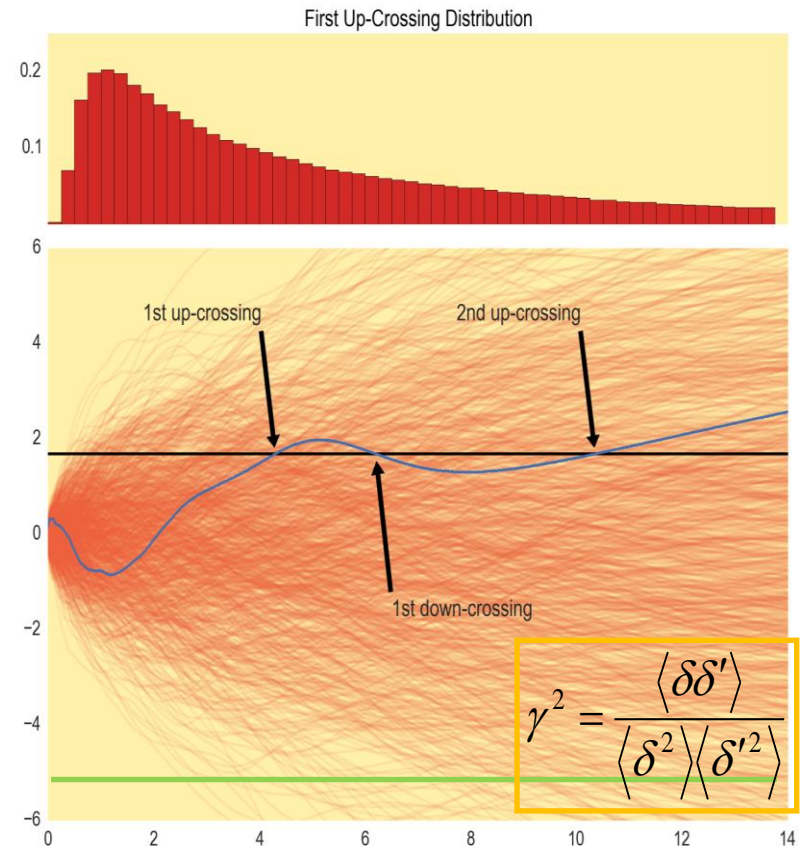
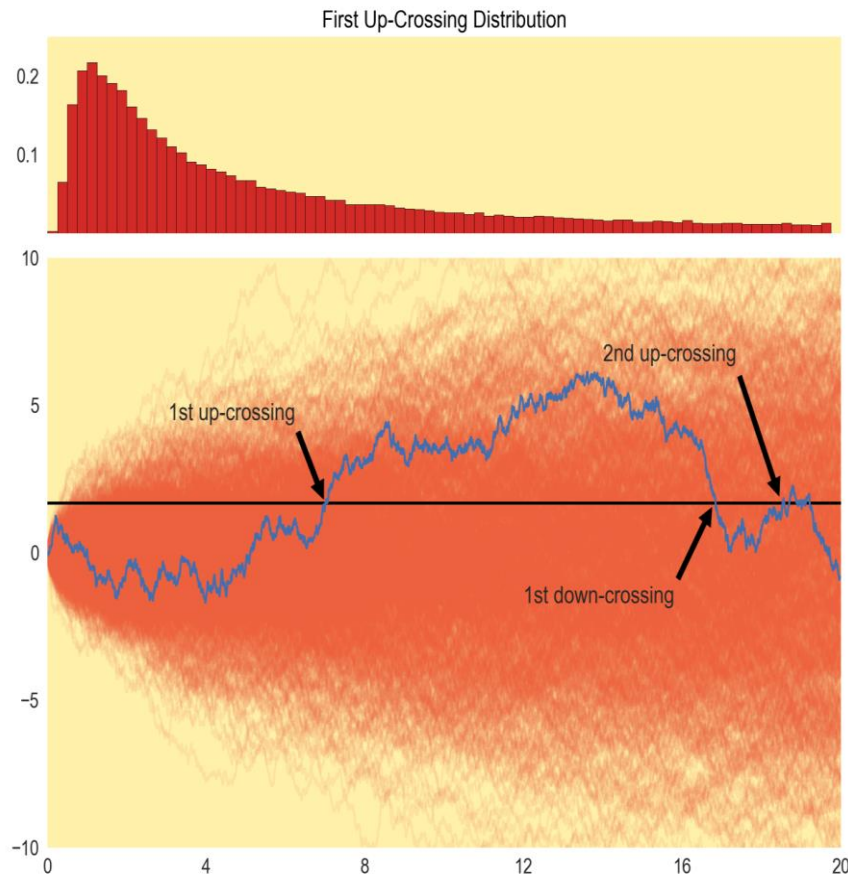
- ❖ SB et al. *Physical Review E* 99, 062101 (2019)
- ❖ Farnik Nikakhtar et al. , *MNRAS*, Volume 478, Issue 4, (2018)
- ❖ Farnik Nikakhtar, SB, *Phys. Rev. D* 96, 043524 (2017)



M. Reza Rahimitabar and Saman Moghimi @ SUT

Ravi K. Shet @ Pennsylvania

Stochastic Processes and Structure formation



$$\delta(s - \Delta s) < B(s - \Delta s)$$

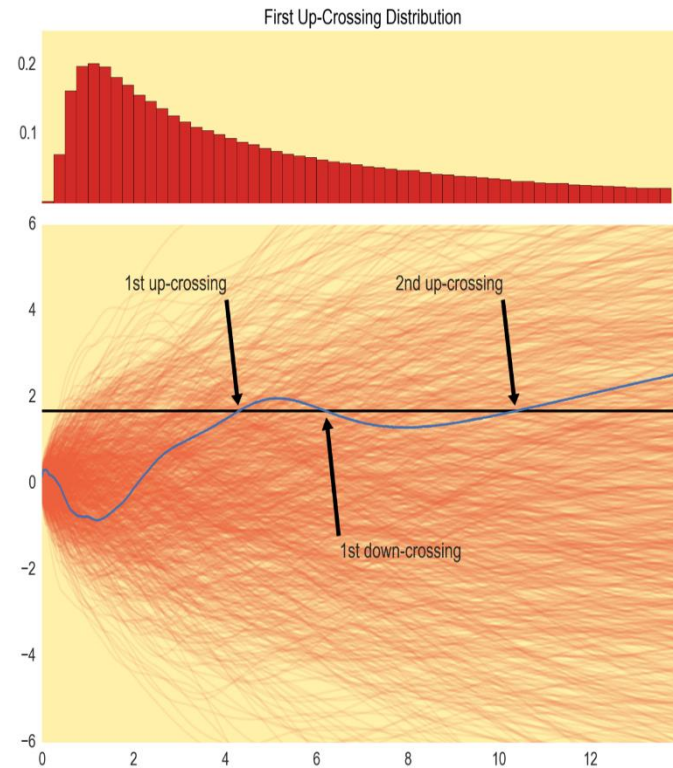
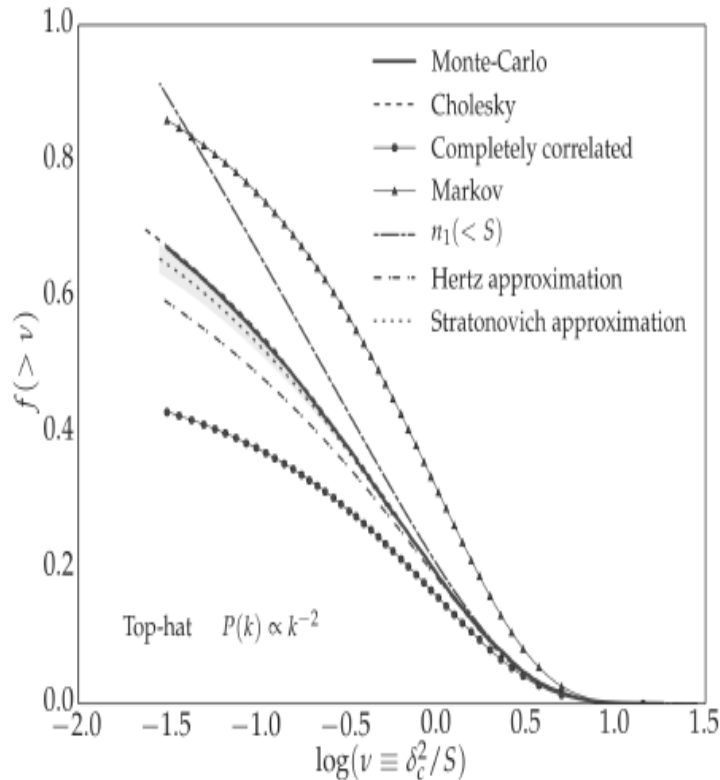
$$B(s) = \delta_c \rightarrow \delta_c \leq \delta \leq \delta_c + \Delta s \delta'$$

$$f(s) ds = \lim_{\Delta s \rightarrow 0} \int_0^{\delta_c + \Delta s \delta'} d\delta' \int_{\delta_c} d\delta P(\delta, \delta') \rightarrow f = f(v, \gamma)$$

One step beyond: The excursion set approach with correlated steps by Marcello Musso and Ravi K. Sheth, arXiv:1201.3876, MNRAS, Letters 423, 1, 2012, L102

Stochastic Processes and Structure formation

F.Nikakhtar @ Pennsylvania – NSF Fellow

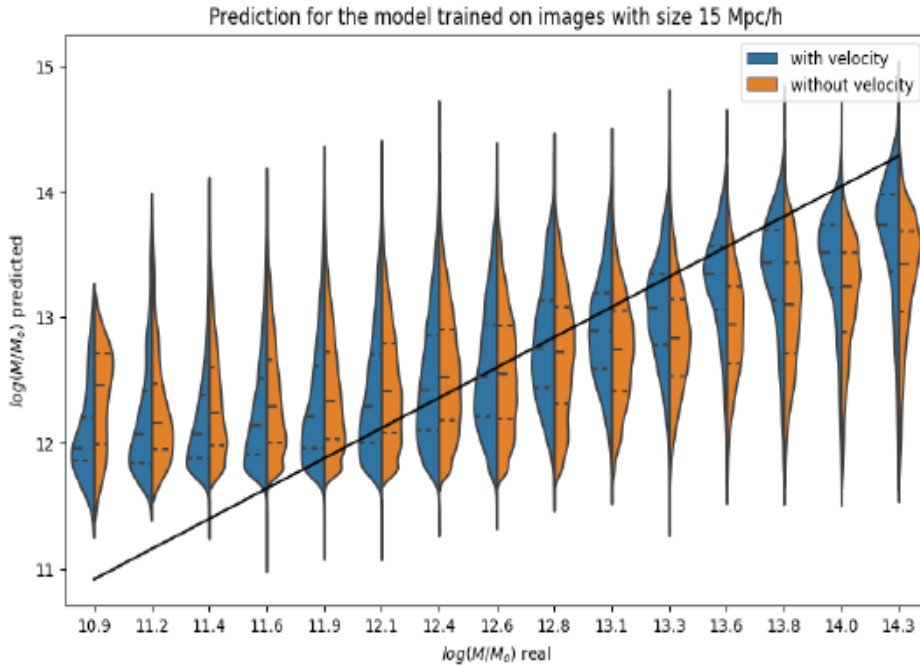


M.Ayromlou @ MPIA - Garching

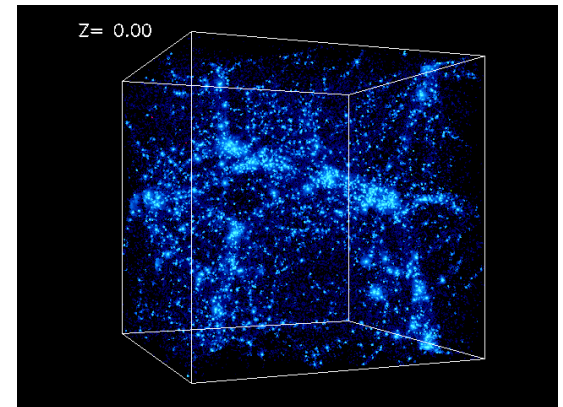
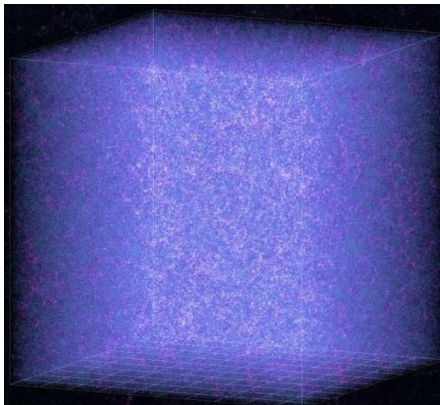
$$\langle \delta_i \delta_j \rangle = C_{ij} = \int \frac{dk}{k} \frac{k^3 P(k)}{2\pi^2} \tilde{W}(kR_i) \tilde{W}(kR_j)$$

$$\delta_i = L_{ij} \xi_j$$

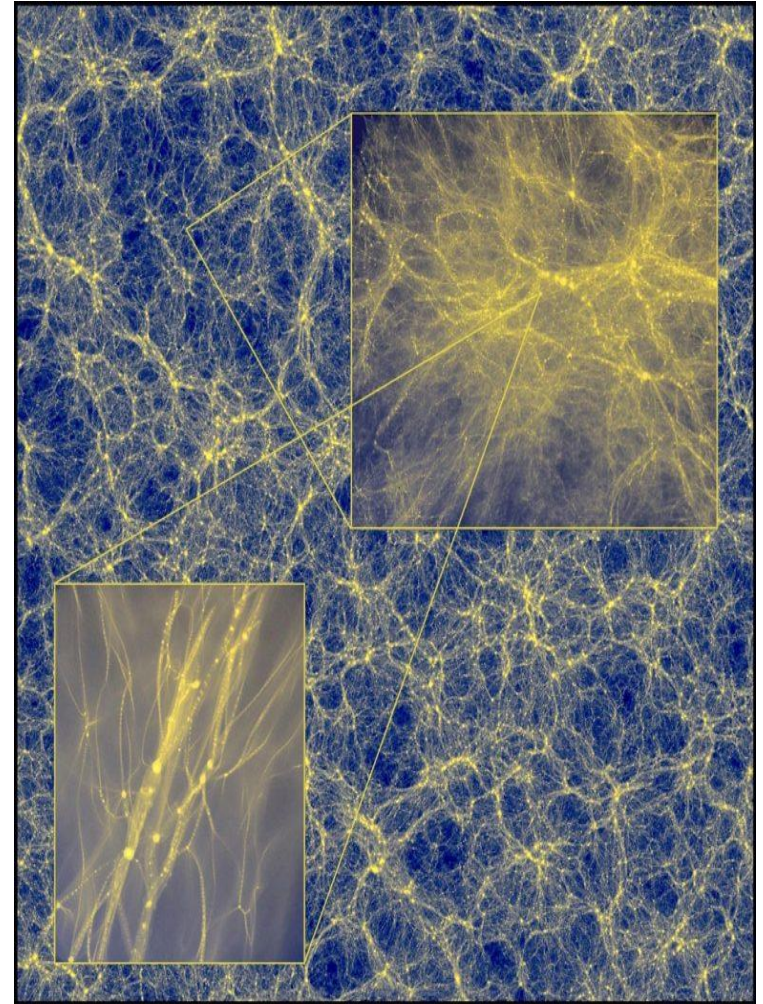
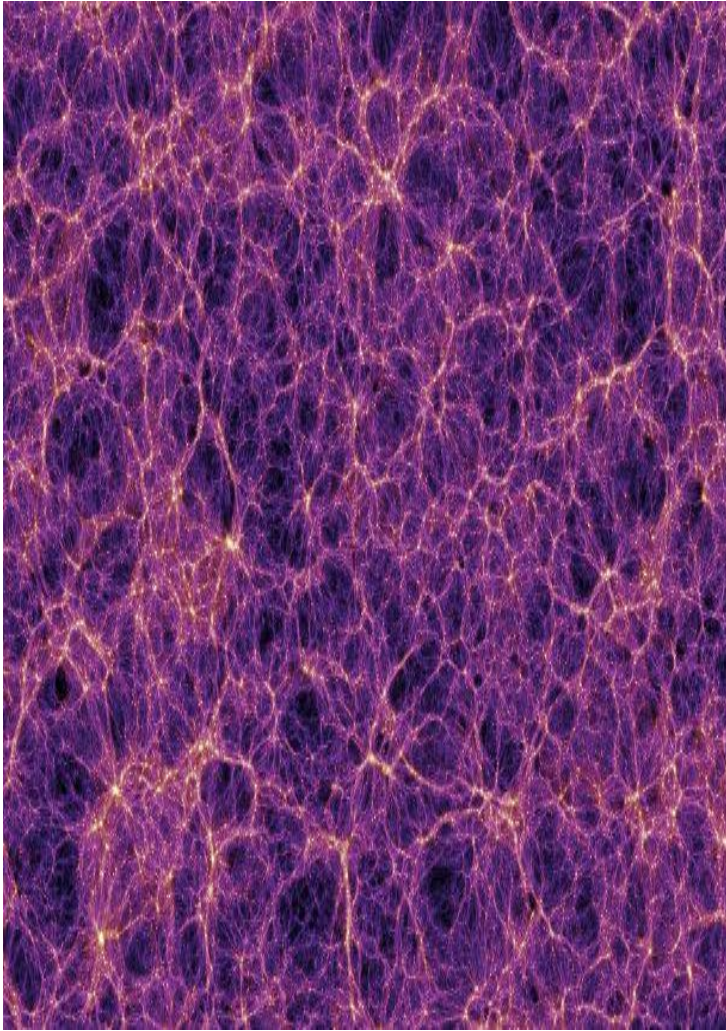
Small groups to Big science and Big Data



Sadegh Raiesi @ SUT



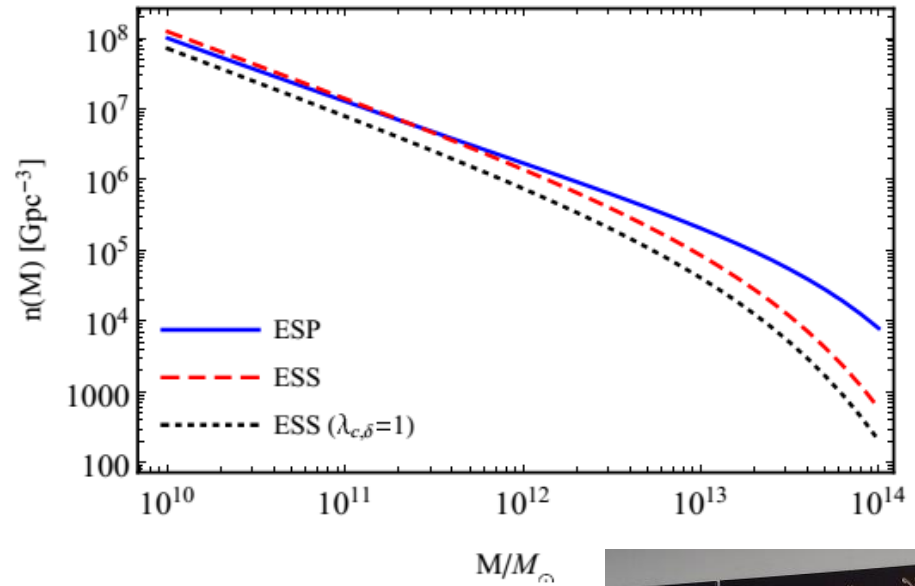
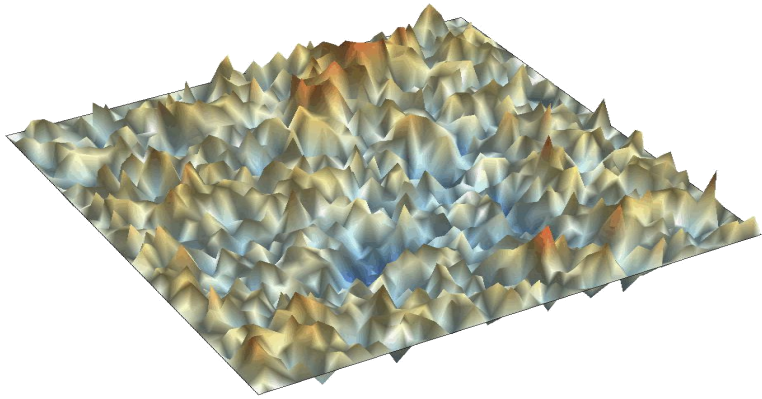
Cosmic Web



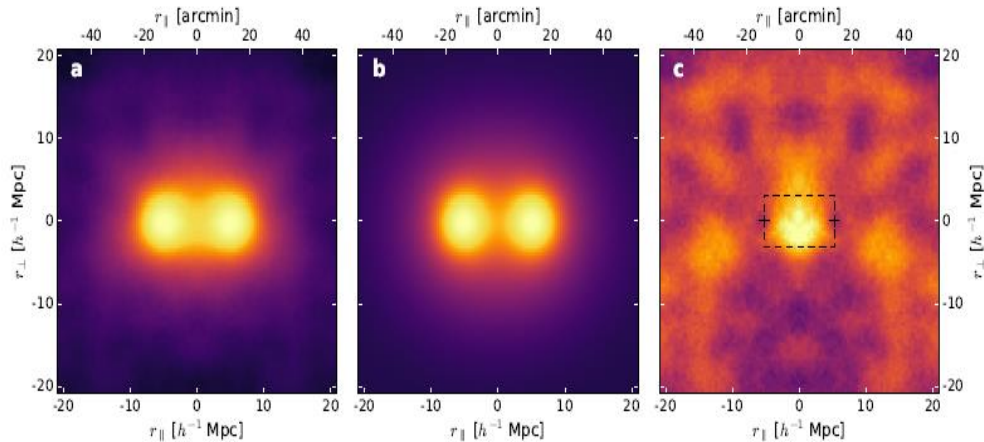
© Millenium – 2005 - 2020

When the nettle is young, the leaves make excellent greens; when it grows old it has filaments and fibers like hemp and flax ... **Victor Hugo**

Cosmic Web (Filaments, ...)



Mohammad Ansari, Sina Taamoli and SB
arXiv:1811.12398, MNRAS, 489, 1, 2019, Pages
900–909



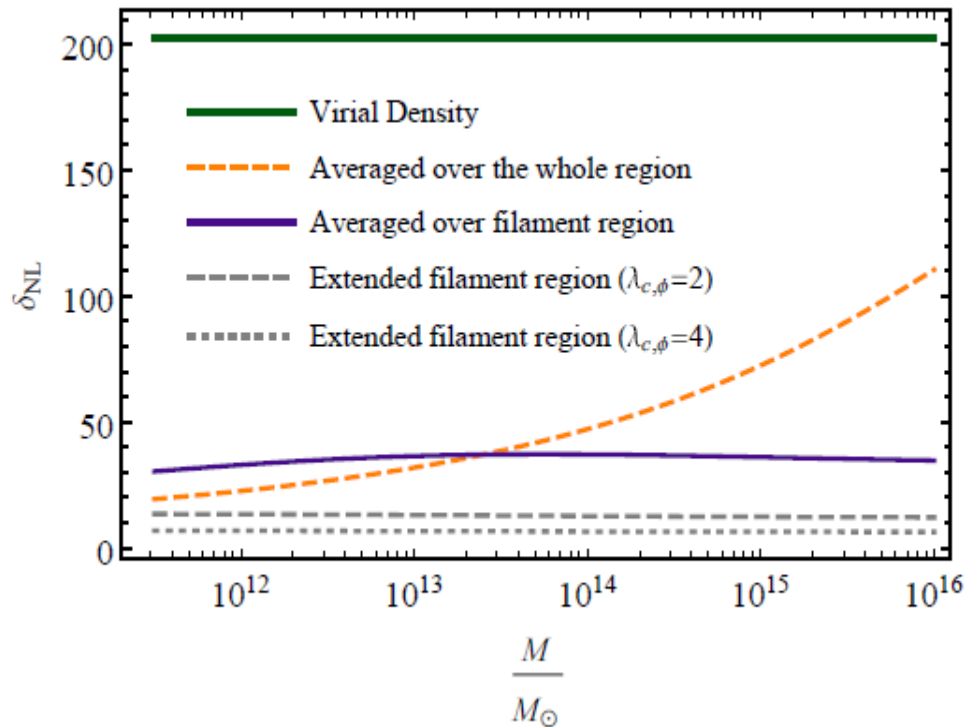
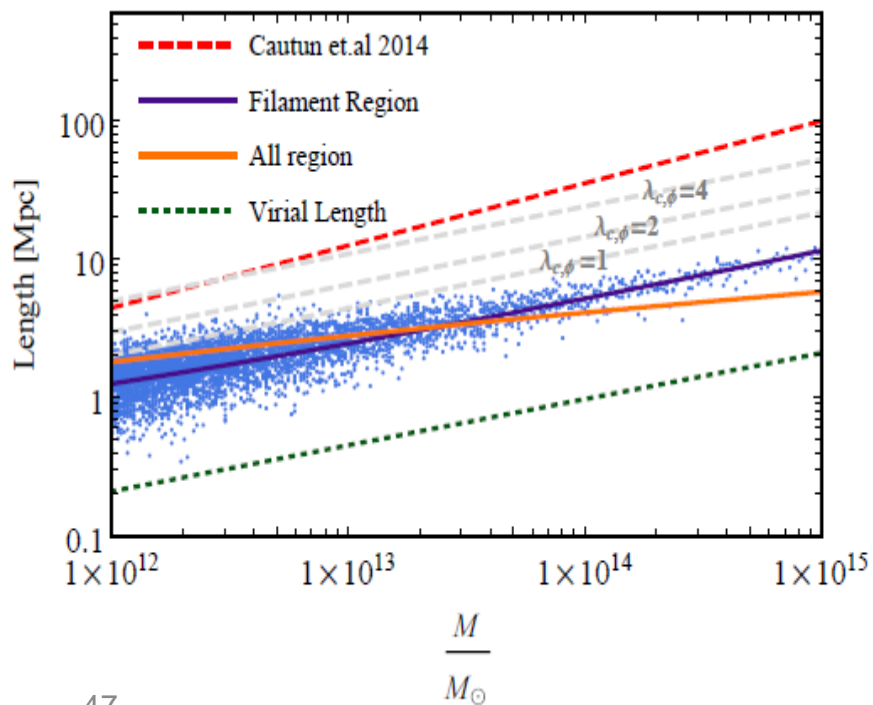
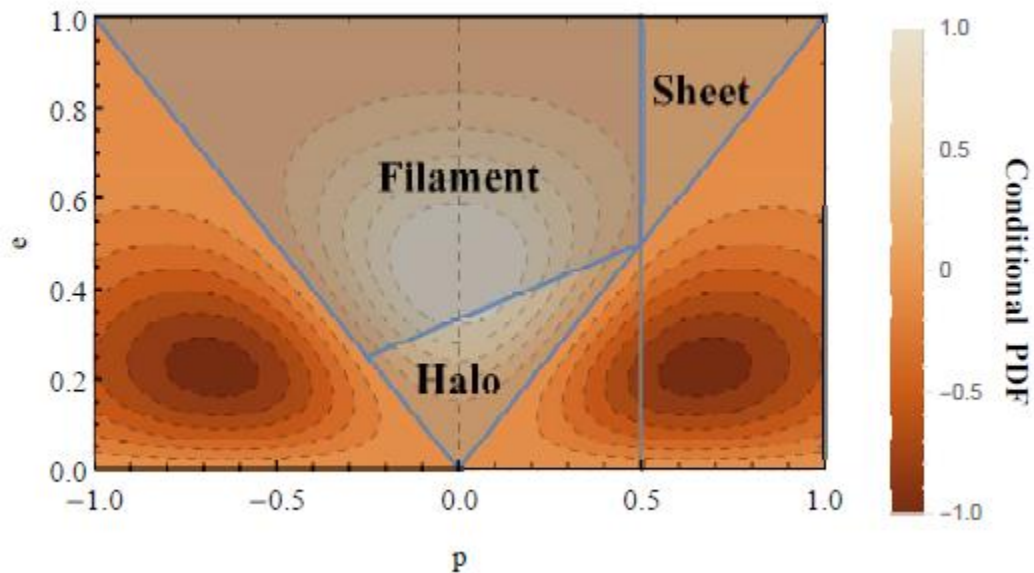
Missing baryons in the cosmic web revealed by the Sunyaev-Zel'dovich effect

Anna de Graaff¹, Yan-Chuan Cai¹, Catherine Heymans¹ & John A. Peacock¹

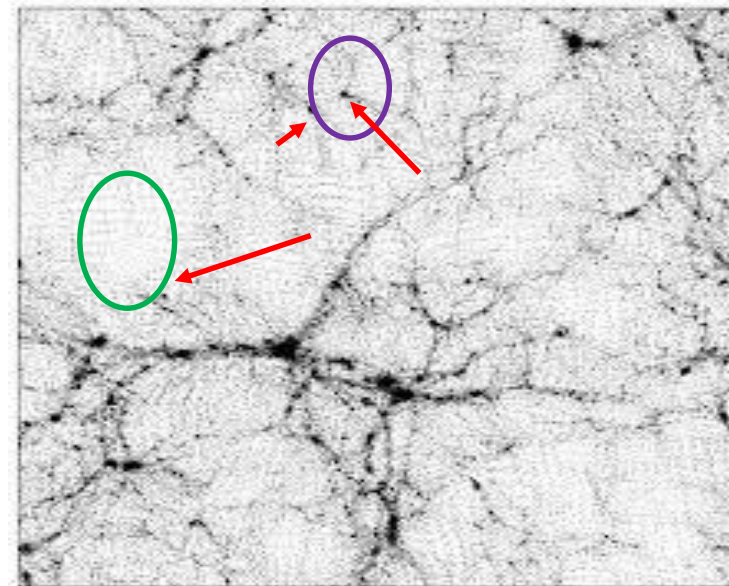
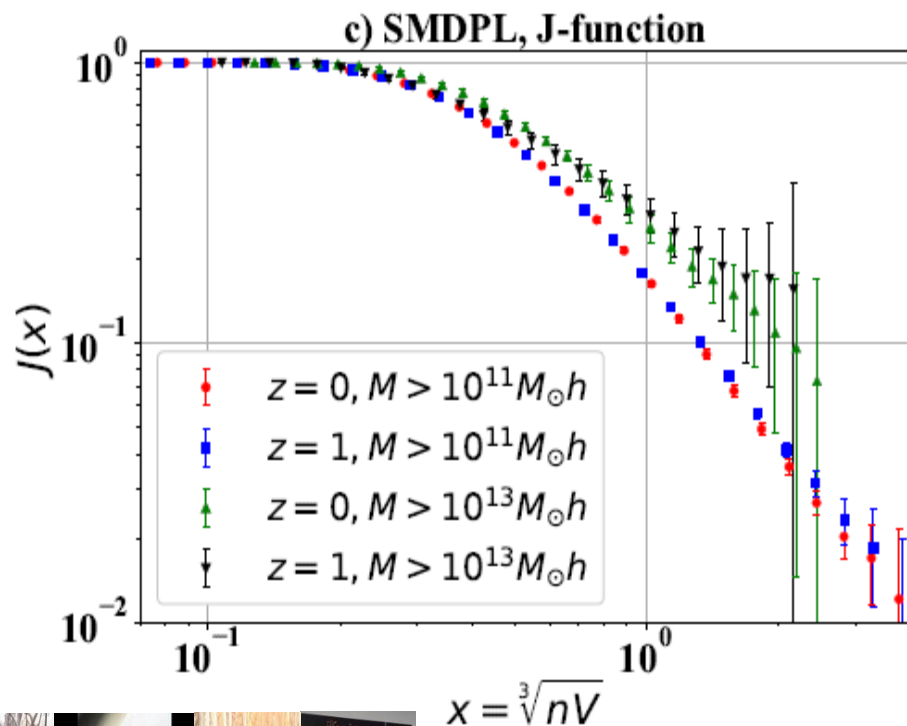


Mohammad Ansari
PhD candidate in SUT

Filaments! ESS



Distance Indicators...



$$J(r) = \frac{1 - NN(r)}{1 - SC(r)}$$



Nearest neighbour and spherical contact distribution in simulations and galaxy groups

Mohammad AnsariFard,¹ Zahra Baghkhani,¹ Laya Ghodsi,² Sina Taamoli,³
Farbod Hassani,⁴ Shant Baghram¹ *



Farbod Hassani @ Oslo

Rhapsody *

***A rhapsody in music is a one-movement work that is episodic yet integrated, free-flowing in structure, featuring a range of highly contrasted moods, colour, and tonality.**

Again P.J.E. Peebles

The natural science of cosmology

International Conference on Gravitation and Cosmology, Goa, December 2011

P J E Peebles

Joseph Henry Laboratories, Princeton University, Princeton NJ 08544, USA

E-mail: PJEP@Princeton.edu

1. Serendipitous discovery of suggestive phenomena
 2. The philosophical appeal of ideas
 3. Mathematical incompleteness
- ❖ Testing ideas
 - ❖ Anomalies
1. Learning to compute
 2. Adding decimal places

arXiv:1203.6334v1 [astro-ph.CO] 28 Mar 2012

James Peebles speaks to well wishers after his win.
(Eduardo Munoz/Reuters/TPX Images of the Day)



6 Lines of Thought to 6 parameter model

I. General relativity and the Universe

Asking for a **Homogenous and Isotropic one!**

II. Expanding Universe and measuring Ω

III. **Cosmic Microwave Background Radiation**

IV. Structure Formation and LSS

V. Subluminal matter

VI. Non-baryonic Dark Matter

❖ **Initial Conditions? ECP?**



Roya Mohayaee @ IAP



Hassan Firouzjahi @ IPM

6 Lines of Thought to 6 parameter model

I. General relativity and the Universe

Asking for a Homogenous and Isotropic one!

II. Expanding Universe and measuring Ω

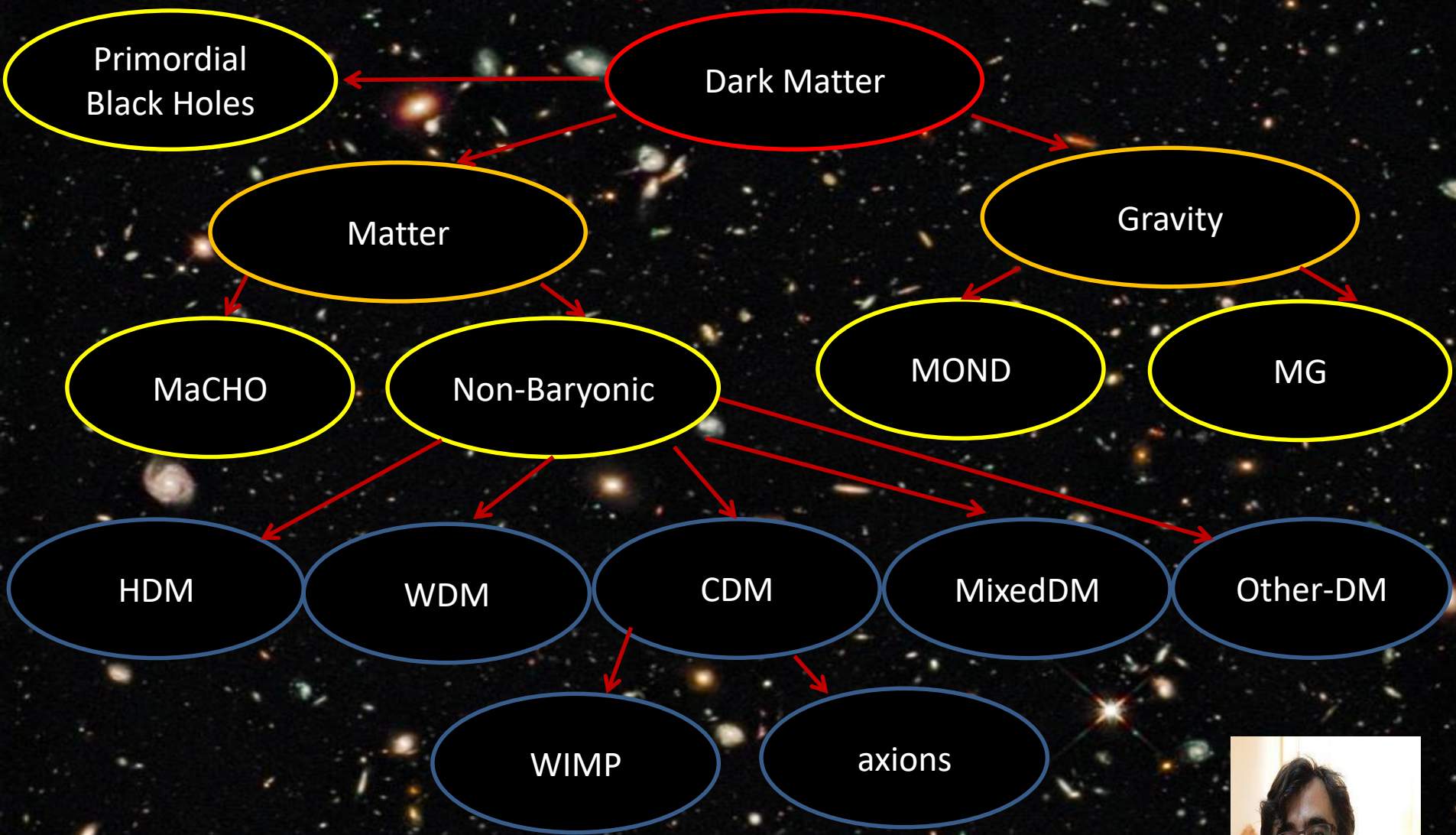
III. Cosmic Microwave Background Radiation

IV. Structure Formation and LSS

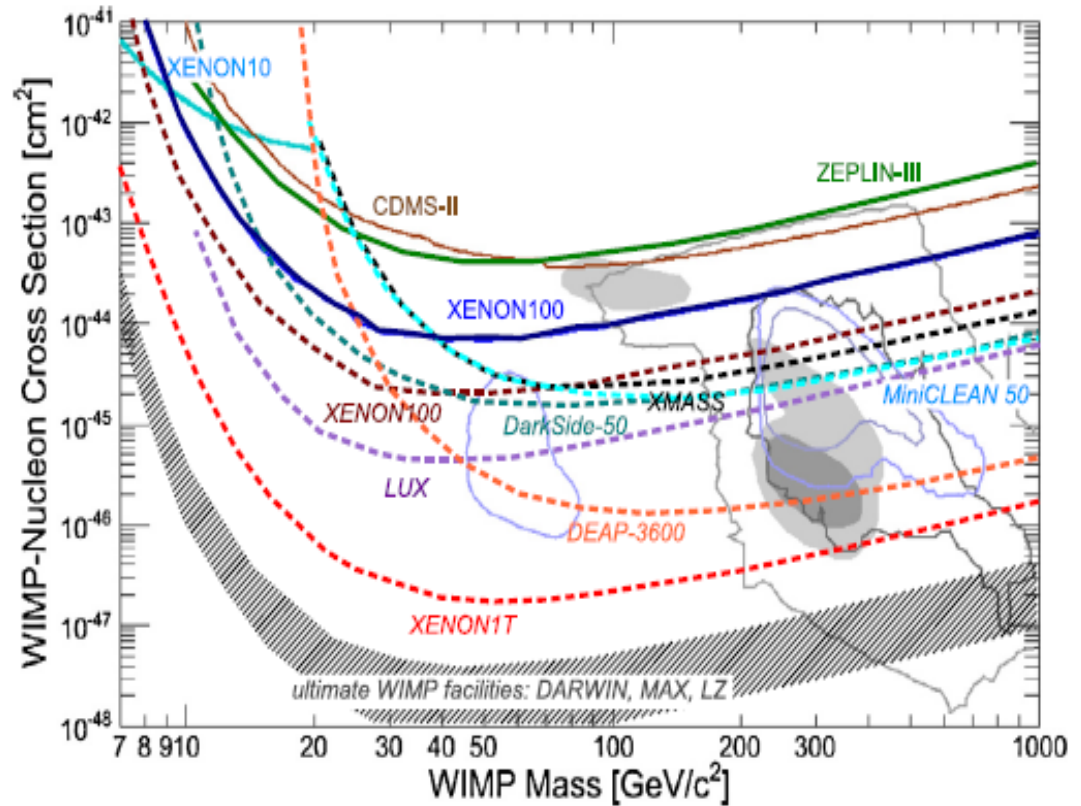
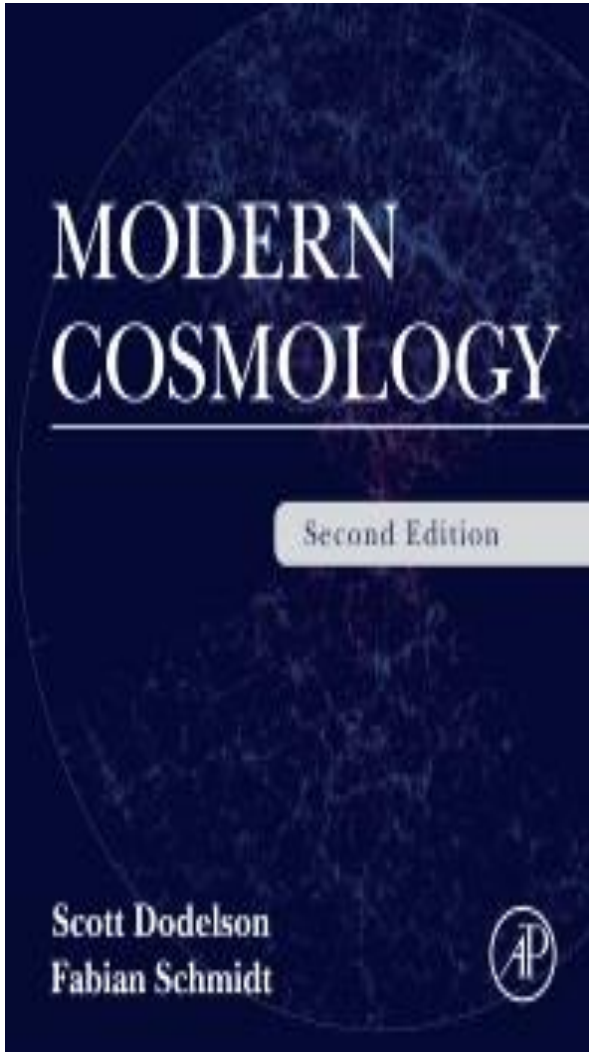
V. Subluminal matter

VI. **Non-baryonic Dark Matter**

❖ **Dark matter in galactic scales... modified CDM?!**

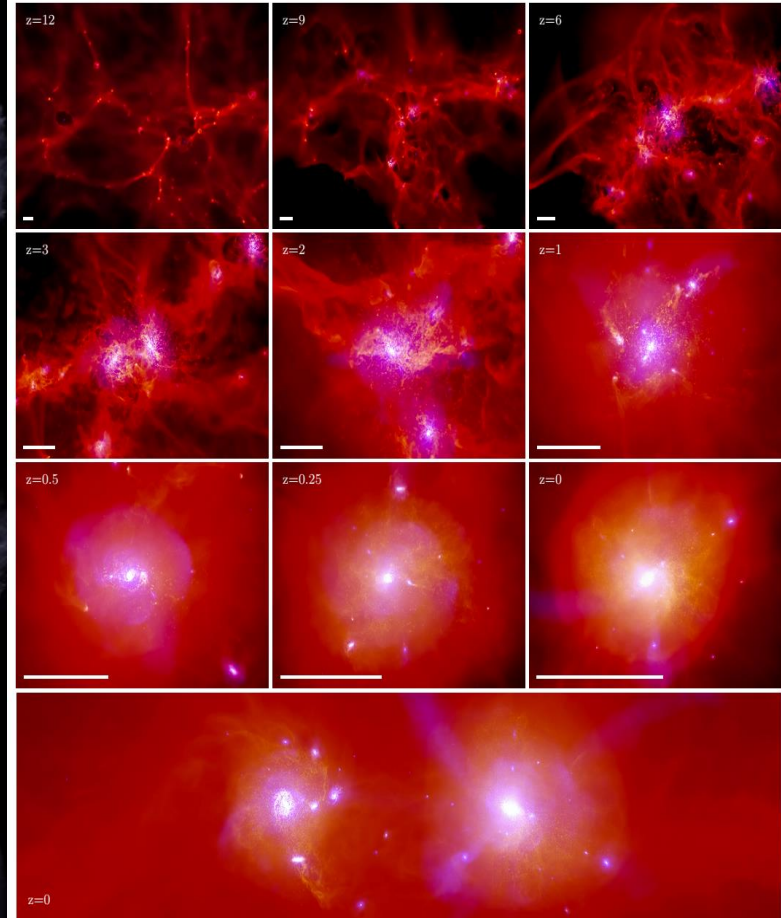
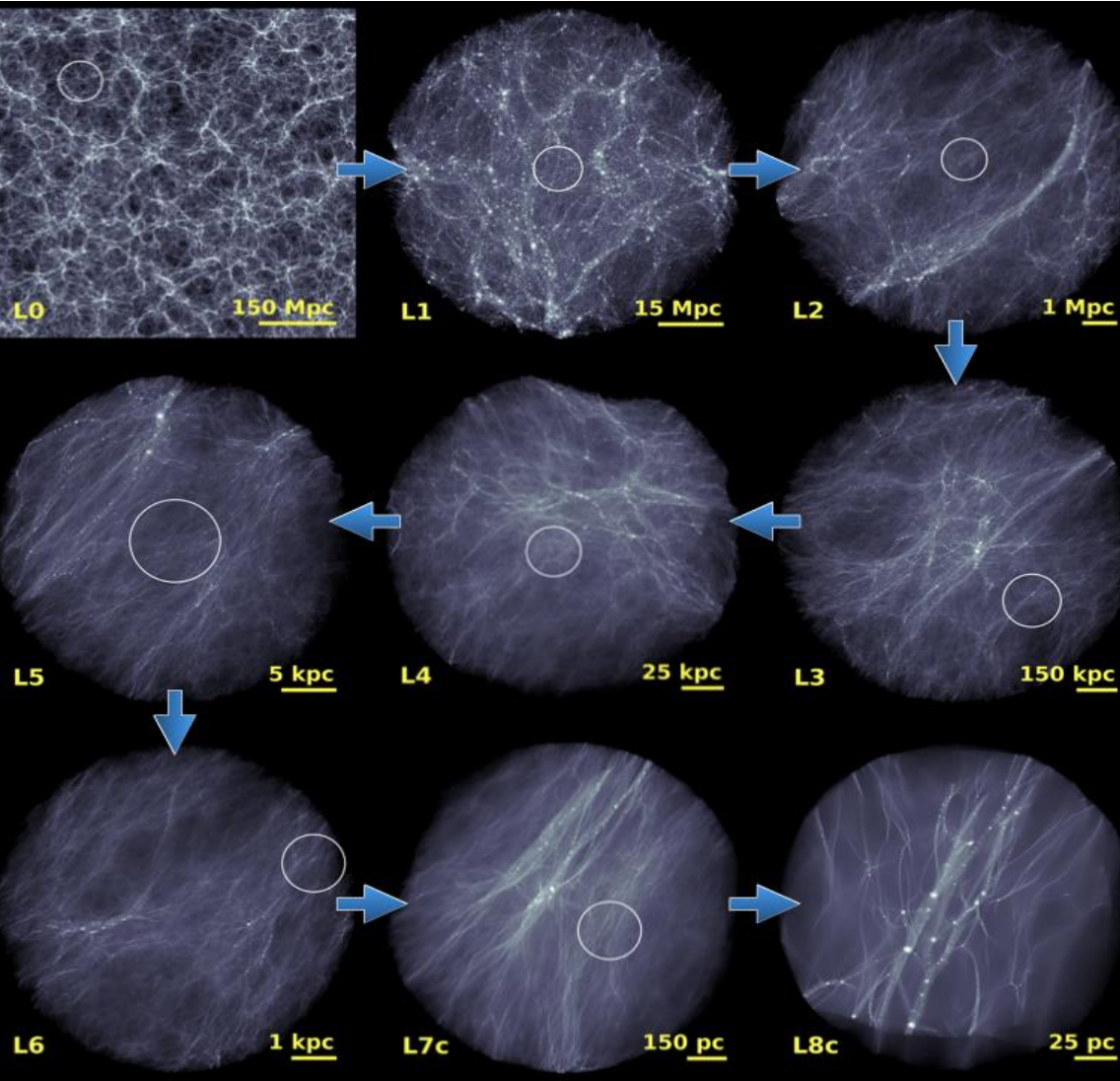


WIMPs



34 There are no classes in life for beginners; right away you are always asked to deal with what is most difficult,
Rainer Maria Rilke

The triumph of cosmology and computers

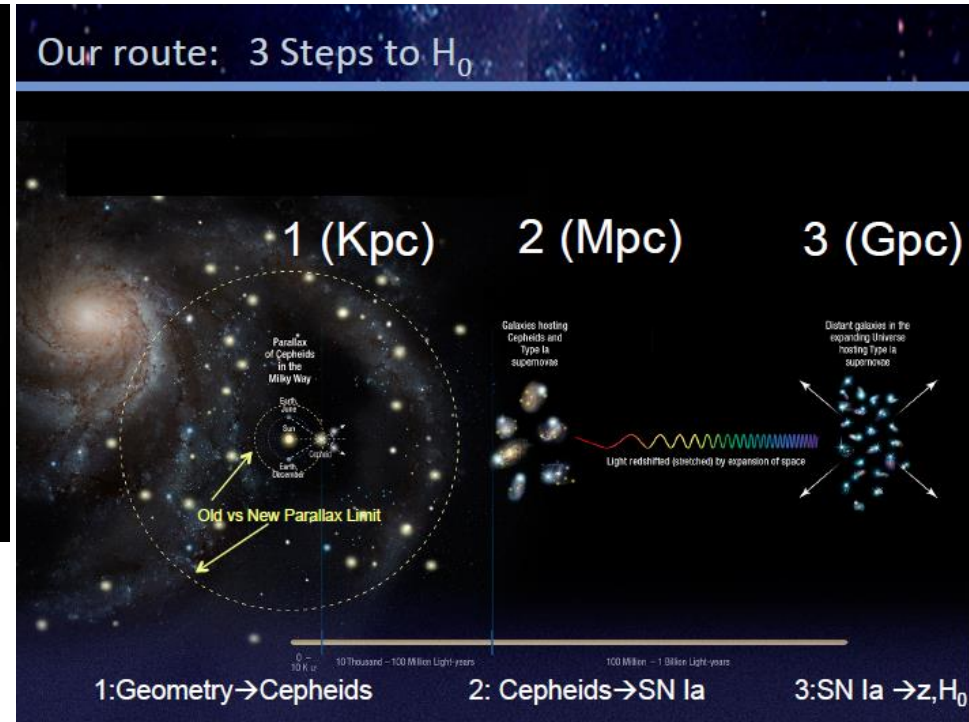
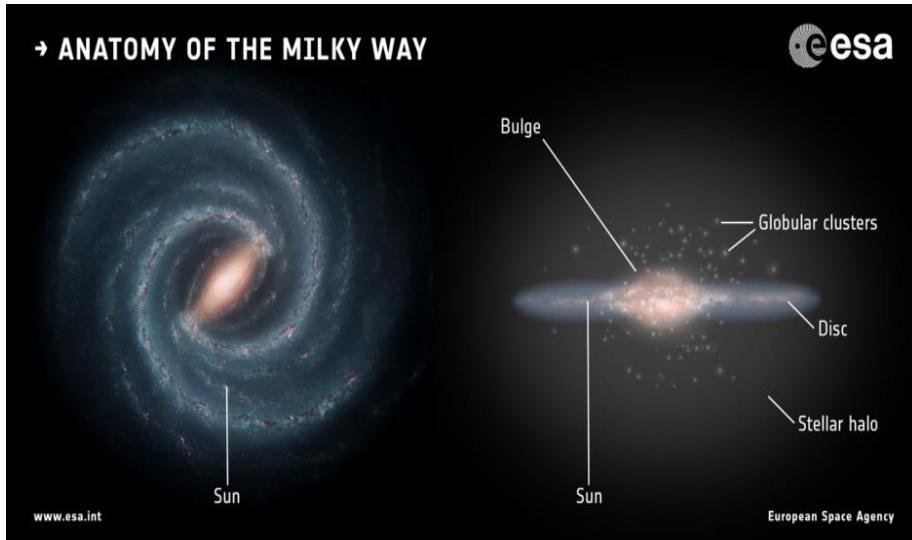


The APOSTLE simulations: solutions to the Local Group's cosmic puzzles Till Sawala , Carlos S. Frenk , Azadeh Fattahi , Julio F. Navarro et al. , Monthly Notices of the Royal Astronomical Society, Volume 457, Issue 2, 01 April 2016, Pages 1931–1943

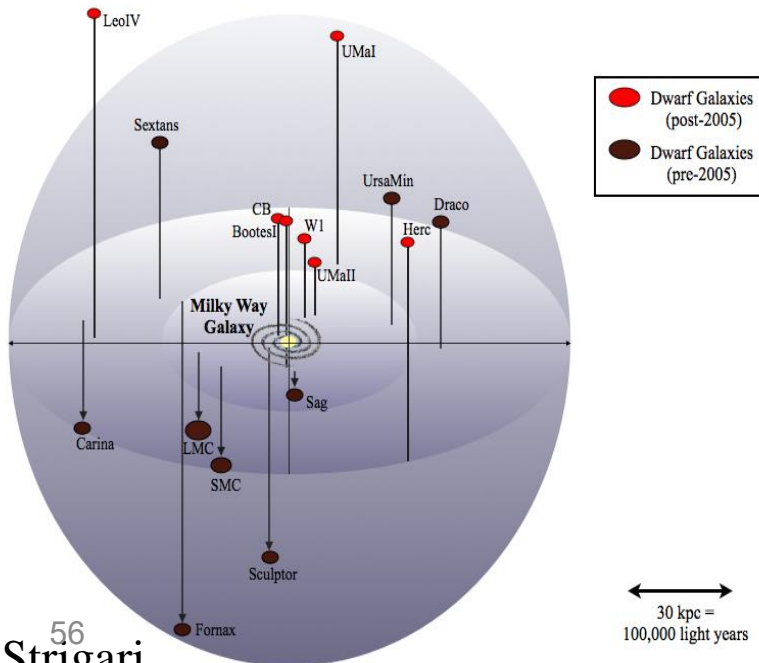
Universal structure of dark matter haloes over a mass range of 20 orders of magnitude

55

All about our neighborhood!



© Riess



- ❖ SB, Niayesh Afshordi, and Kathryn M. Zurek, *PRD* 84, 043511 (2011)
- ❖ Sohrab Rahvar, SB and Niayesh Afshordi, *PRD* 89, 063001 (2014)
- ❖ Alireza Maleki, SB, Sohrab Rahvar, *Phys. Rev. D* 101, 023508 (2020)
- ❖ Alireza Maleki, SB, Sohrab Rahvar, *Phys. Rev. D* 101, 103504 (2020)
- ❖ Hamed kameli and SB, *MNRAS*, V. 494, Issue 4, 2020, 4907

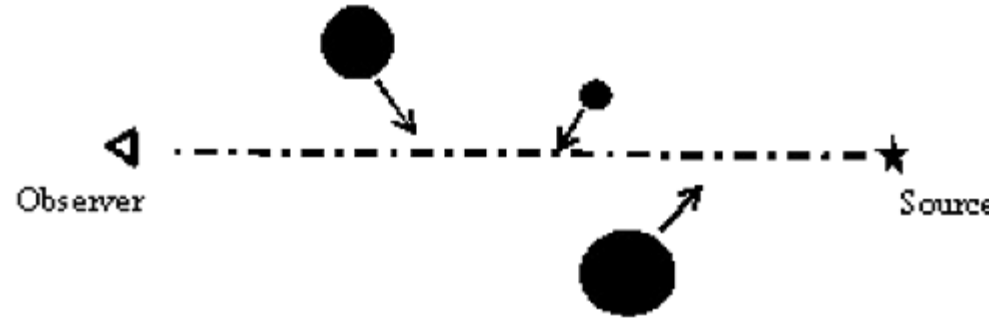
Searches for Dark Matter substructures



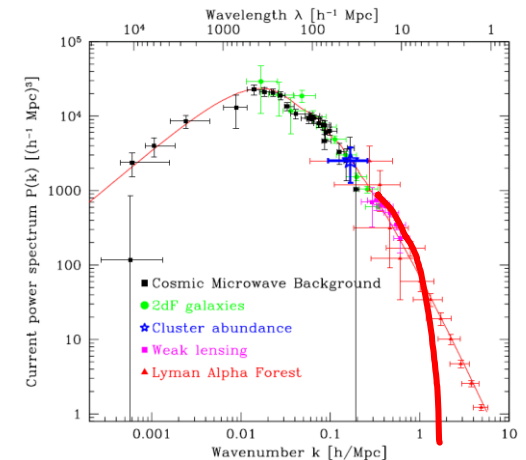
Sohrab Rahvar @ SUT



Niayesh Ashordi@ PI/Waterloo

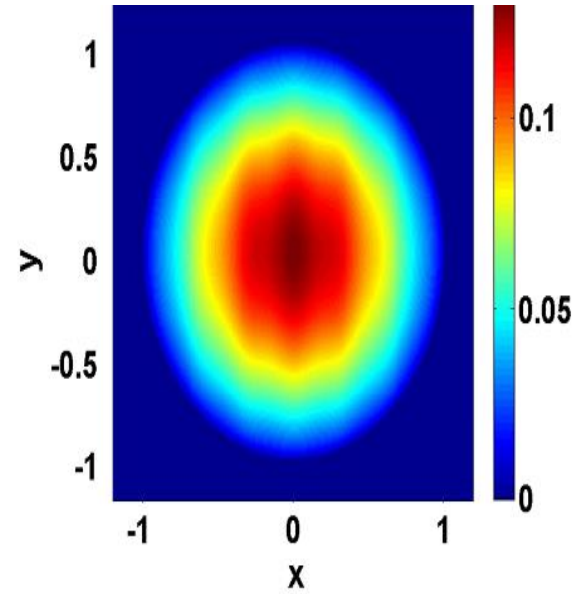
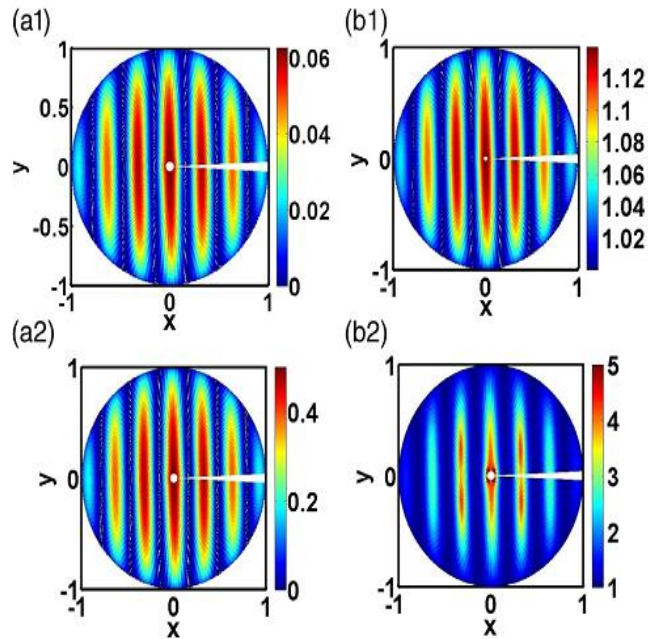
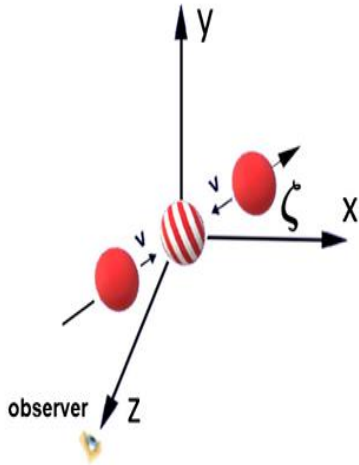


$$\begin{aligned} \omega P(\omega) = & 18\pi^2 H_0^4 \Omega_m^{(0)2} \int_0^{\chi_s} \left(1 - \frac{\chi'}{\chi_s}\right)^2 \chi'^2 d\chi' \\ & \times \int_0^\infty dv e^{-v^2/2\sigma^2} \left[\frac{v}{\sigma(\frac{\omega}{v}, z_{\chi'})}\right]^2 \\ & \times \frac{\Delta^2(\frac{\omega a}{v}, z_{\chi'})}{\omega} (1 + z_{\chi'})^3, \end{aligned}$$



SB, Niayesh Afshordi, and Kathryn M. Zurek, PRD 84, 043511 (2011)
Sohrab Rahvar, SB and Niayesh Afshordi, PRD 89, 063001 (2014)

Modified CDM and alternatives



PHYSICAL REVIEW D **101**, 023508 (2020)

Investigation of two colliding solitonic cores in fuzzy dark matter models

Alireza Maleki @ SUT

Alireza Maleki, Shant Baghrani, and Sohrab Rahvar

Department of Physics, Sharif University of Technology, P. O. Box 11155-9161 Tehran, Iran

What are the solutions galactic scale challenges of CDM?

- Baryonic Physics
- Modified CDM
- **Modified Initial Condition**



Modified initial power spectrum and too big to fail problem

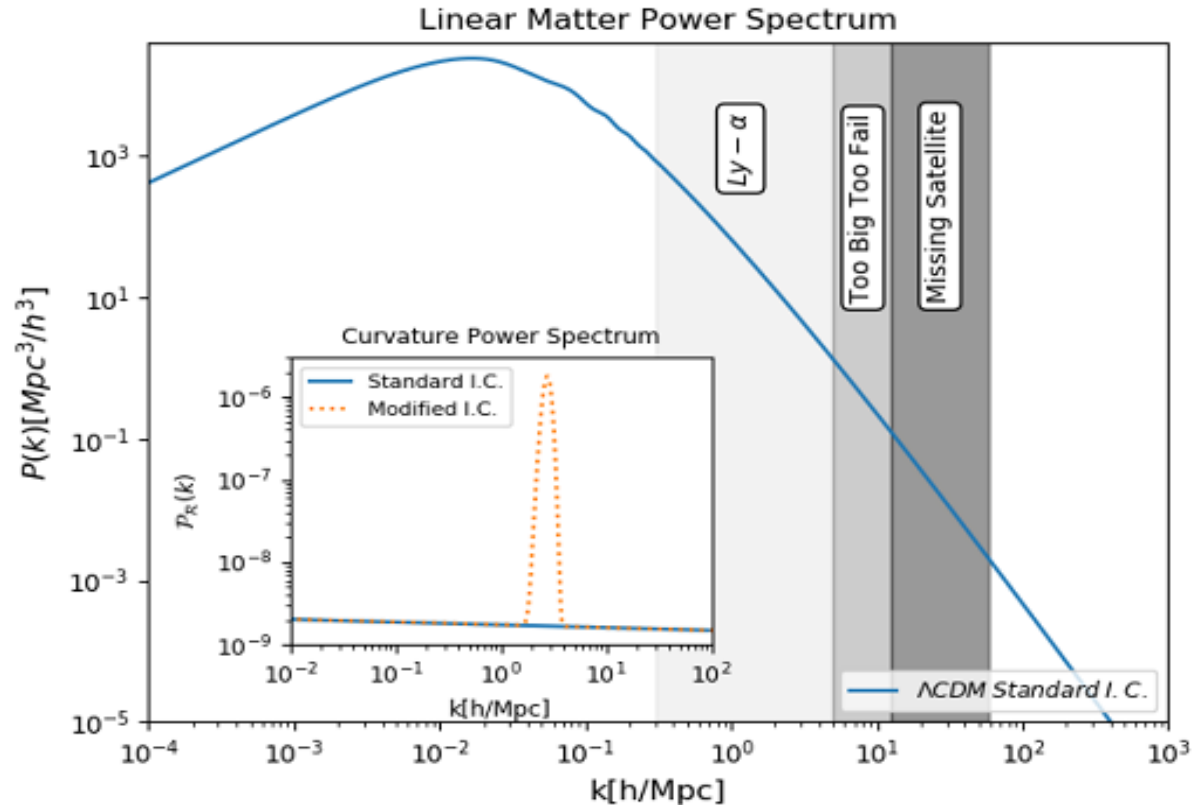
Hamed Kameli and Shant Baghram  

Department of Physics, Sharif University of Technology, PO Box 11155-9161, Tehran, Iran



Hamed Kameli @ SUT

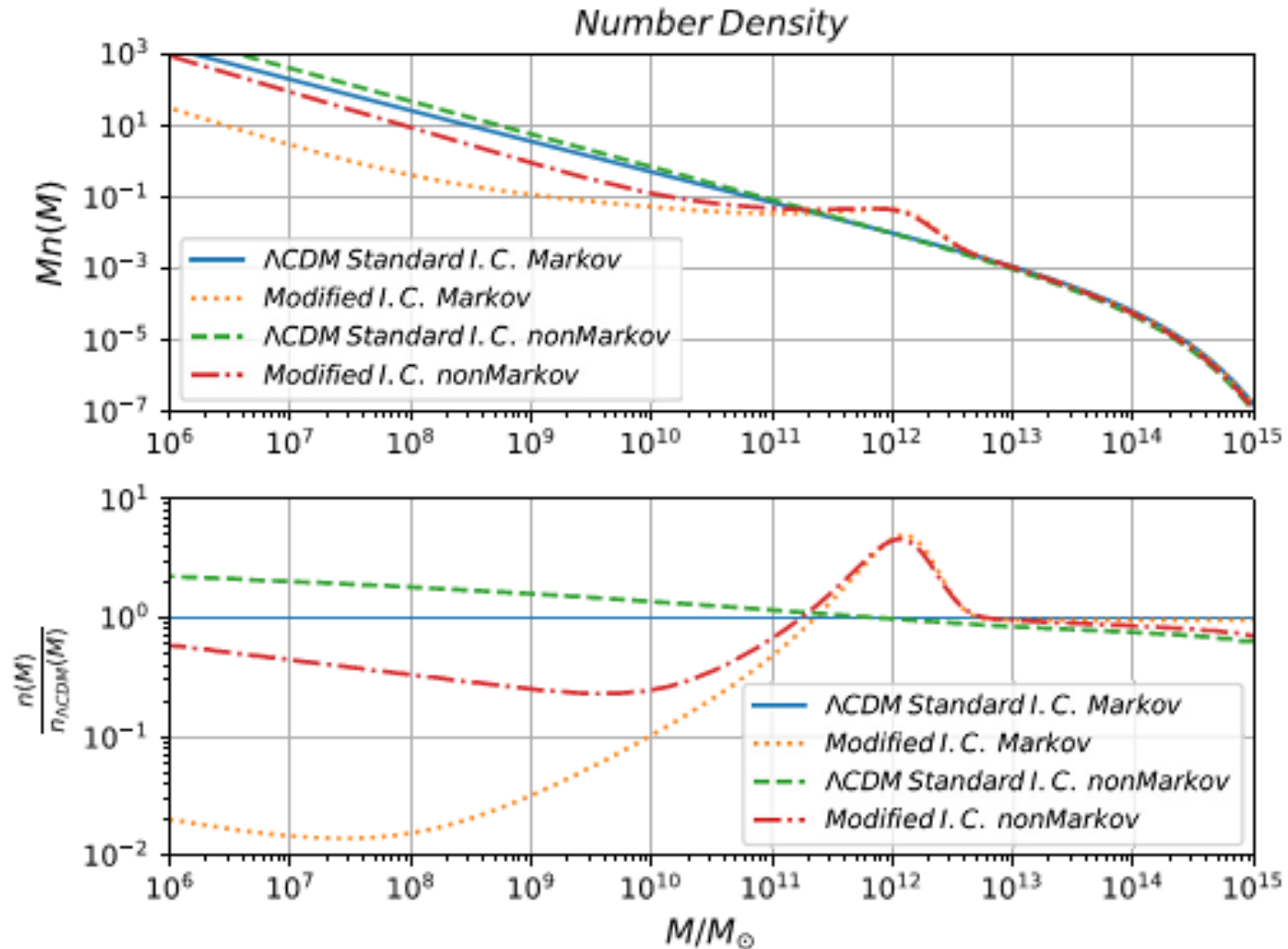
Small Scale power spectrum



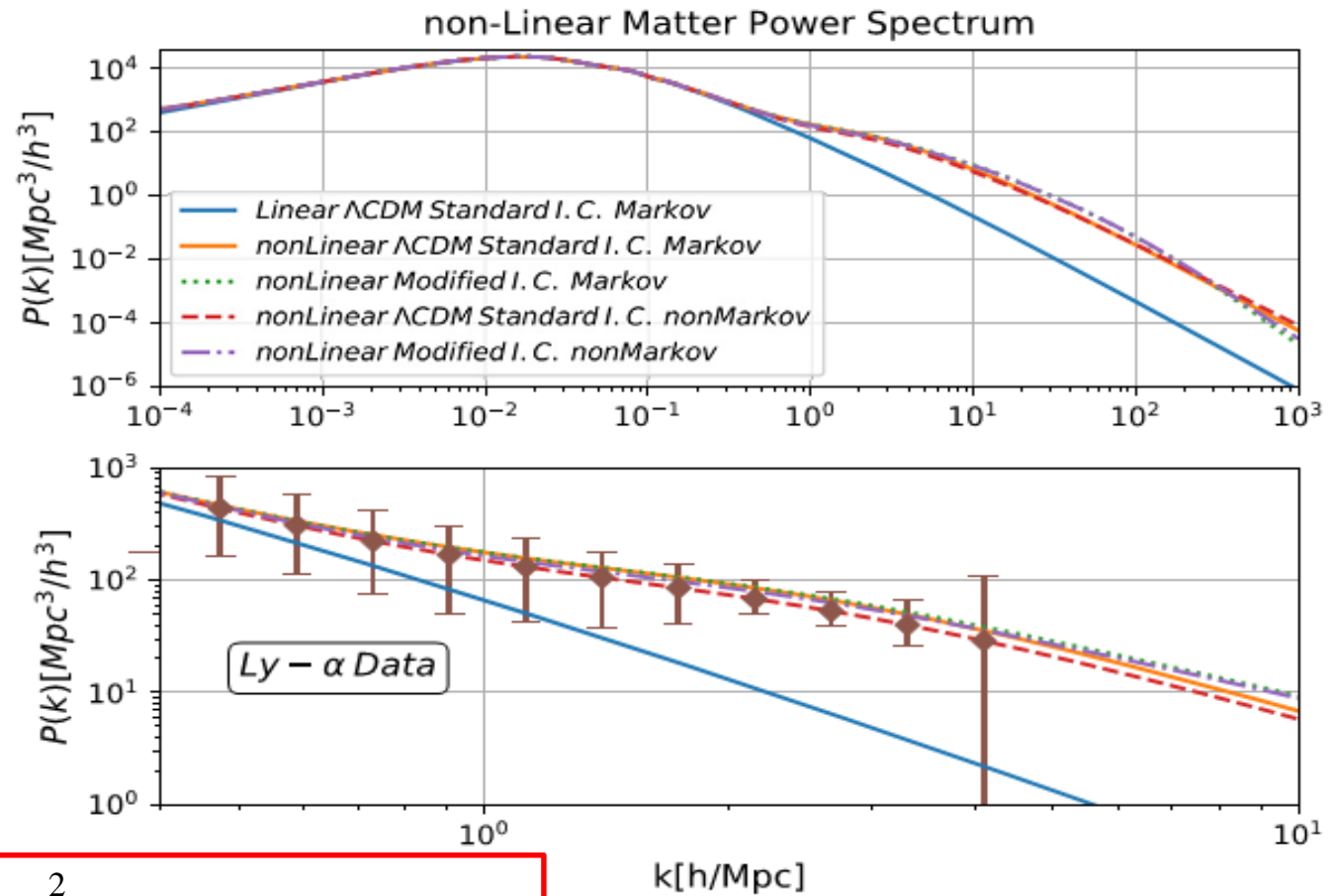
$$P_{\mathcal{R}}^{\text{bump}}(k) = \frac{A_b}{\sqrt{2\pi}\sigma_b} \exp \left[-(k - k_*)^2 / 2\sigma_b^2 \right],$$

$$k_* = 2.7 h Mpc^{-1} \Leftrightarrow M_* = 10^{11} M_{\text{sun}}$$

Number density of dark matter halos



Non linear Power spectrum and Lyman Alpha data



$$P^{1h}(k) = \int dm n(m) \left(\frac{m}{\bar{\rho}}\right)^2 |u(k|m)|^2$$

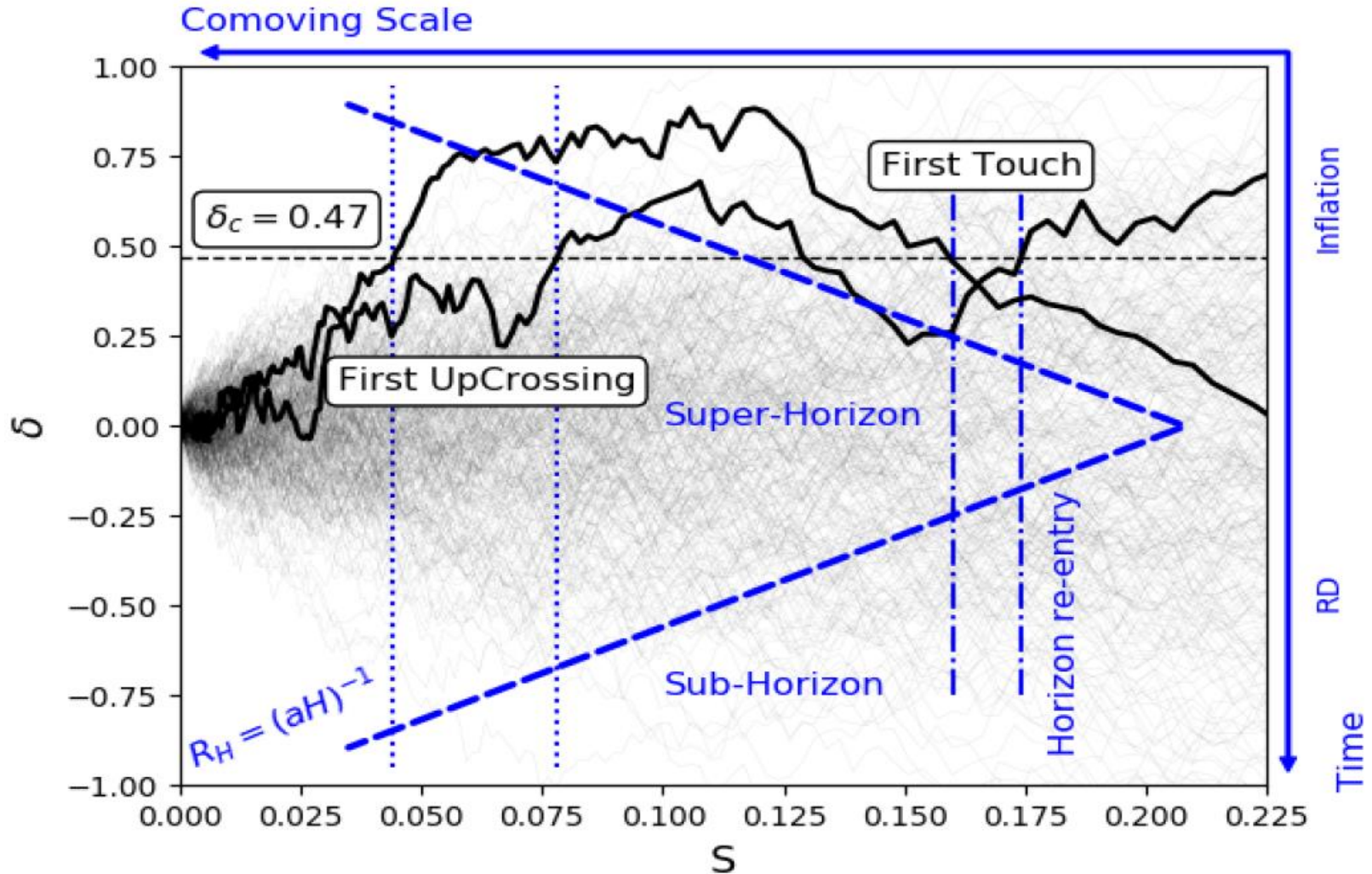
$$P^{2h}(k) = \int dm_1 n(m_1) \left(\frac{m}{\bar{\rho}}\right) |u(k|m_1)|$$

$$\times \int_{62} dm_2 n(m_2) \left(\frac{m_2}{\bar{\rho}}\right) |u(k|m_2)| P_{hh}(k|m_1, m_2)$$

Primordial Black Holes

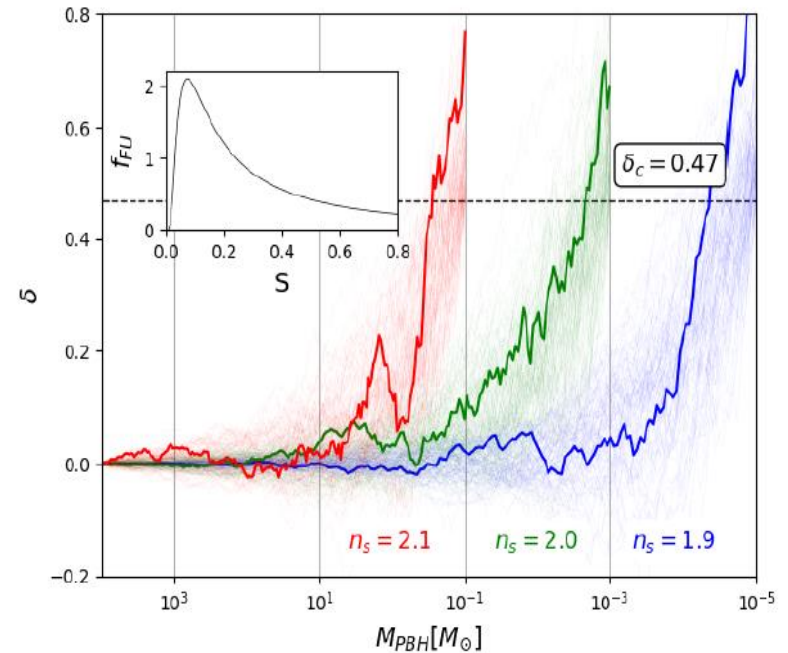


Primordial Black Holes



New constraints on primordial PS

	mass range	f_{PBH}	lower bound of mass range	spectral index	
				EST	PS
asteroid mass range	$(10^{16} - 10^{17})$ g	1	10^{16} g	1.490	1.616
sublunar mass range	$(10^{20} - 10^{24})$ g	1	10^{20} g	1.540	1.703
			10^{22} g	1.600	1.756
Subaru HSC	$(10^{-11} - 10^{-6}) M_{\odot}$	10^{-3}	$10^{-10} M_{\odot}$	1.604	1.560
			$10^{-8} M_{\odot}$	1.666	1.605
OGLE	$(10^{-6} - 10^{-3}) M_{\odot}$	10^{-2}	$10^{-6} M_{\odot}$	1.729	1.757
			$10^{-4} M_{\odot}$	1.845	1.835
EROS/MACHO	$(10^{-3} - 10^{-1}) M_{\odot}$	0.04	$10^{-3} M_{\odot}$	1.862	1.947
			$10^{-2} M_{\odot}$	1.942	1.970
sub-Solar mass range*	$(0.2 - 1.0) M_{\odot}$	0.02	$0.2 M_{\odot}$	2.018	2.046
			$0.6 M_{\odot}$	2.115	2.078
		1	$0.2 M_{\odot}$	2.028	2.258
			$0.6 M_{\odot}$	2.126	2.297
intermediate mass range	$(10^1 - 10^3) M_{\odot}$	10^{-4}	$10 M_{\odot}$	2.103	1.848
			$10^2 M_{\odot}$	2.204	1.911
SLABs	$\geq 10^{11} M_{\odot}$	1	$10^{11} M_{\odot}$	5.220	5.598
			$10^{12} M_{\odot}$	6.660	6.891



Intermezzo*

* In music, an intermezzo, in the most general sense, is a composition which fits between other musical or dramatic entities, such as acts of a play or movements of a larger musical work.

Every evening words, not stars, light the sky Umberto Saba
1883 – 1957 live and write in Trieste

6 Lines of Thought to 6 parameter model

I. General relativity and the Universe

Asking for a Homogenous and Isotropic one!

II. Expanding Universe and measuring Ω

III. Cosmic Microwave Background Radiation

IV. Structure Formation and LSS

V. Subluminal matter

VI. Non-baryonic Dark Matter

❖ **Beyond Einstein in cosmological scales? The legacy of Λ ?**

A four sigmaish tension - 2019

Any cracks in this standard cosmological model might herald yet another surprise in our understanding of the cosmos

$$H_0 = 74.03 \pm 1.42 \text{ km / s / Mpc}$$

1.9%
Measurement

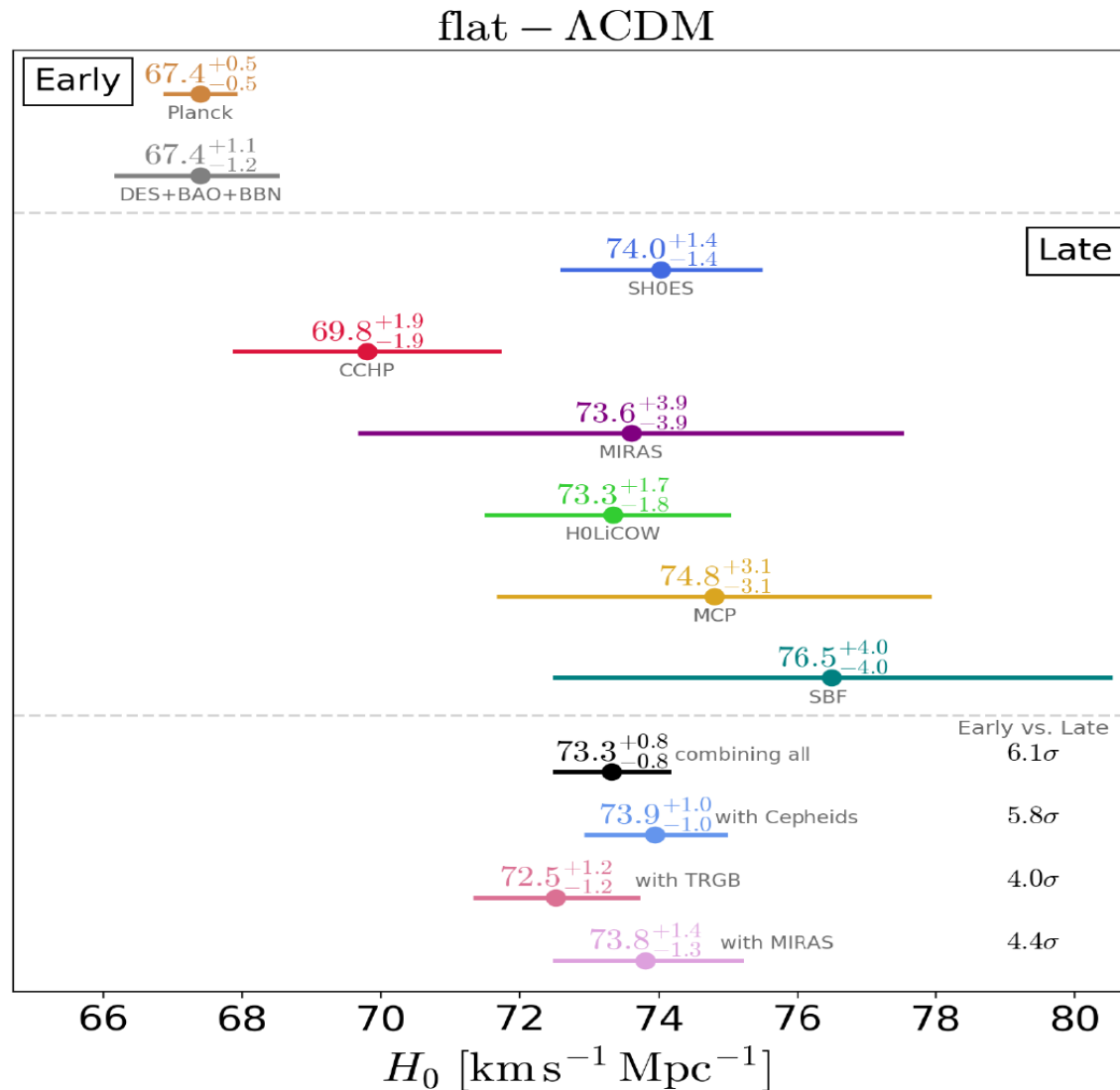
$$H_0 = 67.27 \pm 0.60 \text{ km / s / Mpc}$$

0.9%
Measurement

$$H^2 = \left(\frac{\dot{a}}{a}\right)^2 = \frac{8\pi G}{3} (\rho_\gamma + \rho_{\nu(\text{rel})} (N_\nu T^4) + \rho_m + \rho_b + \rho_\Lambda a^{-3(1+w)})$$

- Planck 2018 results. VI. Cosmological parameters, arXiv:1807.06209
- Adam G. Riess, Stefano Casertano, Wenlong Yuan, Lucas M. Macri, Dan Scolnic, The Astrophysical Journal, Volume 876, Number 1, 2019, <https://arxiv.org/abs/1903.07603v2>

A challenge in cosmological scales



Tensions between the Early and the Late Universe L. Verde , T. Treu , A.G. Riess, Nature Astronomy volume 3, pages891–895(2019)

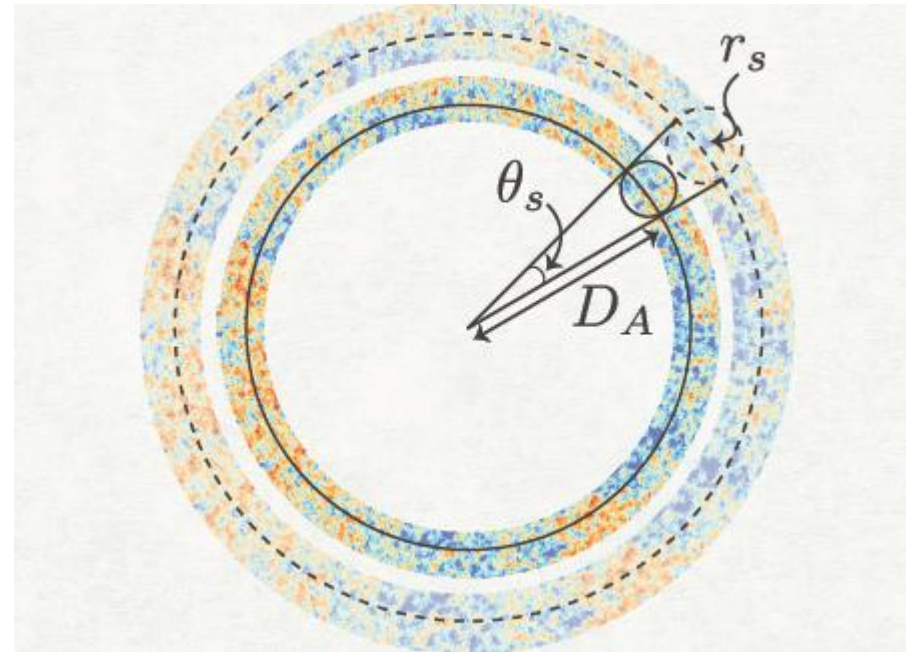
Angular diameter distance to CMB

- The angle in which we see the first peak of CMB is an observable

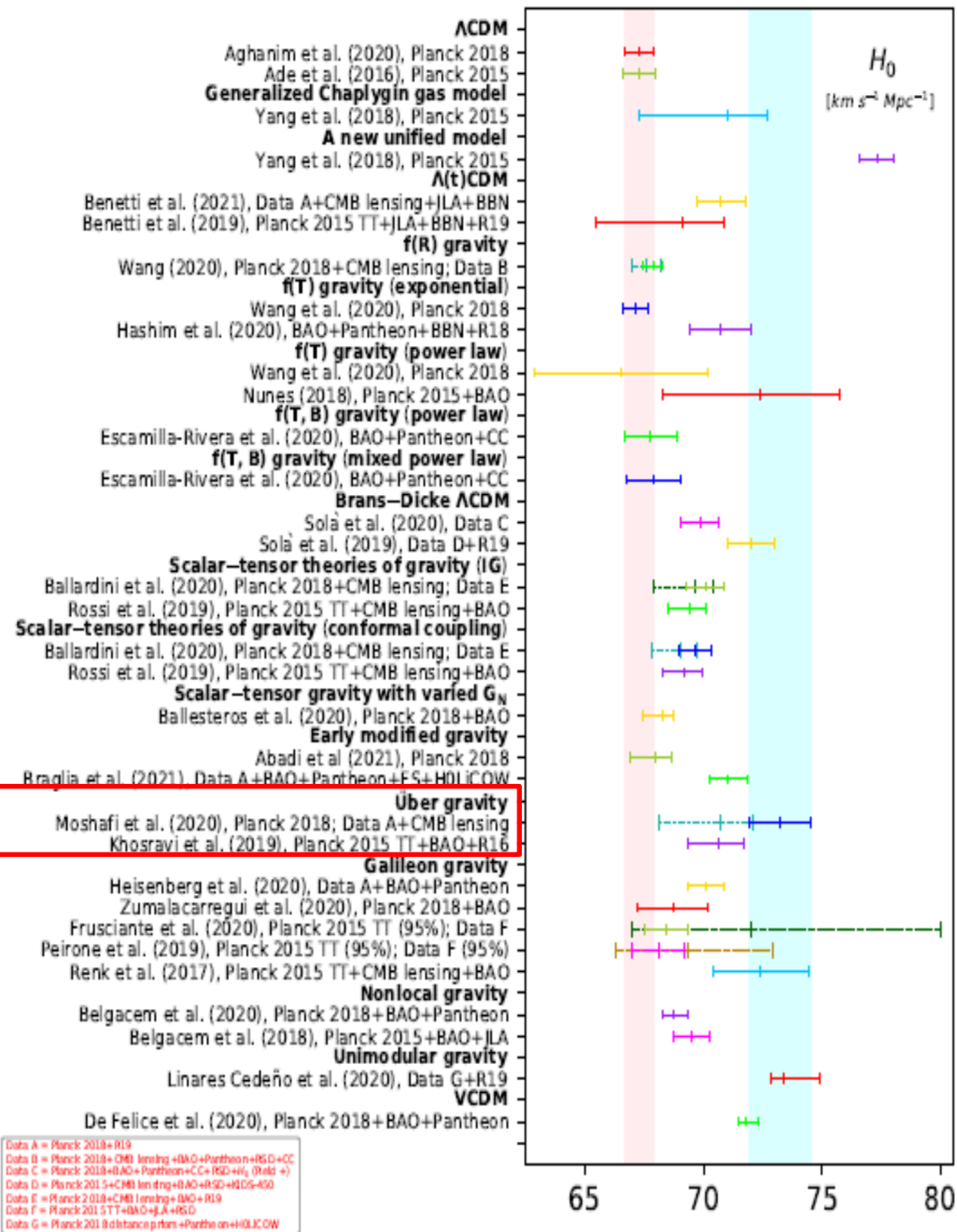
$$\theta = \frac{r_s^*}{d_A}$$

$$d_A = \frac{1}{1+z} cH_0^{-1} \int \frac{dz}{E(z)}$$

$$r_s^* = \int_0^{t_*} \frac{dt c_s(t)}{a(t)} = \int_{z_*}^{\infty} \frac{dz c_s(t)}{H(z)}$$



- Higher H_0 means smaller d_A in order to compensate, we should have smaller r_s^*
- Early Universe** Solutions and **Late Time** Solutions



*Nima Khosravi
@ SBU*



*Niayesh Ashordi@
PI/Waterloo*



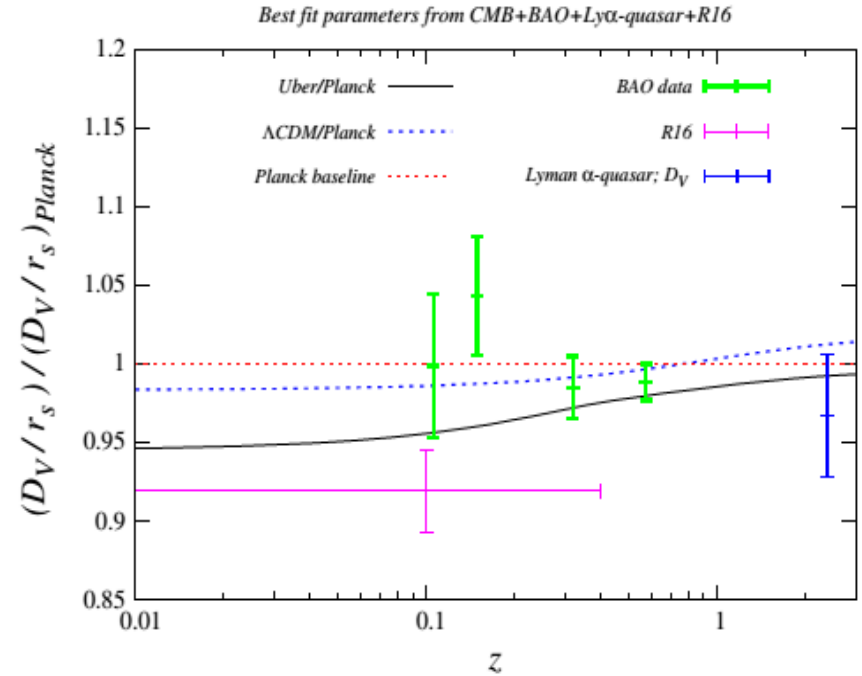
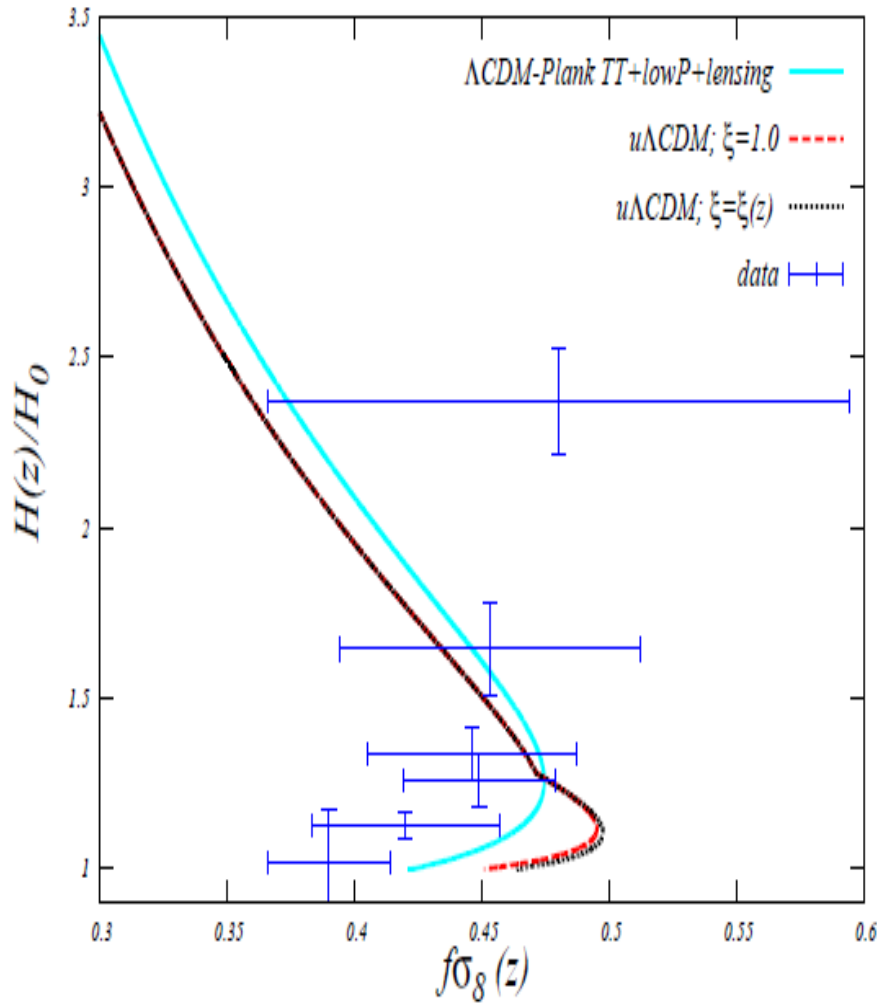
*Hossein
Moshafi @ IPM*



*Natacha Altamirano
@ PI/Waterloo*

$\ddot{u}\Lambda\text{CDM}$ as an

example of late time solution to the H_0 problem

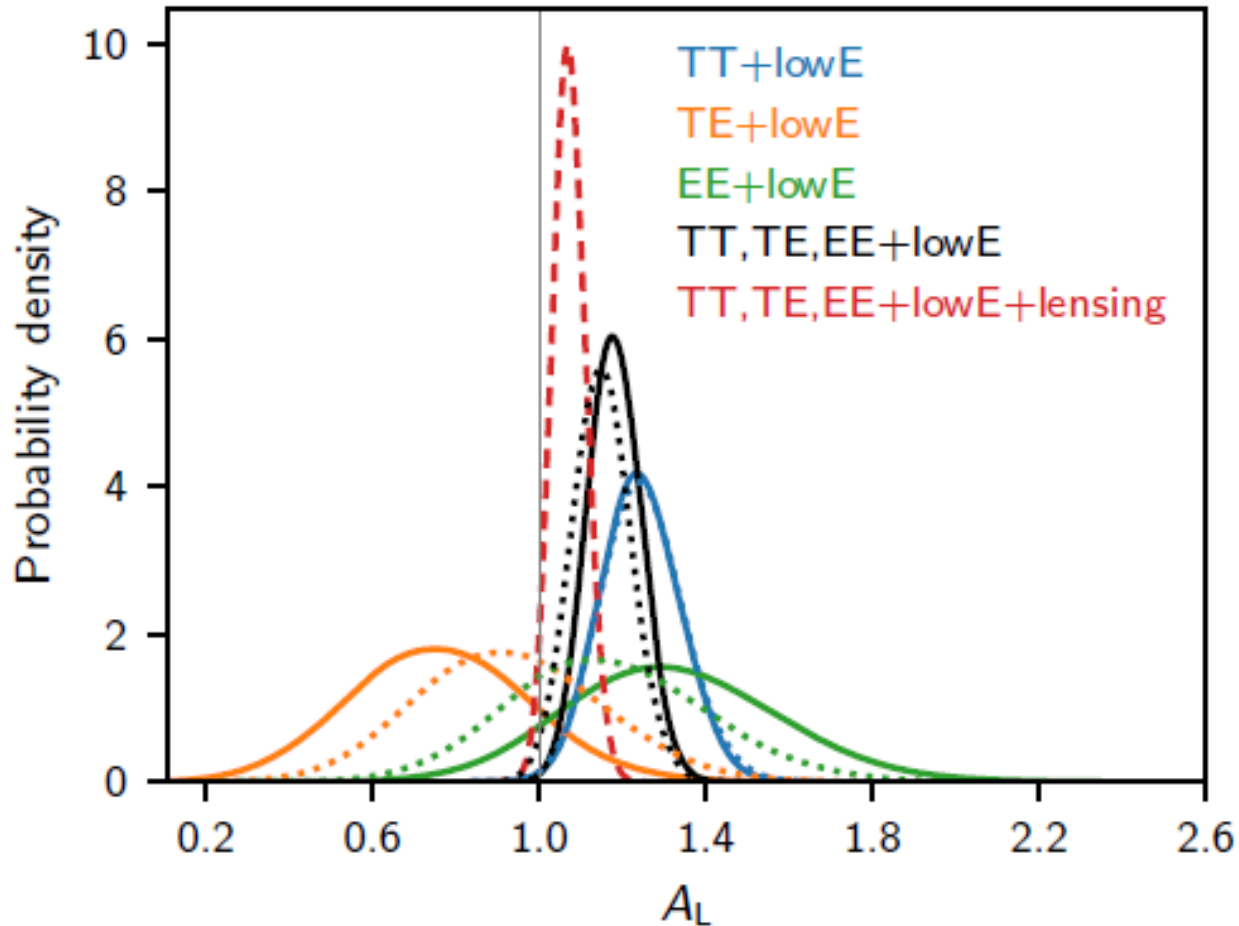


$$E^2(z) = \Omega_m(1+z)^3 + \Omega_\Lambda, \quad (6)$$

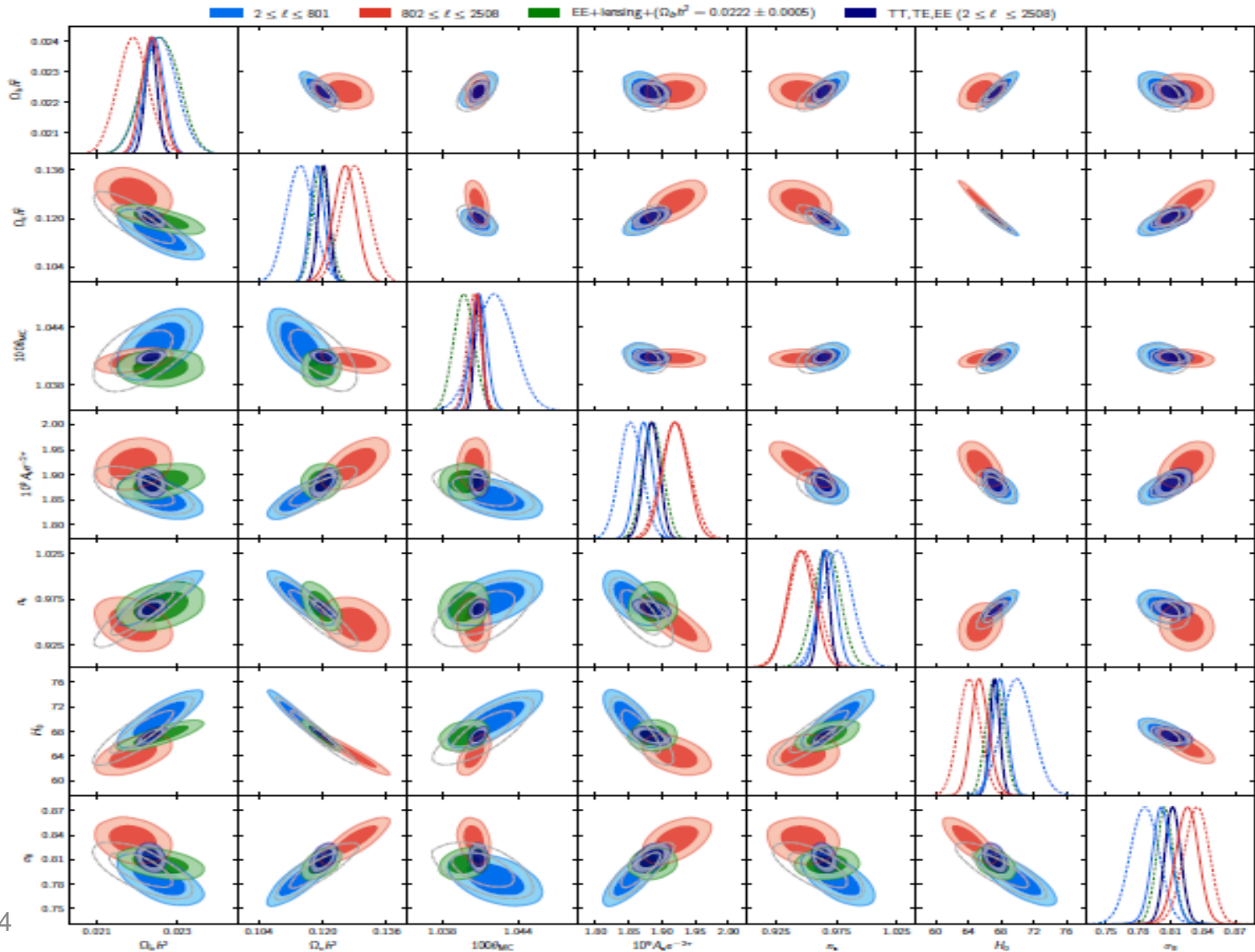
where $E(z) \equiv H(z)/H_0$ and H_0 is Hubble parameter at $z = 0$. For $z < z_\oplus$ we have

$$E^2(z) = \frac{1}{2}\bar{R}_0 + (1 - \frac{1}{2}\bar{R}_0)(1+z)^4 \quad (7)$$

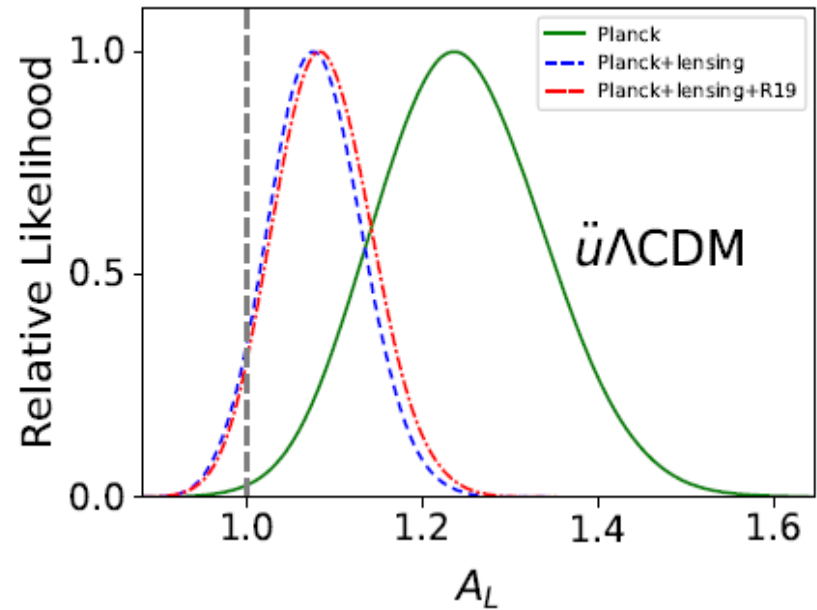
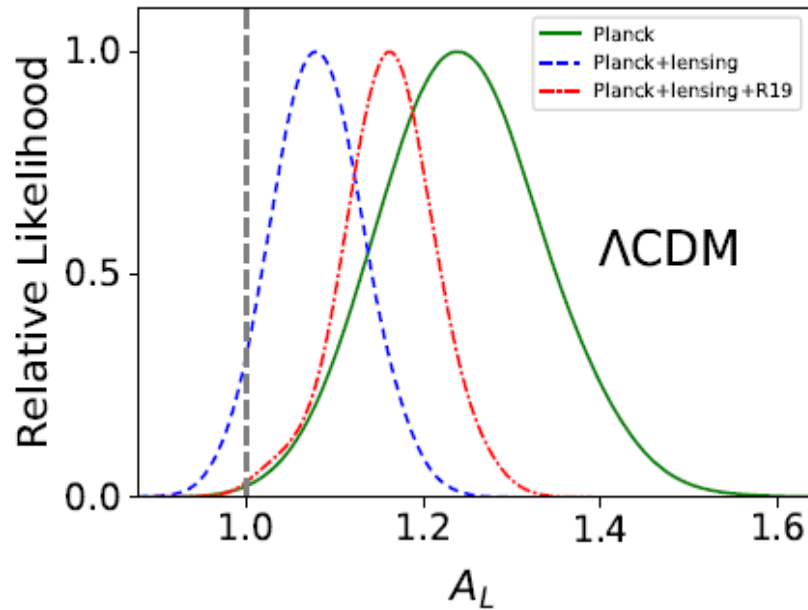
Self consistent CMB?



Self consistent CMB?



H_0 and CMB lensing!



$$\ell^4 C_\ell^{\phi\phi} = 18\Omega_m^2 H_0^4 \int_0^{\chi_*} d\chi \chi^2 \left(\frac{\chi_* - \chi}{\chi_* \chi} \right)^2 P_m^{\ddot{u}}\left(\frac{\ell}{\chi}\right) \times \left[\frac{D^{\ddot{u}}(z)(1+z)}{D^{\ddot{u}}(z=0)\xi(z)} \right]^2,$$

Hossein Moshafi, Shant Baghran,
Nima Khosravi, arXiv:2012.14377

Postlude *

*The final part of a piece; especially music played (normally on the organ)

New ideas in NL-structure formation

- **GRAVITATIONAL WAVE ASTRONOMY!**
- Seed of SMBH

Timothy M. Heckman and Philip N. Best, *Annual Review of Astronomy and Astrophysics* Vol. 52:589-660 (Volume publication date August 2014)

- Quenching of galaxies and mergers

More massive galaxies have systematically older stars

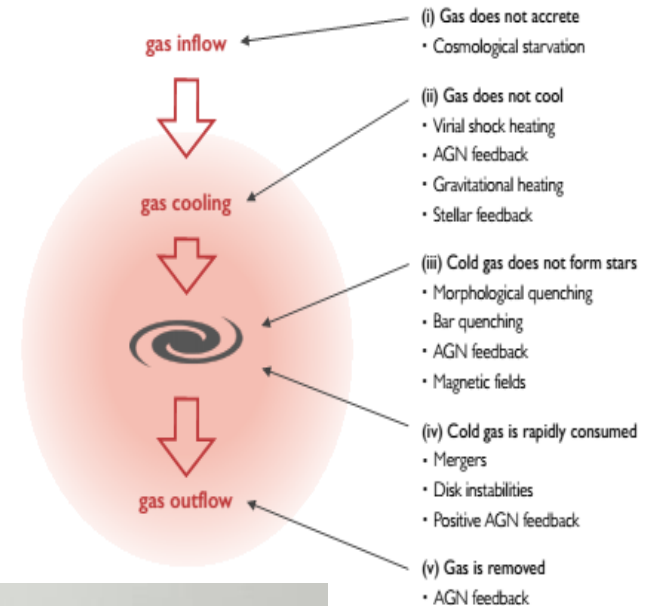
Star formation quenching in massive galaxies Allison Man, Sirio Belli, arXiv:1809.00722

- Flat disk galaxies

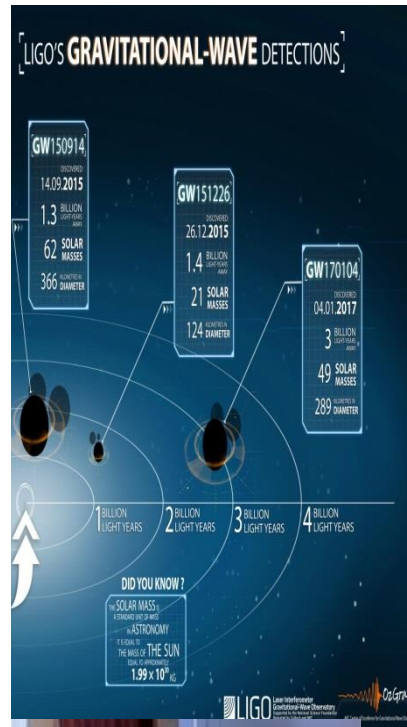
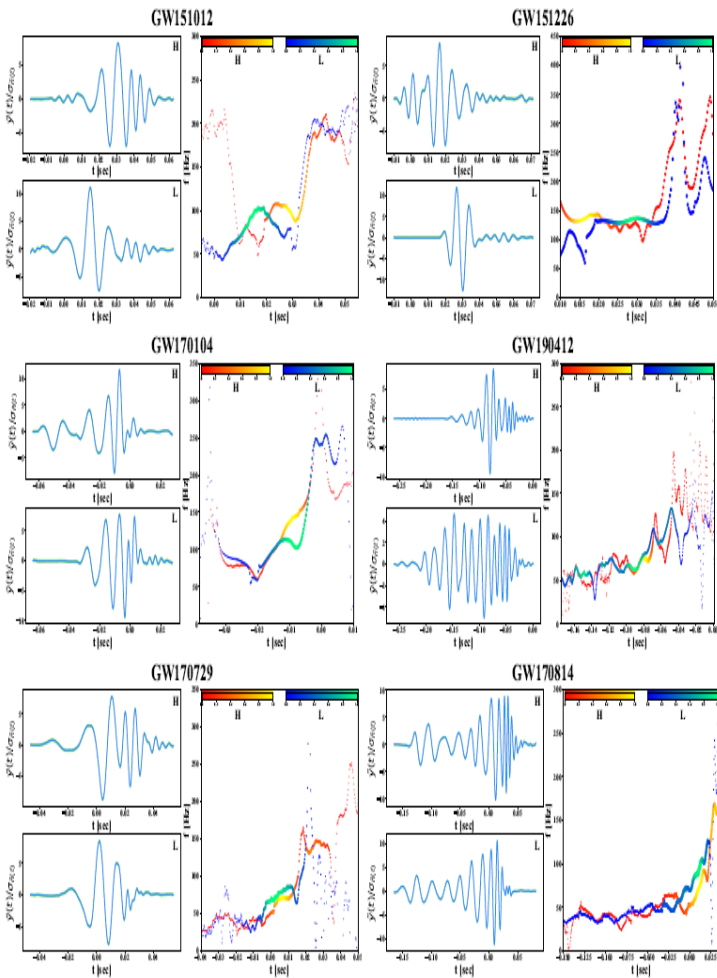
Formation of the Large Nearby Galaxies P. J. E. Peebles, arXiv:2005.07588

Hamed Kameli
PhD candidate in SUT

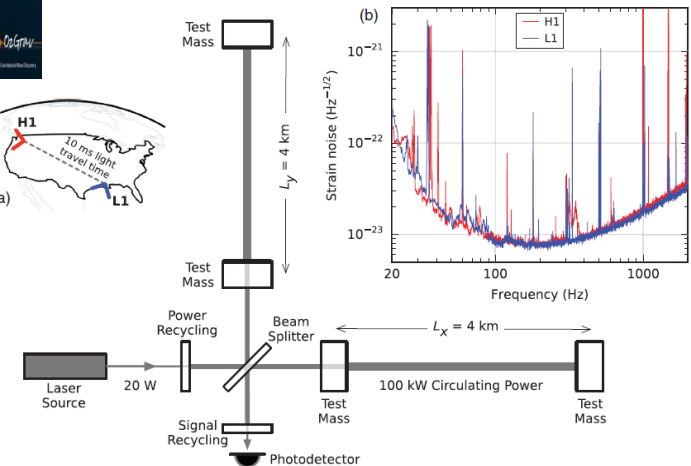
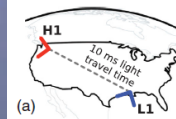
What causes quenching in massive galaxies?



Gravitational Wave Astronomy



H. Arfaei @ SUT

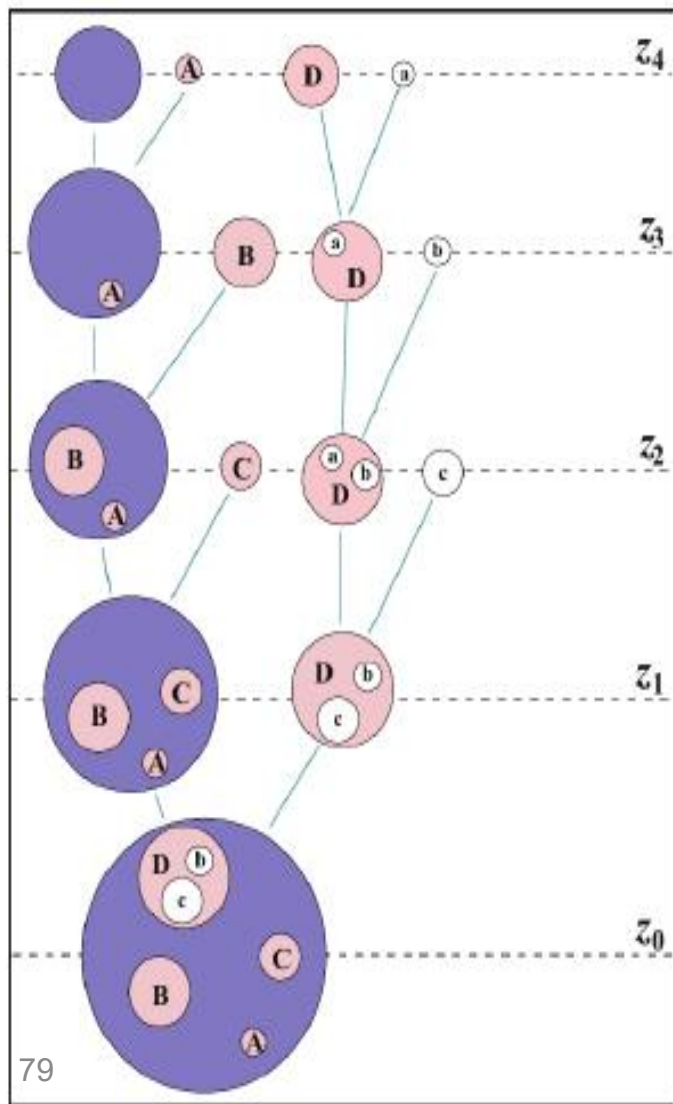


A Data-Driven Approach for the Extraction of Gravitational Waveforms

A. Akhshi¹, H. Alimohammadi^{1,2}, S. Baghrani¹, S. Rahvar¹, M. Reza Rahimi Tabar^{1,3,†}, and H. Arfaei^{1,2}



M. Reza Rahimitabar + Akhshi and Alimohammadi

DM Halo Mergers and emergence of sub-halos

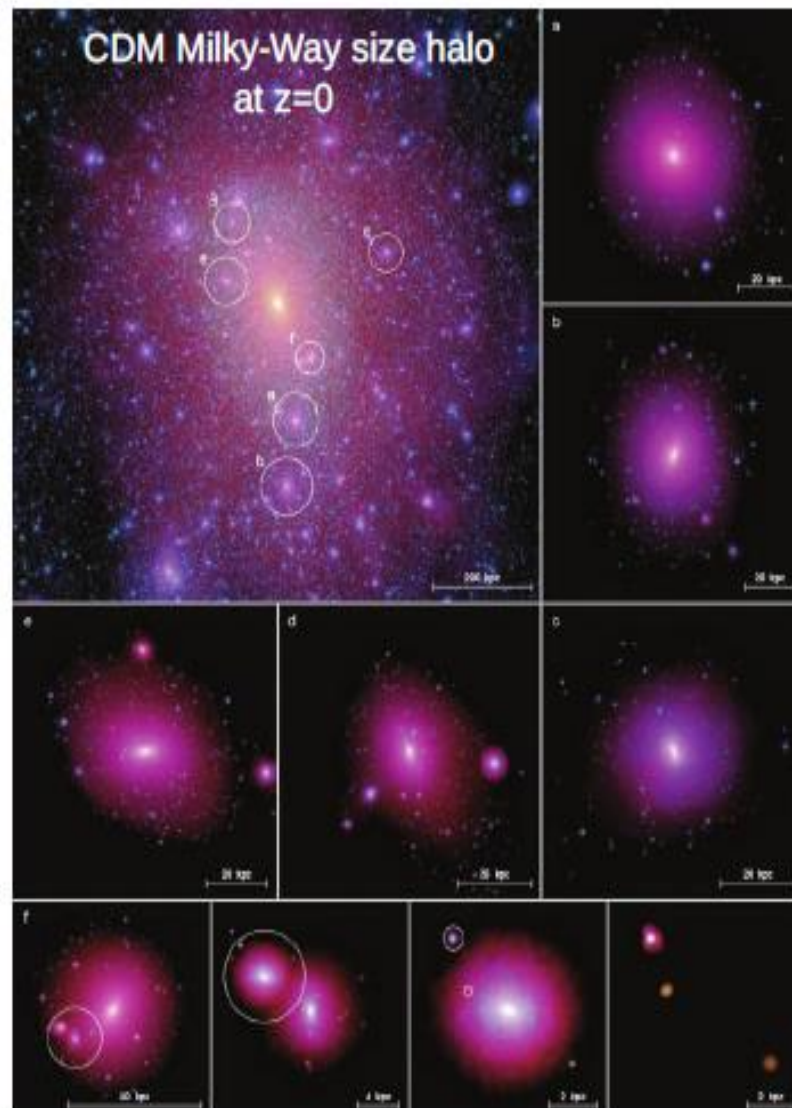


Review

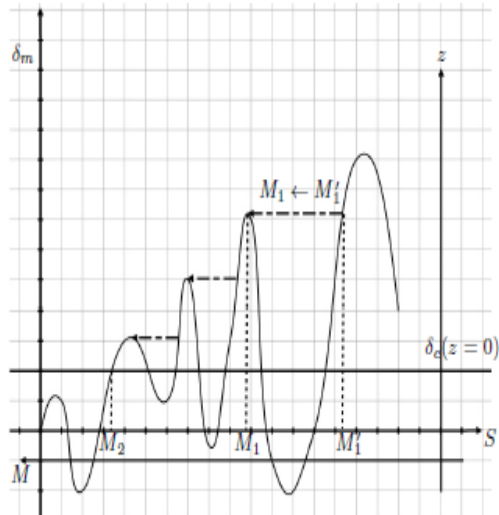
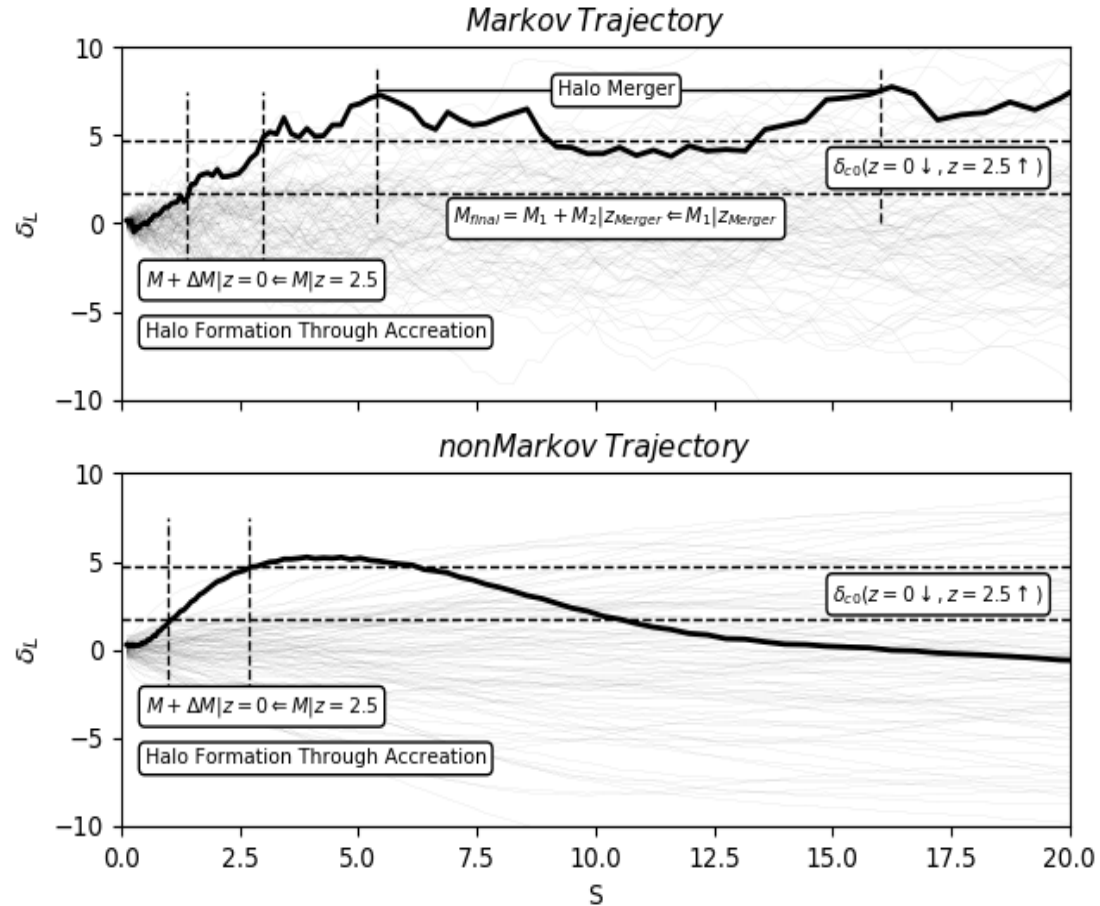
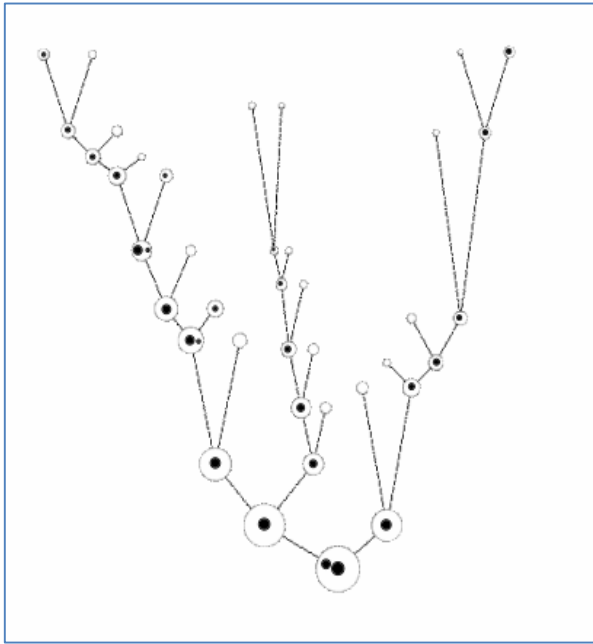
Dark matter haloes and subhaloes

Jesús Zavala¹ , Carlos S. Frenk² 

<https://arxiv.org/pdf/1907.11775.pdf>



Hierarchical Structure Formation and EST

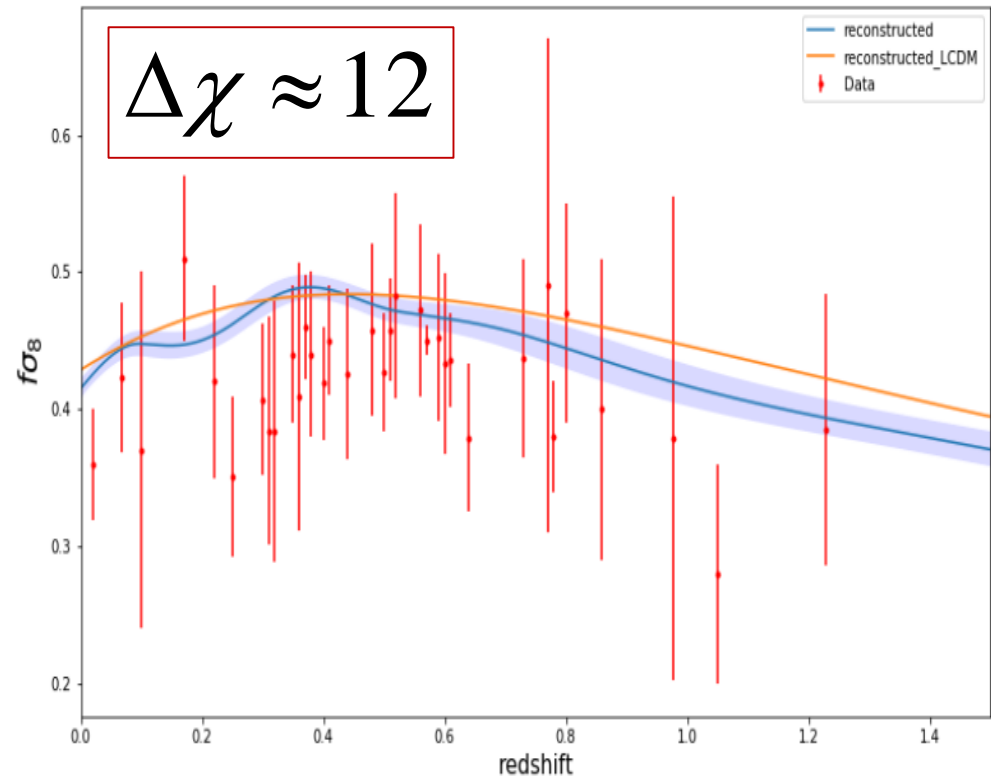


- ❖ Farnik Nikakhtar, Shant Baghram, *Phys. Rev. D* **96**, 043524 (2017)
- ❖ Merger history of dark matter halos in the light of H_0 tension Hamed Kameli, Shant Baghram, arXiv:2008.13175

Reconstructed Hubble parameter and linear theory

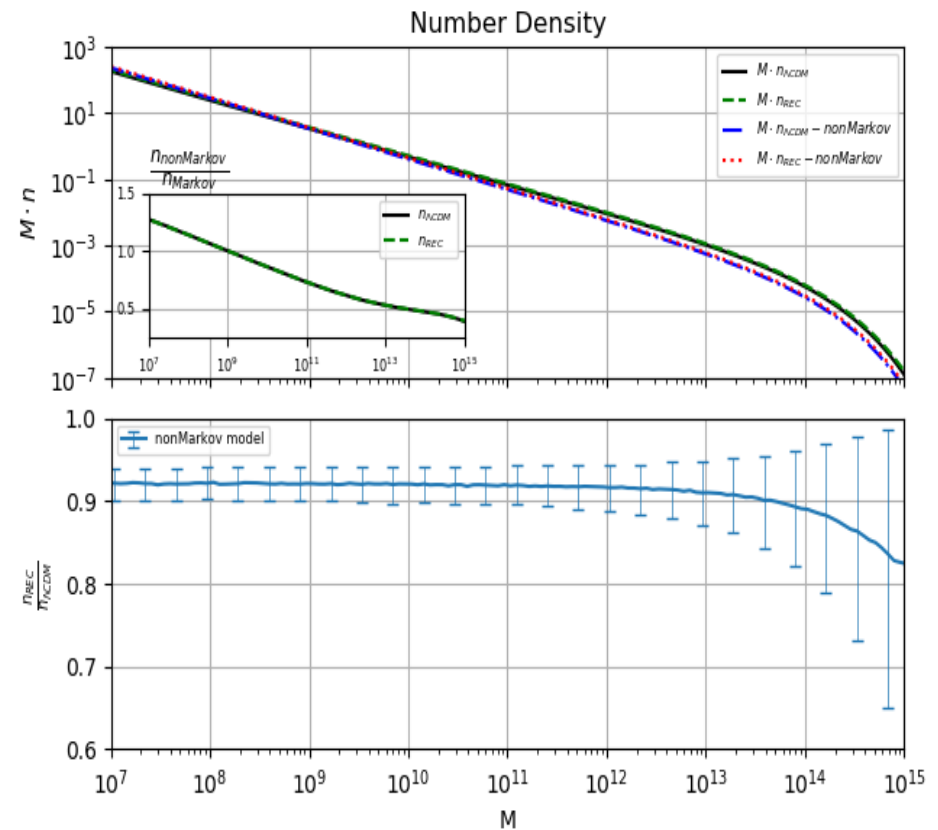
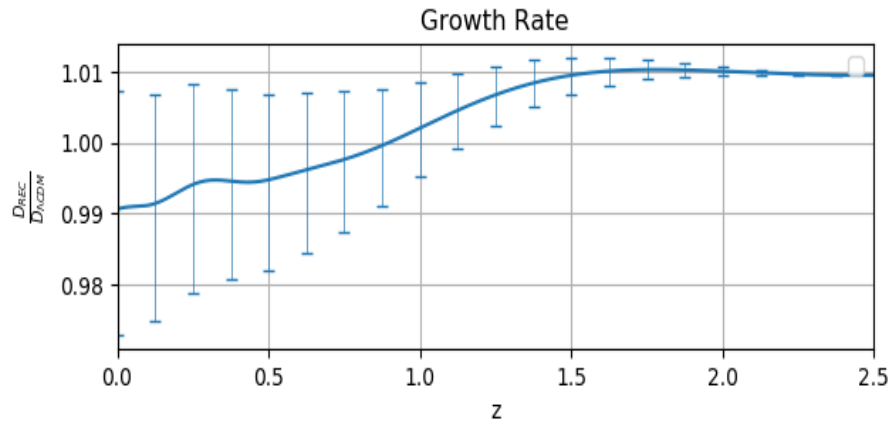
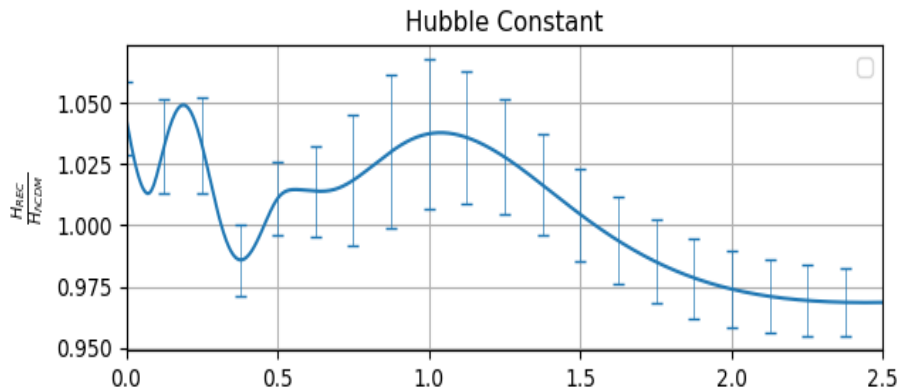
Table I: A compilation of recent RSD data from different surveys.

Index	Dataset	z	$f\sigma_8(z)$	Refs.	Year
1	THF	0.020	0.360 ± 0.0405	[44]	2013
2	6dFGRS	0.067	0.423 ± 0.055	[45]	2012
3	SDSS-veloc	0.100	0.370 ± 0.130	[46]	2015
4	2dFGRS	0.170	0.510 ± 0.060	[47]	2009
5	WiggleZ	0.220	0.420 ± 0.070	[48]	2011
6	SDSS-LRG-200	0.250	0.3512 ± 0.0583	[49]	2012
7	SDSS-BOSS	0.300	0.407 ± 0.055	[50]	2012
8	SDSS-BOSS DR12	0.310	0.384 ± 0.083	[51]	2017
9	BOSS-LOWZ	0.320	0.384 ± 0.095	[52]	2013
10	SDSS-LRG	0.350	0.440 ± 0.050	[47]	2009
11	SDSS-BOSS DR12	0.360	0.409 ± 0.098	[51]	2017
12	SDSS-LRG-200	0.370	0.4602 ± 0.0378	[49]	2011
13	GAMA	0.380	0.440 ± 0.060	[53]	2013
14	SDSS-BOSS	0.400	0.419 ± 0.041	[50]	2012
15	WiggleZ	0.410	0.450 ± 0.040	[48]	2011
16	SDSS-BOSS DR12	0.440	0.426 ± 0.062	[51]	2017
17	SDSS-BOSS DR12	0.480	0.458 ± 0.063	[51]	2017
18	SDSS-BOSS	0.500	0.427 ± 0.043	[50]	2012
19	BOSS DR12	0.510	0.458 ± 0.038	[54]	2016
20	SDSS-BOSS DR12	0.520	0.483 ± 0.075	[51]	2017
21	SDSS-BOSS DR12	0.560	0.472 ± 0.063	[51]	2017
22	SDSS-LRG-200	0.570	0.423 ± 0.052	[55]	2014
23	SDSS-BOSS DR12	0.590	0.452 ± 0.061	[51]	2017
24	SDSS-BOSS	0.600	0.433 ± 0.067	[50]	2012
25	BOSS DR12	0.610	0.436 ± 0.034	[54]	2016
26	SDSS-BOSS DR12	0.640	0.379 ± 0.054	[51]	2017
27	WiggleZ	0.730	0.437 ± 0.072	[56]	2012
28	VVDS	0.770	0.490 ± 0.018	[47]	2009
29	Vipers	0.800	0.470 ± 0.080	[57]	2013
30	Vipers PDR-2	0.860	0.400 ± 0.110	[58]	2016
31	eBOSS DR14	0.978	0.379 ± 0.176	[59]	2018
32	Vipers v7	1.050	0.280 ± 0.080	[60]	2016
33	eBOSS DR14	1.230	0.385 ± 0.099	[59]	2018
34	eBOSS DR14	1.526	0.342 ± 0.070	[59]	2018
35	eBOSS DR14	1.944	0.364 ± 0.106	[59]	2018



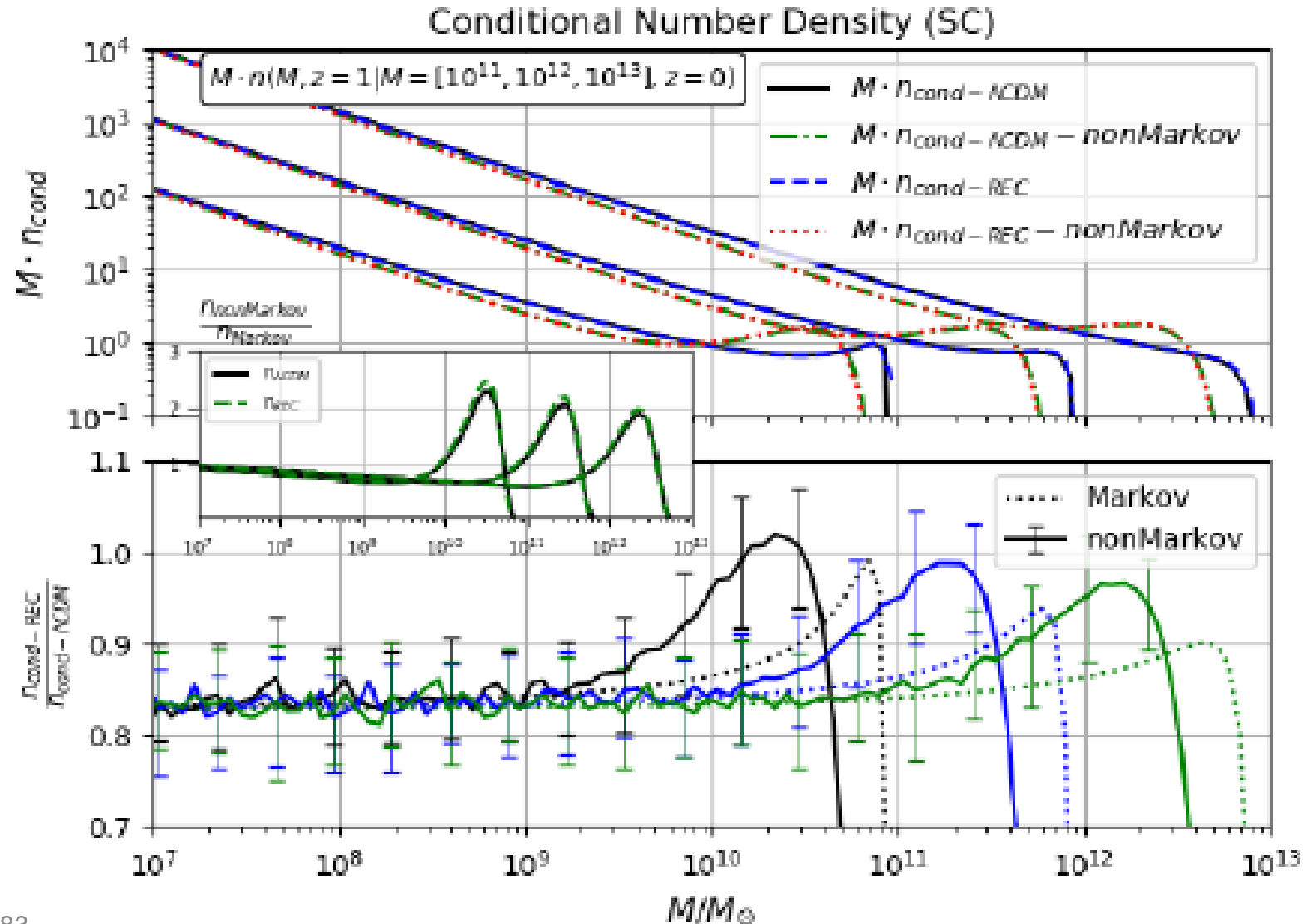
© Laya Parkavosi

From Reconstructed Hubble to DM halos

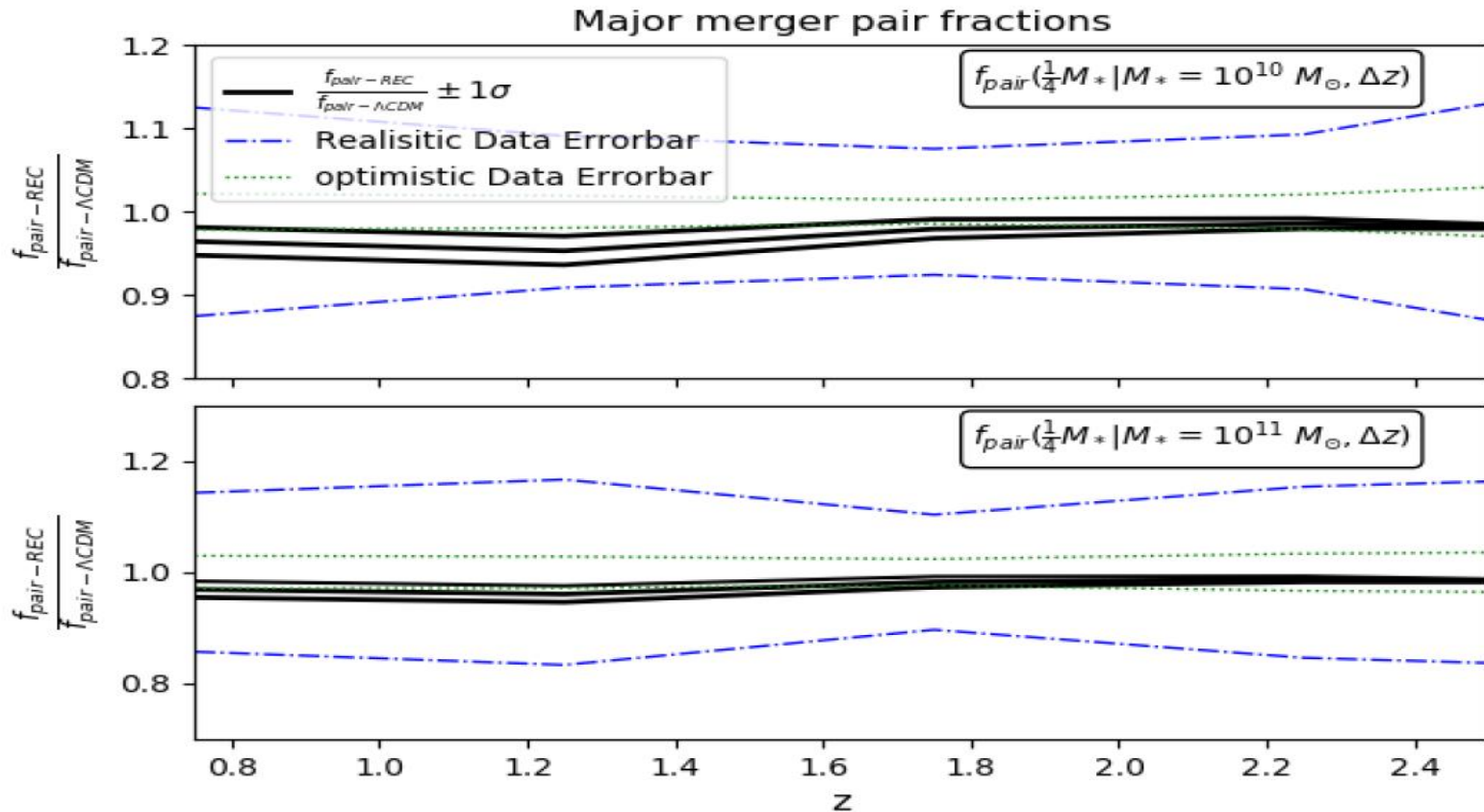


$$\begin{aligned}
 f_{\text{FU}}(S_2, \delta_2 | S_1, \delta_1) dS_2 &= \frac{f_{\text{FU}}(S_1, \delta_1 | S_2, \delta_2) f_{\text{FU}}(S_2, \delta_2)}{f_{\text{FU}}(S_1, \delta_1)} dS_2 \\
 &= \frac{1}{\sqrt{2\pi}} \frac{\delta_2(\delta_1 - \delta_2)}{\delta_1} \left[\frac{S_1}{S_2(S_1 - S_2)} \right]^{3/2} \exp \left[-\frac{(\delta_2 S_1 - \delta_1 S_2)^2}{2S_1 S_2 (S_1 - S_2)} \right] dS_2
 \end{aligned}$$

Merger Rate and observations



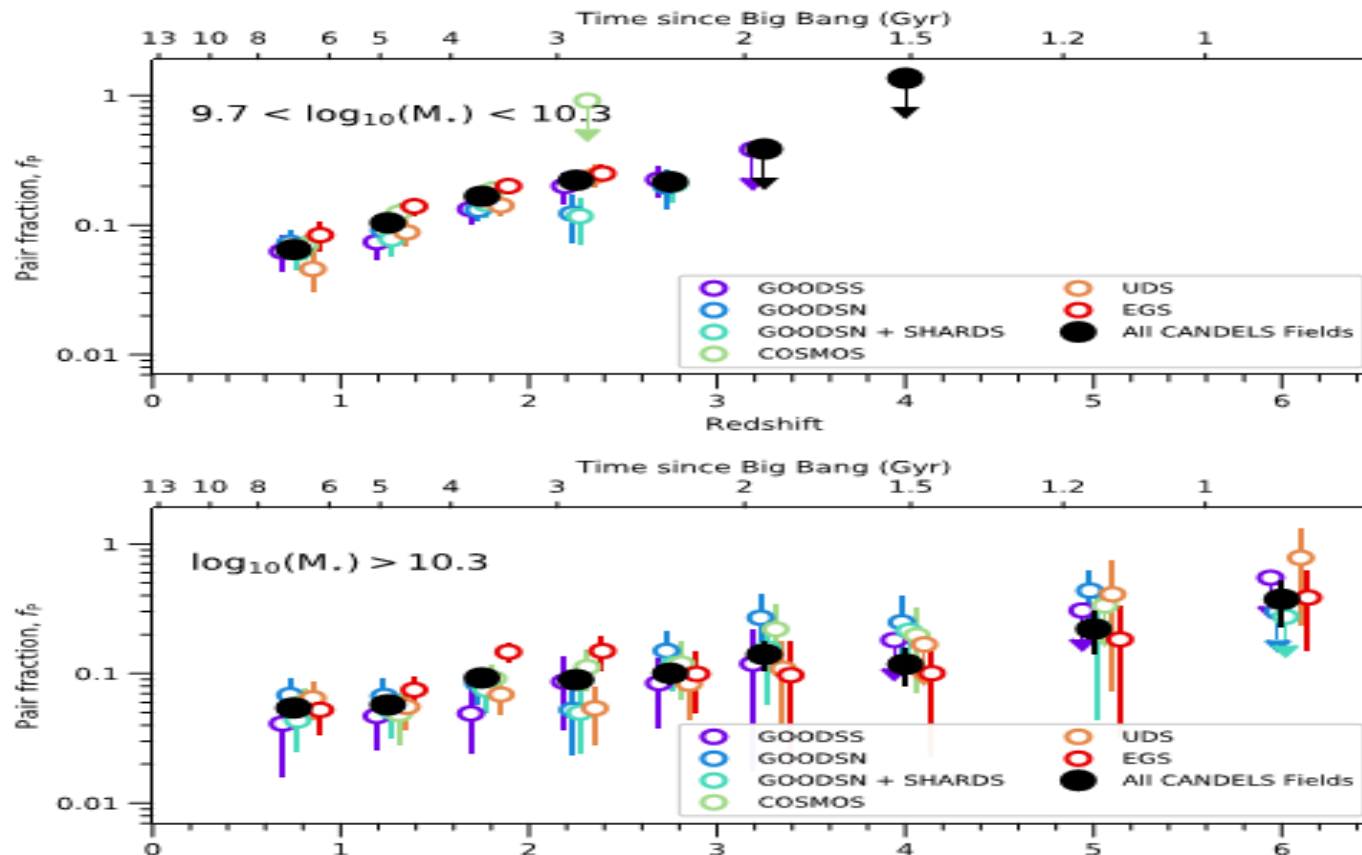
conclude: Merger rate can be a new probe of H_0



Observational constraints on the merger history of galaxies since $z \approx 6$:
 Probabilistic galaxy pair counts in the CANDELS fields

KENNETH DUNCAN,^{1,2} CHRISTOPHER J. CONSELICE,² CARL MUNDY,² ERIC BELL,³ JENNIFER DONLEY,⁴
 AUDREY GALAMETZ,⁵ YICHENG GUO,⁶ NORMAN A. GROGIN,⁷ NIMISH HATHI,⁷ JEYHAN KARTALTEPE,⁸ DALE KOCEVSKI,⁹
 ANTON M. KOEKEMOER,⁷ PABLO G. PÉREZ-GONZÁLEZ,^{10,11} KAMESWARA B. MANTHA,¹² GREGORY F. SNYDER,⁷ AND
 MAURO STEFANON¹

Observation: Merger rate can be a new probe of H_0



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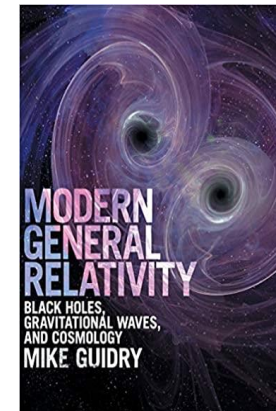
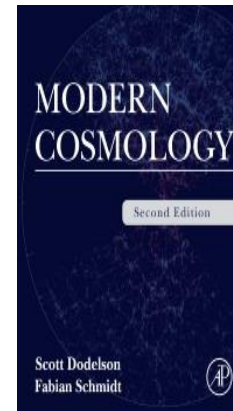
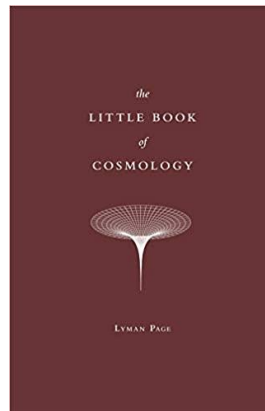
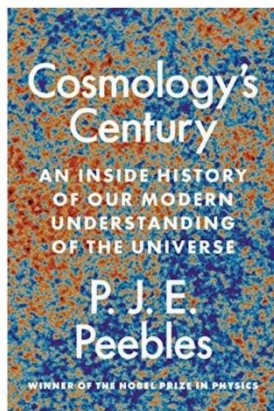
Conclusion and F.R.

- I. General relativity and the Universe
Asking for a Homogenous and Isotropic one!
- II. **Expanding Universe and measuring Ω**
- III. Cosmic Microwave Background Radiation
- IV. **Structure Formation and LSS**
- V. **Subluminal matter**
- VI. **Non-baryonic Dark Matter**

- ❖ A more sophisticated version of EST to study non-linear structure formation \rightarrow Voids, galaxy-DM relation, ...
 - ❖ Filaments in ESS context
- ❖ Developing the methods to look at cosmic web
 - ❖ Statistics of PBH as a DM
- ❖ Observational proposal for DM in galactic scale
 - ❖ Uber-gravity hint to H_0
 - ❖ Reconstructed H_0 merger tree and LSS

An updated reviews and books

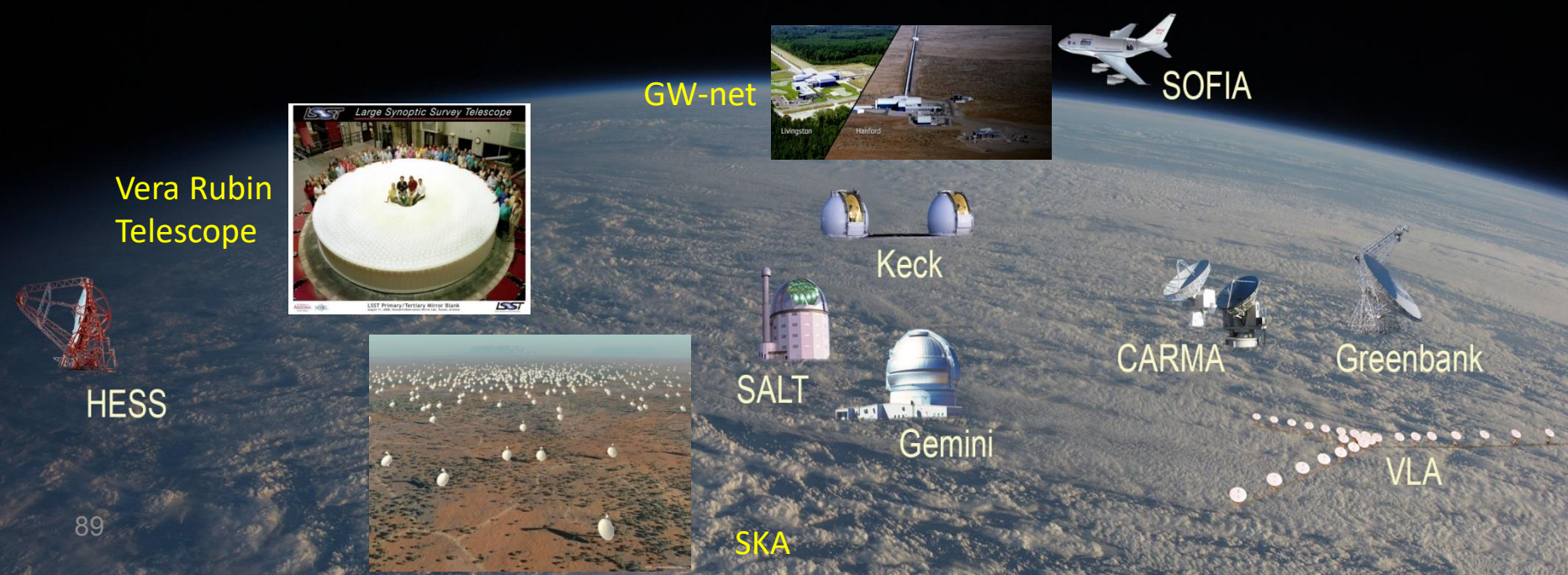
- <http://sharif.edu/~baghram/talks.html>
- ❑ In the Realm of the Hubble tension – a Review of Solutions; Eleonora Di Valentino, et al. <https://arxiv.org/abs/2103.01183>.
- ❑ Challenges for Λ CDM: An update Leandros Perivolaropoulos, Foteini Skara <https://arxiv.org/abs/2105.05208>
- ❑ Primordial Black Holes as Dark Matter: Recent Developments Bernard Carr, Florian Kuhnel <https://arxiv.org/abs/2006.02838>
- ❑ Dark matters on the scale of galaxies Ivan de Martino, Sankha S. Chakrabarty, Valentina Cesare, Arianna Gallo, Luisa Ostorero, Antonaldo Diaferio et al. <https://arxiv.org/abs/2007.15539>







gamma ray X-ray ultraviolet visible infrared microwave radio



Final Word!

- Probably Tensions will open new possibilities
- LSST (V. Rubin) + EULCID + WFIRST (Nancy Roman)+ JWT + eLISA+ SKA + GAIA + ... + Big data + ML+...
- More insight to Structure Formation is crucial!
- GW Astronomy is just here !!!



A little and a little, collected together, become a great deal; the heap in the barn consists of single grains, and drop and drop make the inundation. Saadi